Physics 369-011 Quantum Mechanics II

Lehigh University, Spring 2023

Instructor: Ariel Sommer

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Office hours: by appointment (please email)

Class: Tues/Thurs 1:35 - 2:50 pm

Room: Lewis 512

Course Overview

The first course in a two-semester sequence on quantum mechanics at the graduate level. This course reviews the basic structure and applications of quantum mechanics while introducing some more advanced concepts.

Textbook: Sakurai and Napolitano, Modern Quantum Mechanics, 3rd ed., Cambridge, 2021

Additional reference (both free online through Lehigh library)

- Ballentine, Quantum mechanics: a modern development, World Scientific, 2015
- Mathur and Singh, Concepts in quantum mechanics, CRC 2008

Course Outline

Topics not typically covered in undergraduate courses are highlighted in bold below.

- Ch 1: Fundamentals of quantum mechanics
 - o Bra-ket notation, state vectors, operators, generalized uncertainty principle
 - Momentum and translation operators, wavefunctions
- Ch 2: Dynamics
 - Schrodinger equations, Heisenberg picture
 - Harmonic oscillator, solutions to Schrodinger wave equations
- Ch 3: Angular momentum and rotation
 - o Rotation operators, angular momentum algebra and eigenstates
 - o Orbital angular momentum, central potentials, and hydrogen atom
 - o Addition of angular momentum, Clebsch-Gordan coefficients
 - Density operators

Homework: Homework will be assigned weekly. You are expected to turn in homework on time. You may work together on the homework, but make sure that you are able to complete the problems on your own. The work you turn in must be your own.

Late homework: Please contact me if you would like to request an extension due to illness or other circumstances.

Exams: The course will have two midterm exams, plus a final exam.

Grading: Final grades in the course will be based on attendance (10%), homework (40%), midterms (20%), and the final exam (30%).

Learning Outcomes:

Students will learn the following skills.

Ch 1:

- Apply the postulates of quantum mechanics to describe quantum systems using state vectors, and calculate measurement probabilities
- Calculate the eigenstates and eigenvalues of observables
- Convert between matrix and bra-ket representations of state vectors and operators
- Determine whether two observables are compatible and apply the uncertainty principle
- Apply a change of basis to a representation of a state vector or operator
- Understand the displacement operator and its relation to the momentum operator

Ch 2:

- Express time evolution in terms of the time-evolution operator and Schrodinger equation
- Calculate the time-dependence of a state vector by expanding in energy eigenstates
- Calculate the time-dependence of expectation values
- Convert between the Schrodinger picture and the Heisenberg picture
- Calculate the time-dependence of operators in the Heisenberg picture
- Understand the connection between the Heisenberg picture and classical physics
- Employ ladder operators to calculate properties of harmonic oscillator systems
- Solve the Schrodinger wave equation for constant potentials
- Employ special functions to work with solutions of wave equations

Ch 3:

- Understand how rotation operators relate to angular momentum operators
- Apply rotations to spin-½ systems, employ Pauli matrices to represent observables
- Describe mixed ensembles using density operators
- Know the eigenvalues and eigenstates of general angular momentum operators
- Compute matrix representations of angular momentum operators
- Understand spherical harmonics and the radial equation for central potentials
- Non-relativistic hydrogen: understand the quantum numbers
- Know the rules of angular momentum addition
- Compute Clebsch-Gordan coefficients and employ them to solve problems

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