

Supplementary Material Table 1 – Global fit rate coefficients ($k_p^{\Delta J}$) in units of the radiative rate Γ and in units of cm^3s^{-1} [the latter obtained by multiplying the fitted parameters ($k_p^{\Delta J}/\Gamma$) by $\Gamma = 4.4 \times 10^7 \text{ s}^{-1}$] for rotationally inelastic collisions of NaK $2(A)^1\Sigma^+(v = 16, J = 30)$ molecules with argon, helium, and potassium atoms ($p = Ar, He, \text{ and } K$). Quenching rate coefficients are also given.

| ΔJ | $k_{Ar}^{\Delta J}/\Gamma$ (10^{-18} cm^3) | $k_{He}^{\Delta J}/\Gamma$ (10^{-18} cm^3) | $k_K^{\Delta J}/\Gamma$ (10^{-17} cm^3) | $k_{Ar}^{\Delta J}$ ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | $k_{He}^{\Delta J}$ ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | $k_K^{\Delta J}$ ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
|------------|---|---|--|---|---|--|
| -4 | 2.08 ± 0.15 | 2.47 ± 0.15 | 0.35 ± 0.04 | 9.16 ± 0.68 | 10.89 ± 0.66 | 1.56 ± 0.20 |
| -3 | 1.57 ± 0.12 | 0.53 ± 0.05 | 0.45 ± 0.05 | 6.93 ± 0.54 | 2.32 ± 0.22 | 1.97 ± 0.22 |
| -2 | 4.57 ± 0.31 | 4.51 ± 0.27 | 0.82 ± 0.09 | 20.13 ± 1.36 | 19.84 ± 1.18 | 3.61 ± 0.38 |
| -1 | 2.33 ± 0.16 | 0.98 ± 0.08 | 1.11 ± 0.11 | 10.23 ± 0.72 | 4.29 ± 0.36 | 4.90 ± 0.46 |
| 0 | | | | | | |
| 1 | 1.88 ± 0.15 | 0.91 ± 0.11 | 1.87 ± 0.16 | 8.25 ± 0.65 | 4.02 ± 0.51 | 8.24 ± 0.71 |
| 2 | 4.45 ± 0.28 | 4.57 ± 0.28 | 1.57 ± 0.15 | 19.57 ± 1.24 | 20.09 ± 1.22 | 6.91 ± 0.66 |
| 3 | 1.20 ± 0.09 | 0.76 ± 0.06 | 0.53 ± 0.06 | 5.27 ± 0.40 | 3.35 ± 0.28 | 2.35 ± 0.25 |
| 4 | 1.95 ± 0.14 | 2.62 ± 0.16 | 0.38 ± 0.05 | 8.59 ± 0.61 | 11.54 ± 0.71 | 1.66 ± 0.24 |
| | k_{Ar}^Q/Γ (10^{-18} cm^3) | k_{He}^Q/Γ (10^{-18} cm^3) | k_K^Q/Γ (10^{-17} cm^3) | k_{Ar}^Q ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | k_{He}^Q ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | k_K^Q ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
| | 28.1 ± 2.5 | 41.5 ± 3.4 | 26.9 ± 2.8 | 123.7 ± 11.0 | 182.6 ± 15.0 | 118.5 ± 12.5 |

Supplementary Material Table 2 – Global fit fraction of orientation destroyed ($f_p^{\Delta J}$) for rotationally inelastic collisions of NaK $2(A)^1\Sigma^+(v = 16, J = 30)$ molecules with argon, helium, and potassium atoms ($p = Ar, He, \text{ and } K$), and g'_p values obtained from Eq. 37.

| ΔJ | $f_{Ar}^{\Delta J}$ | $f_{He}^{\Delta J}$ | $f_K^{\Delta J}$ |
|------------|---|---|--|
| -4 | 0.67 ± 0.04 | 0.61 ± 0.06 | 0.94 ± 0.04 |
| -3 | 0.64 ± 0.06 | 0.00 ± 0.35 | 0.84 ± 0.06 |
| -2 | 0.47 ± 0.04 | 0.26 ± 0.05 | 0.91 ± 0.02 |
| -1 | 0.46 ± 0.05 | 0.26 ± 0.17 | 0.96 ± 0.01 |
| 1 | 0.37 ± 0.05 | 0.00 ± 0.21 | 0.94 ± 0.01 |
| 2 | 0.57 ± 0.02 | 0.25 ± 0.05 | 0.93 ± 0.01 |
| 3 | 0.62 ± 0.05 | 0.00 ± 0.28 | 0.90 ± 0.05 |
| 4 | 0.58 ± 0.05 | 0.11 ± 0.09 | 1.00 ± 0.13 |
| | g'_{Ar} ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | g'_{He} ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | g'_K ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
| | 3.89 (fixed) | 0.56 (fixed) | 6.23 (fixed) |

Supplementary Material Table 3 – Separate buffer gas fit rate coefficients ($k_p^{\Delta J}$) in units of the radiative rate Γ and in units of cm^3s^{-1} [the latter obtained by multiplying the fitted parameters ($k_p^{\Delta J}/\Gamma$) by $\Gamma = 4.4 \times 10^7 \text{ s}^{-1}$] for rotationally inelastic collisions of NaK $2(A)^1\Sigma^+(v = 16, J = 30)$ molecules with argon, helium, and potassium atoms ($p = Ar, He, \text{ and } K$). Quenching rate coefficients are also given.

| ΔJ | $k_{Ar}^{\Delta J}/\Gamma$ (10^{-18} cm^3) | $k_{He}^{\Delta J}/\Gamma$ (10^{-18} cm^3) | $k_K^{\Delta J}/\Gamma$ (10^{-17} cm^3) | $k_{Ar}^{\Delta J}$ ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | $k_{He}^{\Delta J}$ ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | $k_K^{\Delta J}$ ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
|------------|---|---|--|---|---|--|
| -4 | 2.11 ± 0.17 | 2.52 ± 0.13 | 0.37 ± 0.05 | 9.28 ± 0.73 | 11.07 ± 0.59 | 1.64 ± 0.23 |
| -3 | 1.59 ± 0.13 | 0.52 ± 0.05 | 0.48 ± 0.06 | 6.99 ± 0.57 | 2.31 ± 0.22 | 2.12 ± 0.27 |
| -2 | 4.64 ± 0.34 | 4.59 ± 0.24 | 0.85 ± 0.10 | 20.43 ± 1.48 | 20.19 ± 1.07 | 3.75 ± 0.46 |
| -1 | 2.37 ± 0.17 | 0.99 ± 0.08 | 1.14 ± 0.13 | 10.43 ± 0.77 | 4.38 ± 0.36 | 5.00 ± 0.58 |
| 0 | | | | | | |
| 1 | 1.86 ± 0.15 | 0.90 ± 0.11 | 2.00 ± 0.21 | 8.18 ± 0.67 | 3.94 ± 0.50 | 8.80 ± 0.92 |
| 2 | 4.49 ± 0.30 | 4.62 ± 0.25 | 1.68 ± 0.19 | 19.74 ± 1.33 | 20.32 ± 1.10 | 7.37 ± 0.85 |
| 3 | 1.21 ± 0.10 | 0.77 ± 0.06 | 0.56 ± 0.07 | 5.32 ± 0.42 | 3.37 ± 0.26 | 2.49 ± 0.31 |
| 4 | 1.98 ± 0.15 | 2.67 ± 0.14 | 0.40 ± 0.06 | 8.71 ± 0.66 | 11.74 ± 0.63 | 1.75 ± 0.28 |
| | k_{Ar}^Q/Γ (10^{-18} cm^3) | k_{He}^Q/Γ (10^{-18} cm^3) | k_K^Q/Γ (10^{-17} cm^3) | k_{Ar}^Q ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | k_{He}^Q ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | k_K^Q ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
| | 28.4 ± 2.6 | 42.2 ± 3.3 | 28.4 ± 3.6 | 125.2 ± 11.6 | 185.6 ± 14.5 | 125.1 ± 15.9 |

Supplementary Material Table 4 – Separate buffer gas fit fraction of orientation destroyed ($f_p^{\Delta J}$) for rotationally inelastic collisions of NaK $2(A)^1\Sigma^+(v = 16, J = 30)$ molecules with argon, helium, and potassium atoms ($p = Ar, He, \text{ and } K$), and g'_p values obtained from Eq. 37.

| ΔJ | $f_{Ar}^{\Delta J}$ | $f_{He}^{\Delta J}$ | $f_K^{\Delta J}$ |
|------------|---|---|--|
| -4 | 0.67 ± 0.04 | 0.60 ± 0.06 | 0.94 ± 0.04 |
| -3 | 0.62 ± 0.06 | 0.00 ± 0.35 | 0.86 ± 0.06 |
| -2 | 0.47 ± 0.04 | 0.25 ± 0.05 | 0.90 ± 0.02 |
| -1 | 0.45 ± 0.05 | 0.26 ± 0.17 | 0.96 ± 0.01 |
| 1 | 0.35 ± 0.05 | 0.00 ± 0.21 | 0.94 ± 0.01 |
| 2 | 0.56 ± 0.03 | 0.24 ± 0.05 | 0.93 ± 0.01 |
| 3 | 0.60 ± 0.06 | 0.00 ± 0.28 | 0.91 ± 0.05 |
| 4 | 0.58 ± 0.05 | 0.10 ± 0.09 | 1.00 ± 0.13 |
| | g'_{Ar} ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | g'_{He} ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | g'_K ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
| | 3.80 (fixed) | 0.58 (fixed) | 6.55 (fixed) |

Supplementary Material Table 5 – Fluorescence and polarization fit rate coefficients ($k_p^{\Delta J}$) in units of the radiative rate Γ and in units of cm^3s^{-1} [the latter obtained by multiplying the fitted parameters ($k_p^{\Delta J}/\Gamma$) by $\Gamma = 4.4 \times 10^7 \text{ s}^{-1}$] for rotationally inelastic collisions of NaK $2(A)^1\Sigma^+(v = 16, J = 30)$ molecules with argon, helium, and potassium atoms ($p = Ar, He, \text{ and } K$). Quenching rate coefficients are also given.

| ΔJ | $k_{Ar}^{\Delta J}/\Gamma$ (10^{-18} cm^3) | $k_{He}^{\Delta J}/\Gamma$ (10^{-18} cm^3) | $k_K^{\Delta J}/\Gamma$ (10^{-17} cm^3) | $k_{Ar}^{\Delta J}$ ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | $k_{He}^{\Delta J}$ ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | $k_K^{\Delta J}$ ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
|------------|---|---|--|---|---|--|
| -4 | 2.00 ± 0.13 | 2.20 ± 0.11 | 0.21 ± 0.03 | 8.80 ± 0.58 | 9.69 ± 0.49 | 0.91 ± 0.14 |
| -3 | 1.55 ± 0.11 | 0.50 ± 0.04 | 0.28 ± 0.04 | 6.80 ± 0.47 | 2.19 ± 0.18 | 1.22 ± 0.16 |
| -2 | 4.44 ± 0.27 | 4.03 ± 0.20 | 0.49 ± 0.06 | 19.54 ± 1.18 | 17.72 ± 0.88 | 2.16 ± 0.27 |
| -1 | 2.32 ± 0.15 | 0.97 ± 0.07 | 0.69 ± 0.08 | 10.22 ± 0.66 | 4.27 ± 0.29 | 3.03 ± 0.34 |
| 0 | | | | | | |
| 1 | 1.97 ± 0.14 | 0.92 ± 0.09 | 1.23 ± 0.12 | 8.65 ± 0.62 | 4.06 ± 0.40 | 5.39 ± 0.53 |
| 2 | 4.41 ± 0.26 | 4.15 ± 0.21 | 0.97 ± 0.11 | 19.42 ± 1.12 | 18.27 ± 0.93 | 4.27 ± 0.49 |
| 3 | 1.18 ± 0.08 | 0.71 ± 0.05 | 0.34 ± 0.04 | 5.17 ± 0.35 | 3.11 ± 0.22 | 1.49 ± 0.19 |
| 4 | 1.85 ± 0.12 | 2.32 ± 0.12 | 0.22 ± 0.04 | 8.14 ± 0.51 | 10.21 ± 0.53 | 0.95 ± 0.17 |
| | k_{Ar}^Q/Γ (10^{-18} cm^3) | k_{He}^Q/Γ (10^{-18} cm^3) | k_K^Q/Γ (10^{-17} cm^3) | k_{Ar}^Q ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | k_{He}^Q ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | k_K^Q ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
| | 29.5 ± 2.4 | 37.8 ± 2.6 | 14.8 ± 2.0 | 129.7 ± 10.4 | 166.1 ± 11.5 | 65.2 ± 8.7 |

Supplementary Material Table 6 – Fluorescence and polarization fit fraction of orientation destroyed ($f_p^{\Delta J}$) for rotationally inelastic collisions of NaK $2(A)^1\Sigma^+(v = 16, J = 30)$ molecules with argon, helium, and potassium atoms ($p = Ar, He, \text{ and } K$), and g'_p values obtained from Eq. 37.

| ΔJ | $f_{Ar}^{\Delta J}$ | $f_{He}^{\Delta J}$ | $f_K^{\Delta J}$ |
|------------|---|---|--|
| -4 | 0.73 ± 0.03 | 0.62 ± 0.06 | 0.95 ± 0.05 |
| -3 | 0.69 ± 0.04 | 0.00 ± 0.31 | 0.85 ± 0.06 |
| -2 | 0.56 ± 0.02 | 0.28 ± 0.05 | 0.90 ± 0.02 |
| -1 | 0.55 ± 0.03 | 0.33 ± 0.14 | 0.97 ± 0.01 |
| 1 | 0.48 ± 0.02 | 0.00 ± 0.15 | 0.95 ± 0.01 |
| 2 | 0.62 ± 0.01 | 0.31 ± 0.04 | 0.94 ± 0.02 |
| 3 | 0.65 ± 0.04 | 0.00 ± 0.23 | 0.93 ± 0.06 |
| 4 | 0.64 ± 0.04 | 0.15 ± 0.08 | 1.00 ± 0.15 |
| | g'_{Ar} ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | g'_{He} ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | g'_K ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
| | 4.91 (fixed) | 0.71 (fixed) | 4.03 (fixed) |

Supplementary Material Table 7 – Fully separated fit rate coefficients ($k_p^{\Delta J}$) in units of the radiative rate Γ and in units of cm^3s^{-1} [the latter obtained by multiplying the fitted parameters ($k_p^{\Delta J}/\Gamma$) by $\Gamma = 4.4 \times 10^7 \text{ s}^{-1}$] for rotationally inelastic collisions of NaK $2(A)^1\Sigma^+(v = 16, J = 30)$ molecules with argon, helium, and potassium atoms ($p = Ar, He, \text{ and } K$). Quenching rate coefficients are also given.

| ΔJ | $k_{Ar}^{\Delta J}/\Gamma$ (10^{-18} cm^3) | $k_{He}^{\Delta J}/\Gamma$ (10^{-18} cm^3) | $k_K^{\Delta J}/\Gamma$ (10^{-17} cm^3) | $k_{Ar}^{\Delta J}$ ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | $k_{He}^{\Delta J}$ ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | $k_K^{\Delta J}$ ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
|------------|---|---|--|---|---|--|
| -4 | 1.83 ± 0.11 | 2.09 ± 0.09 | 0.15 ± 0.03 | 8.05 ± 0.51 | 9.20 ± 0.38 | 0.67 ± 0.12 |
| -3 | 1.43 ± 0.09 | 0.50 ± 0.03 | 0.20 ± 0.03 | 6.31 ± 0.41 | 2.20 ± 0.15 | 0.89 ± 0.15 |
| -2 | 4.08 ± 0.23 | 3.84 ± 0.16 | 0.35 ± 0.06 | 17.97 ± 1.03 | 16.89 ± 0.69 | 1.55 ± 0.25 |
| -1 | 2.17 ± 0.13 | 0.99 ± 0.06 | 0.48 ± 0.07 | 9.56 ± 0.58 | 4.36 ± 0.24 | 2.10 ± 0.32 |
| 0 | | | | | | |
| 1 | 1.87 ± 0.12 | 0.98 ± 0.07 | 0.91 ± 0.12 | 8.24 ± 0.54 | 4.31 ± 0.32 | 4.02 ± 0.53 |
| 2 | 4.10 ± 0.23 | 3.97 ± 0.17 | 0.73 ± 0.11 | 18.06 ± 1.00 | 17.49 ± 0.75 | 3.20 ± 0.48 |
| 3 | 1.10 ± 0.07 | 0.70 ± 0.04 | 0.24 ± 0.04 | 4.82 ± 0.31 | 3.10 ± 0.18 | 1.07 ± 0.17 |
| 4 | 1.68 ± 0.10 | 2.20 ± 0.09 | 0.16 ± 0.03 | 7.40 ± 0.45 | 9.66 ± 0.41 | 0.69 ± 0.15 |
| | k_{Ar}^Q/Γ (10^{-18} cm^3) | k_{He}^Q/Γ (10^{-18} cm^3) | k_K^Q/Γ (10^{-17} cm^3) | k_{Ar}^Q ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | k_{He}^Q ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | k_K^Q ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
| | 27.1 ± 2.1 | 36.4 ± 2.2 | 9.7 ± 1.9 | 119.3 ± 9.0 | 160.3 ± 9.6 | 42.7 ± 8.2 |

Supplementary Material Table 8 – Fully separated fit fraction of orientation destroyed ($f_p^{\Delta J}$) for rotationally inelastic collisions of NaK $2(A)^1\Sigma^+(v = 16, J = 30)$ molecules with argon, helium, and potassium atoms ($p = Ar, He, \text{ and } K$), and g'_p values obtained from Eq. 37.

| ΔJ | $f_{Ar}^{\Delta J}$ | $f_{He}^{\Delta J}$ | $f_K^{\Delta J}$ |
|------------|---|---|--|
| -4 | 0.75 ± 0.03 | 0.62 ± 0.05 | 0.95 ± 0.06 |
| -3 | 0.70 ± 0.04 | 0.00 ± 0.29 | 0.87 ± 0.07 |
| -2 | 0.59 ± 0.02 | 0.30 ± 0.04 | 0.90 ± 0.02 |
| -1 | 0.59 ± 0.03 | 0.38 ± 0.13 | 0.97 ± 0.01 |
| 1 | 0.53 ± 0.02 | 0.00 ± 0.12 | 0.96 ± 0.01 |
| 2 | 0.65 ± 0.01 | 0.34 ± 0.03 | 0.95 ± 0.02 |
| 3 | 0.66 ± 0.04 | 0.00 ± 0.21 | 0.98 ± 0.07 |
| 4 | 0.64 ± 0.03 | 0.18 ± 0.07 | 1.00 ± 0.17 |
| | g'_{Ar} ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | g'_{He} ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | g'_K ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
| | 4.97 (fixed) | 0.82 (fixed) | 2.94 (fixed) |

Supplementary Material Table 9 – Rate coefficients ($k_p^{\Delta J}$) in units of the radiative rate Γ and in units of cm^3s^{-1} [obtained by multiplying the fitted parameters ($k_p^{\Delta J}/\Gamma$) by $\Gamma = 4.7 \times 10^7 \text{ s}^{-1}$] for rotationally inelastic collisions of NaK $2(A)^1\Sigma^+(v=0, J=14)$ molecules with argon, helium, and potassium atoms ($p = Ar, He, \text{ and } K$).

| ΔJ | $k_{Ar}^{\Delta J}/\Gamma$ (10^{-18} cm^3) | $k_{He}^{\Delta J}/\Gamma$ (10^{-18} cm^3) | $k_K^{\Delta J}/\Gamma$ (10^{-17} cm^3) | $k_{Ar}^{\Delta J}$ ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | $k_{He}^{\Delta J}$ ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | $k_K^{\Delta J}$ ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
|------------|---|---|--|---|---|--|
| -10 | 0.38 ± 0.09 | 1.13 ± 0.12 | 0.72 ± 0.63 | 1.81 ± 0.41 | 5.33 ± 0.54 | 3.39 ± 2.96 |
| -9 | 0.19 ± 0.05 | 0.60 ± 0.10 | 1.40 ± 0.57 | 0.89 ± 0.22 | 2.80 ± 0.45 | 6.56 ± 2.67 |
| -8 | 0.41 ± 0.06 | 1.49 ± 0.13 | 1.53 ± 0.61 | 1.94 ± 0.26 | 7.02 ± 0.60 | 7.20 ± 2.88 |
| -7 | 0.42 ± 0.05 | 0.85 ± 0.10 | 1.24 ± 0.58 | 1.96 ± 0.25 | 3.99 ± 0.48 | 5.84 ± 2.71 |
| -6 | 0.75 ± 0.07 | 2.12 ± 0.15 | 1.88 ± 0.75 | 3.51 ± 0.34 | 9.97 ± 0.71 | 8.85 ± 3.51 |
| -5 | 0.57 ± 0.06 | 0.96 ± 0.11 | 1.83 ± 0.69 | 2.67 ± 0.30 | 4.51 ± 0.53 | 8.60 ± 3.25 |
| -4 | 1.28 ± 0.10 | 3.12 ± 0.20 | 4.29 ± 0.87 | 6.01 ± 0.48 | 14.67 ± 0.95 | 20.17 ± 4.08 |
| -3 | 0.79 ± 0.07 | 1.32 ± 0.12 | 2.89 ± 0.65 | 3.70 ± 0.33 | 6.23 ± 0.56 | 13.60 ± 3.04 |
| -2 | 2.98 ± 0.21 | 5.11 ± 0.32 | 8.94 ± 1.67 | 14.00 ± 1.01 | 24.04 ± 1.52 | 42.03 ± 7.83 |
| -1 | 1.09 ± 0.09 | 1.42 ± 0.13 | 3.33 ± 0.74 | 5.10 ± 0.41 | 6.66 ± 0.59 | 15.67 ± 3.47 |
| 0 | | | | | | |
| 1 | 1.19 ± 0.09 | 1.59 ± 0.13 | 3.66 ± 0.79 | 5.61 ± 0.44 | 7.49 ± 0.63 | 17.18 ± 3.69 |
| 2 | 3.51 ± 0.25 | 5.97 ± 0.37 | 9.43 ± 1.84 | 16.50 ± 1.15 | 28.04 ± 1.73 | 44.30 ± 8.65 |
| 3 | 0.98 ± 0.08 | 1.54 ± 0.13 | 3.11 ± 0.70 | 4.60 ± 0.38 | 7.25 ± 0.60 | 14.62 ± 3.27 |
| 4 | 1.77 ± 0.13 | 4.30 ± 0.26 | 4.96 ± 1.03 | 8.31 ± 0.61 | 20.22 ± 1.23 | 23.31 ± 4.84 |
| 5 | 0.91 ± 0.08 | 1.68 ± 0.14 | 2.37 ± 0.84 | 4.30 ± 0.39 | 7.88 ± 0.65 | 11.12 ± 3.97 |
| 6 | 1.13 ± 0.10 | 3.52 ± 0.20 | 2.95 ± 0.98 | 5.33 ± 0.45 | 16.54 ± 0.96 | 13.85 ± 4.60 |
| 7 | 0.83 ± 0.08 | 1.76 ± 0.14 | 2.18 ± 0.80 | 3.89 ± 0.36 | 8.27 ± 0.65 | 10.24 ± 3.75 |
| 8 | 0.83 ± 0.08 | 3.14 ± 0.19 | 2.76 ± 0.88 | 3.92 ± 0.39 | 14.75 ± 0.89 | 12.95 ± 4.13 |
| 9 | 0.76 ± 0.07 | 1.69 ± 0.13 | 1.88 ± 0.74 | 3.59 ± 0.34 | 7.93 ± 0.63 | 8.85 ± 3.50 |
| 10 | 0.69 ± 0.07 | 2.78 ± 0.17 | 2.31 ± 0.79 | 3.24 ± 0.35 | 13.04 ± 0.82 | 10.87 ± 3.70 |
| 11 | 0.68 ± 0.07 | 1.71 ± 0.14 | 2.00 ± 0.74 | 3.18 ± 0.33 | 8.03 ± 0.64 | 9.40 ± 3.46 |
| 12 | 0.64 ± 0.07 | 2.61 ± 0.17 | 2.20 ± 0.76 | 3.00 ± 0.33 | 12.27 ± 0.78 | 10.33 ± 3.56 |
| 13 | 0.60 ± 0.07 | 1.64 ± 0.13 | 2.03 ± 0.72 | 2.84 ± 0.32 | 7.69 ± 0.62 | 9.53 ± 3.40 |
| 14 | 0.57 ± 0.06 | 2.31 ± 0.16 | 1.86 ± 0.70 | 2.67 ± 0.30 | 10.83 ± 0.73 | 8.75 ± 3.27 |
| 15 | 0.60 ± 0.07 | 1.62 ± 0.13 | 1.91 ± 0.71 | 2.83 ± 0.31 | 7.62 ± 0.62 | 8.97 ± 3.32 |
| 16 | 0.50 ± 0.07 | 2.15 ± 0.15 | 2.14 ± 0.72 | 2.36 ± 0.31 | 10.10 ± 0.70 | 10.08 ± 3.36 |

Supplementary Material Table 10 – Rate coefficients ($k_p^{\Delta J}$) in units of the radiative rate Γ and in units of cm^3s^{-1} [obtained by multiplying the fitted parameters ($k_p^{\Delta J}/\Gamma$) by $\Gamma = 4.7 \times 10^7 \text{ s}^{-1}$] for rotationally inelastic collisions of NaK $2(A)^1\Sigma^+(v=0, J=30)$ molecules with argon, helium, and potassium atoms ($p = Ar, He, \text{ and } K$).

| ΔJ | $k_{Ar}^{\Delta J}/\Gamma$ (10^{-18} cm^3) | $k_{He}^{\Delta J}/\Gamma$ (10^{-18} cm^3) | $k_K^{\Delta J}/\Gamma$ (10^{-17} cm^3) | $k_{Ar}^{\Delta J}$ ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | $k_{He}^{\Delta J}$ ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | $k_K^{\Delta J}$ ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
|------------|---|---|--|---|---|--|
| -20 | 0.26 ± 0.02 | 0.69 ± 0.15 | 0.50 ± 0.13 | 1.22 ± 0.11 | 3.24 ± 0.73 | 2.34 ± 0.60 |
| -19 | 0.32 ± 0.03 | 0.84 ± 0.15 | 0.60 ± 0.14 | 1.50 ± 0.12 | 3.97 ± 0.71 | 2.81 ± 0.66 |
| -18 | 0.32 ± 0.03 | 0.77 ± 0.16 | 0.65 ± 0.15 | 1.51 ± 0.13 | 3.62 ± 0.73 | 3.04 ± 0.69 |
| -17 | 0.35 ± 0.03 | 0.84 ± 0.17 | 0.64 ± 0.15 | 1.62 ± 0.13 | 3.96 ± 0.80 | 2.99 ± 0.69 |
| -16 | 0.37 ± 0.03 | 0.97 ± 0.16 | 0.10 ± 0.02 | 1.74 ± 0.14 | 4.55 ± 0.73 | 0.46 ± 0.07 |
| -15 | 0.44 ± 0.03 | 1.21 ± 0.17 | 0.77 ± 0.17 | 2.08 ± 0.14 | 5.70 ± 0.80 | 3.63 ± 0.79 |
| -14 | 0.46 ± 0.03 | 1.06 ± 0.16 | 0.94 ± 0.19 | 2.16 ± 0.16 | 4.96 ± 0.75 | 4.44 ± 0.89 |
| -13 | 0.49 ± 0.03 | 1.19 ± 0.17 | 0.86 ± 0.18 | 2.32 ± 0.15 | 5.57 ± 0.79 | 4.05 ± 0.85 |
| -12 | 0.53 ± 0.04 | 1.20 ± 0.17 | 1.13 ± 0.21 | 2.50 ± 0.17 | 5.65 ± 0.78 | 5.32 ± 1.00 |
| -11 | 0.56 ± 0.04 | 1.28 ± 0.17 | 1.00 ± 0.20 | 2.64 ± 0.17 | 6.02 ± 0.80 | 4.69 ± 0.93 |
| -10 | 0.67 ± 0.04 | 1.49 ± 0.18 | 1.30 ± 0.24 | 3.15 ± 0.19 | 7.02 ± 0.85 | 6.12 ± 1.15 |
| -9 | 0.69 ± 0.04 | 1.53 ± 0.18 | 1.08 ± 0.22 | 3.25 ± 0.18 | 7.20 ± 0.87 | 5.08 ± 1.02 |
| -8 | 0.83 ± 0.05 | 1.67 ± 0.19 | 1.83 ± 0.30 | 3.92 ± 0.23 | 7.86 ± 0.88 | 8.60 ± 1.42 |
| -7 | 0.70 ± 0.04 | 1.72 ± 0.19 | 1.45 ± 0.25 | 3.29 ± 0.20 | 8.09 ± 0.90 | 6.80 ± 1.16 |
| -6 | 1.12 ± 0.06 | 1.98 ± 0.20 | 2.42 ± 0.37 | 5.27 ± 0.28 | 9.32 ± 0.94 | 11.36 ± 1.76 |
| -5 | 0.96 ± 0.05 | 1.96 ± 0.20 | 1.49 ± 0.27 | 4.50 ± 0.22 | 9.19 ± 0.96 | 6.98 ± 1.28 |
| -4 | 1.76 ± 0.11 | 3.00 ± 0.23 | 3.82 ± 0.75 | 8.26 ± 0.52 | 14.10 ± 1.08 | 17.97 ± 3.53 |
| -3 | 1.14 ± 0.07 | 2.19 ± 0.19 | 1.83 ± 0.41 | 5.37 ± 0.31 | 10.29 ± 0.89 | 8.59 ± 1.93 |
| -2 | 3.44 ± 0.20 | 4.89 ± 0.34 | 6.58 ± 1.35 | 16.15 ± 0.95 | 23.00 ± 1.62 | 30.94 ± 6.32 |
| -1 | 1.52 ± 0.08 | 2.95 ± 0.23 | 2.10 ± 0.50 | 7.15 ± 0.38 | 13.88 ± 1.08 | 9.85 ± 2.33 |
| 0 | | | | | | |
| 1 | 1.41 ± 0.08 | 2.50 ± 0.20 | 2.20 ± 0.50 | 6.63 ± 0.37 | 11.75 ± 0.96 | 10.35 ± 2.33 |
| 2 | 3.58 ± 0.21 | 5.35 ± 0.37 | 7.02 ± 1.42 | 16.85 ± 1.00 | 25.16 ± 1.74 | 33.01 ± 6.68 |
| 3 | 1.23 ± 0.07 | 2.56 ± 0.21 | 1.95 ± 0.44 | 5.77 ± 0.33 | 12.04 ± 0.98 | 9.19 ± 2.06 |
| 4 | 1.84 ± 0.12 | 3.10 ± 0.24 | 4.09 ± 0.80 | 8.65 ± 0.55 | 14.55 ± 1.11 | 19.23 ± 3.75 |
| 5 | 1.07 ± 0.05 | 2.25 ± 0.22 | 1.71 ± 0.30 | 5.01 ± 0.24 | 10.57 ± 1.02 | 8.02 ± 1.41 |
| 6 | 1.33 ± 0.07 | 2.74 ± 0.24 | 2.79 ± 0.43 | 6.27 ± 0.32 | 12.87 ± 1.12 | 13.09 ± 2.04 |
| 7 | 0.97 ± 0.05 | 2.12 ± 0.21 | 1.56 ± 0.28 | 4.55 ± 0.23 | 9.98 ± 1.00 | 7.33 ± 1.32 |
| 8 | 1.03 ± 0.06 | 2.27 ± 0.22 | 2.06 ± 0.35 | 4.84 ± 0.26 | 10.66 ± 1.02 | 9.70 ± 1.64 |
| 9 | 0.85 ± 0.05 | 2.06 ± 0.21 | 1.43 ± 0.26 | 4.00 ± 0.21 | 9.66 ± 0.99 | 6.72 ± 1.23 |
| 10 | 0.87 ± 0.05 | 2.10 ± 0.21 | 1.70 ± 0.30 | 4.08 ± 0.23 | 9.86 ± 0.99 | 8.01 ± 1.41 |

Supplementary Material Table 11 – Rate coefficients ($k_p^{\Delta J}$) in units of the radiative rate Γ and in units of cm^3s^{-1} [obtained by multiplying the fitted parameters ($k_p^{\Delta J}/\Gamma$) by $\Gamma = 4.7 \times 10^7 \text{ s}^{-1}$] for rotationally inelastic collisions of NaK $2(A)^1\Sigma^+(v=1, J=26)$ molecules with argon, helium, and potassium atoms ($p = Ar, He, \text{ and } K$).

| ΔJ | $k_{Ar}^{\Delta J}/\Gamma$ (10^{-18} cm^3) | $k_{He}^{\Delta J}/\Gamma$ (10^{-18} cm^3) | $k_K^{\Delta J}/\Gamma$ (10^{-17} cm^3) | $k_{Ar}^{\Delta J}$ ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | $k_{He}^{\Delta J}$ ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | $k_K^{\Delta J}$ ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
|------------|---|---|--|---|---|--|
| -17 | 0.20 ± 0.06 | 0.45 ± 0.07 | 0.49 ± 0.36 | 0.93 ± 0.26 | 2.11 ± 0.33 | 2.32 ± 1.68 |
| -16 | 0.24 ± 0.06 | 0.81 ± 0.10 | 0.43 ± 0.36 | 1.13 ± 0.27 | 3.79 ± 0.46 | 2.00 ± 1.68 |
| -15 | 0.27 ± 0.04 | 0.49 ± 0.05 | 0.39 ± 0.26 | 1.27 ± 0.20 | 2.32 ± 0.25 | 1.81 ± 1.24 |
| -14 | 0.34 ± 0.05 | 1.02 ± 0.08 | 0.59 ± 0.31 | 1.59 ± 0.23 | 4.80 ± 0.38 | 2.78 ± 1.46 |
| -13 | 0.28 ± 0.04 | 0.60 ± 0.05 | 0.58 ± 0.25 | 1.32 ± 0.19 | 2.80 ± 0.24 | 2.74 ± 1.20 |
| -12 | 0.37 ± 0.04 | 1.13 ± 0.07 | 0.70 ± 0.26 | 1.75 ± 0.19 | 5.30 ± 0.31 | 3.28 ± 1.21 |
| -11 | 0.37 ± 0.04 | 0.79 ± 0.05 | 0.78 ± 0.26 | 1.76 ± 0.19 | 3.70 ± 0.25 | 3.66 ± 1.24 |
| -10 | 0.46 ± 0.05 | 1.49 ± 0.08 | 1.07 ± 0.31 | 2.16 ± 0.21 | 7.00 ± 0.37 | 5.04 ± 1.47 |
| -9 | 0.48 ± 0.05 | 0.81 ± 0.06 | 1.03 ± 0.31 | 2.27 ± 0.21 | 3.82 ± 0.28 | 4.82 ± 1.47 |
| -8 | 0.66 ± 0.06 | 1.84 ± 0.09 | 1.47 ± 0.41 | 3.09 ± 0.27 | 8.65 ± 0.43 | 6.89 ± 1.95 |
| -7 | 0.55 ± 0.05 | 0.93 ± 0.06 | 1.33 ± 0.35 | 2.58 ± 0.23 | 4.35 ± 0.28 | 6.25 ± 1.65 |
| -6 | 0.86 ± 0.07 | 2.40 ± 0.11 | 2.52 ± 0.52 | 4.06 ± 0.32 | 11.26 ± 0.51 | 11.83 ± 2.46 |
| -5 | 0.72 ± 0.06 | 0.90 ± 0.06 | 1.27 ± 0.42 | 3.36 ± 0.28 | 4.23 ± 0.28 | 5.96 ± 1.98 |
| -4 | 1.41 ± 0.10 | 3.21 ± 0.18 | 3.81 ± 0.69 | 6.61 ± 0.46 | 15.10 ± 0.85 | 17.89 ± 3.23 |
| -3 | 0.88 ± 0.06 | 1.11 ± 0.07 | 1.60 ± 0.39 | 4.12 ± 0.28 | 5.24 ± 0.33 | 7.50 ± 1.81 |
| -2 | 3.13 ± 0.20 | 5.13 ± 0.29 | 7.30 ± 1.36 | 14.69 ± 0.92 | 24.13 ± 1.37 | 34.31 ± 6.40 |
| -1 | 1.17 ± 0.07 | 1.23 ± 0.08 | 1.51 ± 0.47 | 5.52 ± 0.34 | 5.78 ± 0.36 | 7.11 ± 2.20 |
| 0 | | | | | | |
| 1 | 1.15 ± 0.08 | 1.26 ± 0.08 | 2.14 ± 0.49 | 5.42 ± 0.35 | 5.91 ± 0.37 | 10.07 ± 2.32 |
| 2 | 3.17 ± 0.20 | 5.28 ± 0.30 | 7.48 ± 1.39 | 14.90 ± 0.94 | 24.82 ± 1.41 | 35.17 ± 6.52 |
| 3 | 0.95 ± 0.06 | 1.19 ± 0.07 | 1.49 ± 0.40 | 4.46 ± 0.29 | 5.58 ± 0.35 | 7.00 ± 1.86 |
| 4 | 1.46 ± 0.10 | 3.53 ± 0.20 | 4.00 ± 0.72 | 6.88 ± 0.47 | 16.58 ± 0.93 | 18.81 ± 3.37 |
| 5 | 0.74 ± 0.05 | 1.14 ± 0.07 | 1.25 ± 0.38 | 3.50 ± 0.25 | 5.35 ± 0.31 | 5.89 ± 1.77 |
| 6 | 0.34 ± 0.04 | 1.02 ± 0.06 | 0.87 ± 0.27 | 1.60 ± 0.19 | 4.78 ± 0.29 | 4.10 ± 1.29 |
| 7 | 0.62 ± 0.05 | 1.17 ± 0.07 | 1.29 ± 0.36 | 2.89 ± 0.24 | 5.49 ± 0.32 | 6.07 ± 1.70 |
| 8 | 0.62 ± 0.05 | 1.59 ± 0.08 | 1.20 ± 0.36 | 2.91 ± 0.24 | 7.46 ± 0.40 | 5.64 ± 1.71 |
| 9 | 0.53 ± 0.05 | 1.04 ± 0.06 | 0.86 ± 0.30 | 2.48 ± 0.21 | 4.89 ± 0.29 | 4.06 ± 1.42 |
| 10 | 0.48 ± 0.05 | 1.32 ± 0.09 | 0.87 ± 0.35 | 2.25 ± 0.25 | 6.18 ± 0.41 | 4.11 ± 1.66 |
| 11 | 0.44 ± 0.05 | 0.91 ± 0.06 | 0.62 ± 0.30 | 2.08 ± 0.22 | 4.26 ± 0.30 | 2.90 ± 1.41 |
| 12 | 0.34 ± 0.05 | 1.28 ± 0.09 | 0.84 ± 0.35 | 1.60 ± 0.24 | 6.03 ± 0.44 | 3.96 ± 1.63 |
| 13 | 0.26 ± 0.04 | 0.67 ± 0.06 | 0.50 ± 0.28 | 1.24 ± 0.21 | 3.13 ± 0.29 | 2.35 ± 1.30 |
| 14 | 0.18 ± 0.04 | 0.60 ± 0.06 | 0.20 ± 0.23 | 0.86 ± 0.18 | 2.80 ± 0.28 | 0.95 ± 1.06 |
| 15 | 0.20 ± 0.04 | 0.51 ± 0.05 | 0.39 ± 0.24 | 0.94 ± 0.19 | 2.41 ± 0.26 | 1.84 ± 1.14 |
| 16 | 0.26 ± 0.04 | 0.84 ± 0.07 | 0.37 ± 0.26 | 1.21 ± 0.20 | 3.97 ± 0.34 | 1.75 ± 1.21 |
| 17 | 0.24 ± 0.04 | 0.56 ± 0.06 | 0.36 ± 0.25 | 1.13 ± 0.19 | 2.65 ± 0.27 | 1.70 ± 1.16 |
| 18 | 0.20 ± 0.04 | 0.70 ± 0.06 | 0.52 ± 0.26 | 0.93 ± 0.19 | 3.28 ± 0.30 | 2.46 ± 1.23 |
| 19 | 0.19 ± 0.04 | 0.49 ± 0.05 | 0.39 ± 0.24 | 0.88 ± 0.18 | 2.29 ± 0.25 | 1.83 ± 1.12 |
| 20 | 0.15 ± 0.04 | 0.44 ± 0.05 | 0.28 ± 0.21 | 0.70 ± 0.17 | 2.05 ± 0.24 | 1.33 ± 0.98 |
| 21 | 0.17 ± 0.06 | 0.38 ± 0.07 | 0.26 ± 0.31 | 0.78 ± 0.26 | 1.79 ± 0.32 | 1.22 ± 1.46 |
| 22 | 0.16 ± 0.05 | 0.47 ± 0.08 | 0.43 ± 0.34 | 0.76 ± 0.26 | 2.23 ± 0.35 | 2.00 ± 1.59 |
| 23 | 0.20 ± 0.06 | 0.46 ± 0.07 | 0.39 ± 0.34 | 0.93 ± 0.26 | 2.16 ± 0.35 | 1.83 ± 1.61 |

Supplementary Material Table 12 – Rate coefficients ($k_p^{\Delta J}$) in units of the radiative rate Γ and in units of cm^3s^{-1} [obtained by multiplying the fitted parameters ($k_p^{\Delta J}/\Gamma$) by $\Gamma = 4.7 \times 10^7 \text{ s}^{-1}$] for rotationally inelastic collisions of NaK $2(A)^1\Sigma^+(v=2, J=44)$ molecules with argon, helium, and potassium atoms ($p = Ar, He, \text{ and } K$).

| ΔJ | $k_{Ar}^{\Delta J}/\Gamma$ (10^{-18} cm^3) | $k_{He}^{\Delta J}/\Gamma$ (10^{-18} cm^3) | $k_K^{\Delta J}/\Gamma$ (10^{-17} cm^3) | $k_{Ar}^{\Delta J}$ ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | $k_{He}^{\Delta J}$ ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | $k_K^{\Delta J}$ ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
|------------|---|---|--|---|---|--|
| -17 | 0.20 ± 0.04 | 0.40 ± 0.05 | 0.11 ± 0.22 | 0.93 ± 0.18 | 1.86 ± 0.21 | 0.50 ± 1.03 |
| -16 | 0.16 ± 0.04 | 0.38 ± 0.05 | 0.07 ± 0.22 | 0.73 ± 0.19 | 1.81 ± 0.21 | 0.33 ± 1.04 |
| -15 | 0.18 ± 0.05 | 0.32 ± 0.04 | 0.00 ± 0.24 | 0.85 ± 0.22 | 1.50 ± 0.20 | 0.00 ± 1.14 |
| -14 | 0.23 ± 0.05 | 0.60 ± 0.06 | 0.23 ± 0.27 | 1.09 ± 0.23 | 2.81 ± 0.30 | 1.06 ± 1.29 |
| -13 | 0.27 ± 0.04 | 0.50 ± 0.05 | 0.27 ± 0.24 | 1.28 ± 0.20 | 2.34 ± 0.23 | 1.28 ± 1.11 |
| -12 | 0.35 ± 0.04 | 1.01 ± 0.07 | 0.52 ± 0.26 | 1.65 ± 0.21 | 4.73 ± 0.31 | 2.44 ± 1.21 |
| -11 | 0.40 ± 0.05 | 0.69 ± 0.06 | 0.42 ± 0.27 | 1.90 ± 0.22 | 3.23 ± 0.26 | 1.96 ± 1.28 |
| -10 | 0.48 ± 0.05 | 1.45 ± 0.08 | 0.75 ± 0.30 | 2.27 ± 0.23 | 6.79 ± 0.39 | 3.55 ± 1.39 |
| -9 | 0.50 ± 0.06 | 0.78 ± 0.07 | 0.56 ± 0.34 | 2.36 ± 0.26 | 3.66 ± 0.31 | 2.63 ± 1.59 |
| -8 | 0.68 ± 0.06 | 1.84 ± 0.11 | 0.81 ± 0.40 | 3.21 ± 0.30 | 8.67 ± 0.52 | 3.81 ± 1.87 |
| -7 | 0.64 ± 0.06 | 0.93 ± 0.07 | 0.50 ± 0.35 | 3.03 ± 0.27 | 4.38 ± 0.31 | 2.37 ± 1.65 |
| -6 | 0.88 ± 0.07 | 2.35 ± 0.11 | 1.80 ± 0.44 | 4.14 ± 0.31 | 11.03 ± 0.53 | 8.44 ± 2.07 |
| -5 | 0.81 ± 0.06 | 1.05 ± 0.07 | 0.75 ± 0.39 | 3.83 ± 0.29 | 4.95 ± 0.32 | 3.51 ± 1.85 |
| -4 | 1.40 ± 0.10 | 3.12 ± 0.18 | 3.01 ± 0.65 | 6.58 ± 0.46 | 14.68 ± 0.84 | 14.16 ± 3.04 |
| -3 | 1.03 ± 0.07 | 1.06 ± 0.07 | 0.83 ± 0.44 | 4.83 ± 0.34 | 4.99 ± 0.33 | 3.89 ± 2.09 |
| -2 | 2.98 ± 0.20 | 5.04 ± 0.29 | 6.29 ± 1.30 | 14.03 ± 0.92 | 23.70 ± 1.36 | 29.57 ± 6.12 |
| -1 | 1.10 ± 0.08 | 1.11 ± 0.07 | 0.92 ± 0.47 | 5.15 ± 0.36 | 5.19 ± 0.34 | 4.33 ± 2.19 |
| 0 | | | | | | |
| 1 | 1.29 ± 0.09 | 1.14 ± 0.08 | 1.02 ± 0.53 | 6.04 ± 0.41 | 5.34 ± 0.35 | 4.79 ± 2.51 |
| 2 | 2.94 ± 0.19 | 5.22 ± 0.30 | 6.40 ± 1.30 | 13.83 ± 0.91 | 24.56 ± 1.40 | 30.08 ± 6.09 |
| 3 | 1.03 ± 0.07 | 1.06 ± 0.07 | 0.87 ± 0.44 | 4.84 ± 0.35 | 4.98 ± 0.33 | 4.10 ± 2.09 |
| 4 | 1.42 ± 0.10 | 3.32 ± 0.19 | 3.15 ± 0.66 | 6.68 ± 0.47 | 15.59 ± 0.89 | 14.80 ± 3.11 |
| 5 | 0.83 ± 0.06 | 1.02 ± 0.07 | 0.76 ± 0.40 | 3.89 ± 0.30 | 4.78 ± 0.32 | 3.58 ± 1.86 |
| 6 | 0.90 ± 0.08 | 2.48 ± 0.14 | 1.83 ± 0.52 | 4.21 ± 0.37 | 11.65 ± 0.65 | 8.59 ± 2.45 |
| 7 | 0.66 ± 0.07 | 0.96 ± 0.08 | 0.70 ± 0.41 | 3.10 ± 0.31 | 4.52 ± 0.36 | 3.29 ± 1.91 |
| 8 | 0.73 ± 0.08 | 2.07 ± 0.15 | 1.12 ± 0.51 | 3.42 ± 0.39 | 9.73 ± 0.70 | 5.26 ± 2.41 |
| 9 | 0.53 ± 0.07 | 0.85 ± 0.09 | 0.68 ± 0.43 | 2.48 ± 0.34 | 4.01 ± 0.40 | 3.21 ± 2.04 |
| 10 | 0.54 ± 0.07 | 1.59 ± 0.12 | 0.76 ± 0.44 | 2.54 ± 0.34 | 7.48 ± 0.58 | 3.55 ± 2.06 |
| 11 | 0.45 ± 0.07 | 0.77 ± 0.08 | 0.53 ± 0.41 | 2.12 ± 0.32 | 3.64 ± 0.39 | 2.51 ± 1.90 |
| 12 | 0.50 ± 0.07 | 1.50 ± 0.12 | 0.72 ± 0.42 | 2.33 ± 0.33 | 7.04 ± 0.56 | 3.36 ± 1.98 |
| 13 | 0.42 ± 0.07 | 0.76 ± 0.08 | 0.42 ± 0.40 | 1.99 ± 0.32 | 3.56 ± 0.38 | 1.97 ± 1.86 |
| 14 | 0.38 ± 0.07 | 1.13 ± 0.10 | 0.55 ± 0.38 | 1.79 ± 0.31 | 5.32 ± 0.48 | 2.59 ± 1.78 |
| 15 | 0.41 ± 0.09 | 0.78 ± 0.11 | 0.38 ± 0.51 | 1.90 ± 0.40 | 3.69 ± 0.51 | 1.80 ± 2.40 |
| 16 | 0.32 ± 0.08 | 0.91 ± 0.12 | 0.34 ± 0.45 | 1.48 ± 0.37 | 4.26 ± 0.56 | 1.61 ± 2.13 |

Supplementary Material Table 13 – Rate coefficients, $k_{Ar}^{\Delta J}$, for rotationally inelastic collisions of NaK $2(A)^1\Sigma^+(v = 0, J = 14)$ molecules with argon atoms, corrected for multiple collision effects (using $n_{Ar} = 2.13 \times 10^{17} \text{ cm}^{-3}$ and $n_K = 2.12 \times 10^{15} \text{ cm}^{-3}$). The zeroth, first through sixth, 99th, and 100th order (corrected) rate coefficients are given. The final values are the averages of the 99th and 100th iteration values.

| ΔJ | $k_{Ar}^{D \rightarrow C(0)}$ | $k_{Ar}^{D \rightarrow C(n)}$ for iteration n (in units of $10^{-11} \text{ cm}^3 \text{ s}^{-1}$) | | | | | | | | |
|------------|-------------------------------|---|-------|-------|-------|-------|-------|--------|---------|-------|
| | | $n=1$ | $n=2$ | $n=3$ | $n=4$ | $n=5$ | $n=6$ | $n=99$ | $n=100$ | Final |
| -10 | 1.81 | 1.03 | 1.07 | 1.20 | 1.14 | 1.19 | 1.15 | 1.17 | 1.17 | 1.17 |
| -9 | 0.89 | 0.32 | 0.03 | 0.14 | 0.06 | 0.12 | 0.07 | 0.09 | 0.09 | 0.09 |
| -8 | 1.94 | 0.84 | 0.45 | 0.54 | 0.44 | 0.52 | 0.45 | 0.48 | 0.48 | 0.48 |
| -7 | 1.96 | 0.88 | 0.65 | 0.83 | 0.71 | 0.81 | 0.73 | 0.77 | 0.77 | 0.77 |
| -6 | 3.51 | 1.75 | 1.40 | 1.53 | 1.42 | 1.53 | 1.44 | 1.48 | 1.48 | 1.48 |
| -5 | 2.67 | 1.19 | 0.79 | 0.98 | 0.82 | 0.95 | 0.84 | 0.89 | 0.89 | 0.89 |
| -4 | 6.01 | 3.36 | 2.97 | 3.03 | 2.88 | 3.01 | 2.89 | 2.94 | 2.94 | 2.94 |
| -3 | 3.70 | 1.73 | 1.30 | 1.50 | 1.32 | 1.48 | 1.33 | 1.40 | 1.40 | 1.40 |
| -2 | 14.00 | 10.75 | 11.58 | 11.80 | 11.64 | 11.80 | 11.66 | 11.72 | 11.72 | 11.72 |
| -1 | 5.10 | 2.61 | 2.33 | 2.58 | 2.35 | 2.56 | 2.37 | 2.46 | 2.46 | 2.46 |
| 0 | | | | | | | | | | |
| 1 | 5.61 | 2.87 | 2.62 | 2.93 | 2.66 | 2.91 | 2.69 | 2.79 | 2.79 | 2.79 |
| 2 | 16.50 | 12.56 | 13.63 | 13.94 | 13.70 | 13.94 | 13.72 | 13.82 | 13.82 | 13.82 |
| 3 | 4.60 | 2.03 | 1.37 | 1.70 | 1.37 | 1.67 | 1.40 | 1.53 | 1.53 | 1.53 |
| 4 | 8.31 | 4.53 | 4.08 | 4.30 | 3.96 | 4.26 | 3.98 | 4.11 | 4.11 | 4.11 |
| 5 | 4.30 | 1.83 | 1.22 | 1.65 | 1.28 | 1.62 | 1.31 | 1.46 | 1.46 | 1.46 |
| 6 | 5.33 | 2.39 | 1.66 | 2.05 | 1.67 | 2.02 | 1.70 | 1.86 | 1.86 | 1.86 |
| 7 | 3.89 | 1.59 | 0.98 | 1.46 | 1.06 | 1.43 | 1.09 | 1.25 | 1.25 | 1.25 |
| 8 | 3.92 | 1.57 | 0.81 | 1.30 | 0.89 | 1.27 | 0.93 | 1.09 | 1.09 | 1.09 |
| 9 | 3.59 | 1.44 | 0.87 | 1.36 | 0.93 | 1.32 | 0.97 | 1.13 | 1.13 | 1.13 |
| 10 | 3.24 | 1.22 | 0.50 | 0.99 | 0.57 | 0.96 | 0.60 | 0.77 | 0.77 | 0.77 |
| 11 | 3.18 | 1.25 | 0.68 | 1.14 | 0.72 | 1.10 | 0.75 | 0.92 | 0.92 | 0.92 |
| 12 | 3.00 | 1.16 | 0.60 | 1.07 | 0.66 | 1.04 | 0.69 | 0.86 | 0.86 | 0.86 |
| 13 | 2.84 | 1.11 | 0.59 | 0.97 | 0.57 | 0.93 | 0.60 | 0.76 | 0.76 | 0.76 |
| 14 | 2.67 | 1.04 | 0.57 | 0.95 | 0.56 | 0.91 | 0.59 | 0.74 | 0.74 | 0.74 |
| 15 | 2.83 | 1.29 | 1.21 | 1.59 | 1.27 | 1.57 | 1.30 | 1.43 | 1.43 | 1.43 |
| 16 | 2.36 | 1.01 | 0.86 | 1.21 | 0.90 | 1.19 | 0.93 | 1.06 | 1.06 | 1.06 |

Supplementary Material Table 14 – Rate coefficients, $k_{He}^{\Delta J}$, for rotationally inelastic collisions of NaK $2(A)^1\Sigma^+(v = 0, J = 14)$ molecules with helium atoms, corrected for multiple collision effects (using $n_{He} = 2.95 \times 10^{17} \text{ cm}^{-3}$ and $n_K = 3.02 \times 10^{15} \text{ cm}^{-3}$). The zeroth, first through sixth, 99th, and 100th order (corrected) rate coefficients are given. The final values are the averages of the 5th and 6th iteration values.

| ΔJ | $k_{He}^{D \rightarrow C(0)}$ | $k_{He}^{D \rightarrow C(n)}$ for iteration n (in units of $10^{-11} \text{ cm}^3 \text{ s}^{-1}$) | | | | | | | | |
|------------|-------------------------------|---|---------|---------|---------|---------|---------|----------|-----------|-------|
| | | $n = 1$ | $n = 2$ | $n = 3$ | $n = 4$ | $n = 5$ | $n = 6$ | $n = 99$ | $n = 100$ | Final |
| -10 | 5.33 | 2.81 | 2.82 | 2.96 | 2.86 | 3.03 | 2.81 | 3.78 | 2.08 | 2.92 |
| -9 | 2.80 | 1.13 | 0.84 | 1.11 | 0.88 | 1.14 | 0.83 | 1.92 | 0.00 | 0.99 |
| -8 | 7.02 | 3.41 | 2.96 | 2.99 | 2.81 | 3.07 | 2.73 | 4.17 | 1.66 | 2.90 |
| -7 | 3.99 | 1.62 | 1.18 | 1.55 | 1.20 | 1.60 | 1.13 | 2.63 | 0.00 | 1.37 |
| -6 | 9.97 | 5.00 | 4.52 | 4.54 | 4.27 | 4.65 | 4.17 | 6.11 | 2.73 | 4.41 |
| -5 | 4.51 | 1.65 | 0.74 | 1.17 | 0.66 | 1.21 | 0.57 | 2.70 | 0.00 | 0.89 |
| -4 | 14.67 | 8.04 | 8.02 | 8.04 | 7.66 | 8.17 | 7.53 | 9.99 | 5.71 | 7.85 |
| -3 | 6.23 | 2.50 | 1.87 | 2.54 | 1.90 | 2.63 | 1.78 | 4.21 | 0.00 | 2.20 |
| -2 | 24.04 | 15.82 | 17.65 | 17.99 | 17.52 | 18.17 | 17.37 | 20.31 | 15.21 | 17.77 |
| -1 | 6.66 | 2.50 | 1.45 | 2.24 | 1.40 | 2.33 | 1.24 | 4.34 | 0.00 | 1.78 |
| 0 | | | | | | | | | | |
| 1 | 7.49 | 2.79 | 1.73 | 2.77 | 1.75 | 2.90 | 1.56 | 5.06 | 0.00 | 2.23 |
| 2 | 28.04 | 17.80 | 20.08 | 20.76 | 19.97 | 21.02 | 19.73 | 24.00 | 16.55 | 20.37 |
| 3 | 7.25 | 2.44 | 0.78 | 1.96 | 0.72 | 2.11 | 0.49 | 4.68 | 0.00 | 1.30 |
| 4 | 20.22 | 10.21 | 10.10 | 10.66 | 9.62 | 10.92 | 9.33 | 14.45 | 5.47 | 10.12 |
| 5 | 7.88 | 2.65 | 0.98 | 2.37 | 0.95 | 2.56 | 0.68 | 5.31 | 0.00 | 1.62 |
| 6 | 16.54 | 7.24 | 6.05 | 6.82 | 5.59 | 7.13 | 5.26 | 11.09 | 0.86 | 6.19 |
| 7 | 8.27 | 2.80 | 1.21 | 2.74 | 1.19 | 2.96 | 0.89 | 5.83 | 0.00 | 1.93 |
| 8 | 14.75 | 6.10 | 4.75 | 5.79 | 4.47 | 6.15 | 4.12 | 10.24 | 0.00 | 5.14 |
| 9 | 7.93 | 2.59 | 0.81 | 2.31 | 0.66 | 2.53 | 0.35 | 5.53 | 0.00 | 1.44 |
| 10 | 13.04 | 5.09 | 3.47 | 4.59 | 3.17 | 4.93 | 2.81 | 9.15 | 0.00 | 3.87 |
| 11 | 8.03 | 2.71 | 1.22 | 2.73 | 1.06 | 2.96 | 0.75 | 5.83 | 0.00 | 1.85 |
| 12 | 12.27 | 4.80 | 3.47 | 4.63 | 3.18 | 4.95 | 2.81 | 8.97 | 0.00 | 3.88 |
| 13 | 7.69 | 2.63 | 1.34 | 2.70 | 1.05 | 2.89 | 0.75 | 5.78 | 0.00 | 1.82 |
| 14 | 10.83 | 4.16 | 2.94 | 4.00 | 2.56 | 4.27 | 2.21 | 8.09 | 0.00 | 3.24 |
| 15 | 7.62 | 2.88 | 2.51 | 3.91 | 2.47 | 4.14 | 2.20 | 6.48 | 0.00 | 3.17 |
| 16 | 10.10 | 4.20 | 3.99 | 5.18 | 3.92 | 5.47 | 3.62 | 8.51 | 0.00 | 4.54 |

Supplementary Material Table 15 – Rate coefficients, $k_K^{\Delta J}$, for rotationally inelastic collisions of NaK $2(A)^1\Sigma^+(v = 0, J = 14)$ molecules with potassium atoms, corrected for multiple collision effects (using $n_{Ar} = 2.13 \times 10^{17} \text{ cm}^{-3}$ and $n_K = 2.12 \times 10^{15} \text{ cm}^{-3}$). The zeroth, first through sixth, 99th, and 100th order (corrected) rate coefficients are given. The final values are the averages of the 99th and 100th iteration values.

| ΔJ | $k_K^{D \rightarrow C(0)}$ | $k_K^{D \rightarrow C(n)}$ for iteration n (in units of $10^{-10} \text{ cm}^3 \text{ s}^{-1}$) | | | | | | | | |
|------------|----------------------------|--|-------|-------|-------|-------|-------|--------|---------|-------|
| | | $n=1$ | $n=2$ | $n=3$ | $n=4$ | $n=5$ | $n=6$ | $n=99$ | $n=100$ | Final |
| -10 | 3.39 | 1.45 | 0.86 | 1.13 | 0.97 | 1.10 | 0.98 | 1.04 | 1.04 | 1.04 |
| -9 | 6.56 | 3.77 | 3.96 | 4.37 | 4.17 | 4.35 | 4.20 | 4.27 | 4.27 | 4.27 |
| -8 | 7.20 | 3.56 | 2.95 | 3.36 | 3.12 | 3.34 | 3.15 | 3.24 | 3.24 | 3.24 |
| -7 | 5.84 | 2.46 | 1.33 | 1.67 | 1.35 | 1.61 | 1.38 | 1.48 | 1.48 | 1.48 |
| -6 | 8.85 | 3.92 | 2.11 | 2.35 | 2.02 | 2.31 | 2.05 | 2.17 | 2.17 | 2.17 |
| -5 | 8.60 | 3.85 | 2.57 | 3.04 | 2.63 | 2.99 | 2.67 | 2.82 | 2.82 | 2.82 |
| -4 | 20.17 | 11.90 | 11.28 | 11.54 | 11.12 | 11.49 | 11.15 | 11.31 | 11.31 | 11.31 |
| -3 | 13.60 | 7.01 | 6.33 | 6.95 | 6.45 | 6.91 | 6.50 | 6.70 | 6.70 | 6.70 |
| -2 | 42.03 | 32.18 | 34.72 | 35.31 | 34.85 | 35.29 | 34.90 | 35.08 | 35.08 | 35.08 |
| -1 | 15.67 | 8.03 | 7.16 | 7.79 | 7.14 | 7.70 | 7.19 | 7.43 | 7.43 | 7.43 |
| 0 | | | | | | | | | | |
| 1 | 17.18 | 8.90 | 8.27 | 9.14 | 8.38 | 9.07 | 8.45 | 8.74 | 8.74 | 8.74 |
| 2 | 44.30 | 32.84 | 35.69 | 36.58 | 35.87 | 36.54 | 35.93 | 36.22 | 36.22 | 36.22 |
| 3 | 14.62 | 6.75 | 5.27 | 6.30 | 5.37 | 6.20 | 5.45 | 5.81 | 5.81 | 5.81 |
| 4 | 23.31 | 12.57 | 11.40 | 12.10 | 11.15 | 11.99 | 11.22 | 11.59 | 11.59 | 11.59 |
| 5 | 11.12 | 4.38 | 2.03 | 3.28 | 2.21 | 3.16 | 2.30 | 2.71 | 2.71 | 2.71 |
| 6 | 13.85 | 5.78 | 3.09 | 4.11 | 3.02 | 4.01 | 3.11 | 3.54 | 3.54 | 3.54 |
| 7 | 10.24 | 3.93 | 1.78 | 3.25 | 2.09 | 3.14 | 2.19 | 2.64 | 2.64 | 2.64 |
| 8 | 12.95 | 5.56 | 3.98 | 5.43 | 4.31 | 5.37 | 4.41 | 4.87 | 4.87 | 4.87 |
| 9 | 8.85 | 3.18 | 0.87 | 2.30 | 1.09 | 2.17 | 1.19 | 1.66 | 1.66 | 1.66 |
| 10 | 10.87 | 4.39 | 2.67 | 4.00 | 2.82 | 3.90 | 2.91 | 3.38 | 3.38 | 3.38 |
| 11 | 9.40 | 3.67 | 2.00 | 3.32 | 2.14 | 3.22 | 2.24 | 2.71 | 2.71 | 2.71 |
| 12 | 10.33 | 4.29 | 2.98 | 4.19 | 3.05 | 4.11 | 3.15 | 3.61 | 3.61 | 3.61 |
| 13 | 9.53 | 4.00 | 2.88 | 3.96 | 2.84 | 3.85 | 2.93 | 3.37 | 3.37 | 3.37 |
| 14 | 8.75 | 3.54 | 2.18 | 3.08 | 2.01 | 2.98 | 2.08 | 2.51 | 2.51 | 2.51 |
| 15 | 8.97 | 4.20 | 4.10 | 5.12 | 4.20 | 5.06 | 4.28 | 4.65 | 4.65 | 4.65 |
| 16 | 10.08 | 5.22 | 5.64 | 6.62 | 5.78 | 6.59 | 5.85 | 6.20 | 6.20 | 6.20 |

Supplementary Material Table 16 – Rate coefficients, $k_{Ar}^{\Delta J}$, for rotationally inelastic collisions of NaK $2(A)^1\Sigma^+(v = 0, J = 30)$ molecules with argon atoms, corrected for multiple collision effects (using $n_{Ar} = 2.13 \times 10^{17} \text{ cm}^{-3}$ and $n_K = 2.12 \times 10^{15} \text{ cm}^{-3}$). The zeroth, first through sixth, 99th, and 100th order (corrected) rate coefficients are given. The final values are the averages of the 5th and 6th iteration values.

| ΔJ | $k_{Ar}^{D \rightarrow C(0)}$ | $k_{Ar}^{D \rightarrow C(n)}$ for iteration n (in units of $10^{-11} \text{ cm}^3 \text{ s}^{-1}$) | | | | | | | | |
|------------|-------------------------------|---|---------|---------|---------|---------|---------|----------|-----------|-------|
| | | $n = 1$ | $n = 2$ | $n = 3$ | $n = 4$ | $n = 5$ | $n = 6$ | $n = 99$ | $n = 100$ | Final |
| -20 | 1.22 | 0.45 | 0.36 | 0.62 | 0.32 | 0.65 | 0.28 | 0.96 | 0.00 | 0.47 |
| -19 | 1.50 | 0.59 | 0.53 | 0.83 | 0.51 | 0.87 | 0.47 | 1.20 | 0.00 | 0.67 |
| -18 | 1.51 | 0.53 | 0.30 | 0.61 | 0.24 | 0.66 | 0.19 | 1.07 | 0.00 | 0.43 |
| -17 | 1.62 | 0.55 | 0.22 | 0.54 | 0.13 | 0.58 | 0.08 | 1.07 | 0.00 | 0.33 |
| -16 | 1.74 | 0.58 | 0.18 | 0.55 | 0.11 | 0.60 | 0.05 | 1.11 | 0.00 | 0.33 |
| -15 | 2.08 | 0.74 | 0.42 | 0.83 | 0.37 | 0.89 | 0.32 | 1.40 | 0.00 | 0.60 |
| -14 | 2.16 | 0.74 | 0.34 | 0.80 | 0.31 | 0.86 | 0.25 | 1.42 | 0.00 | 0.56 |
| -13 | 2.32 | 0.79 | 0.33 | 0.79 | 0.28 | 0.85 | 0.22 | 1.48 | 0.00 | 0.53 |
| -12 | 2.50 | 0.85 | 0.29 | 0.78 | 0.25 | 0.84 | 0.19 | 1.54 | 0.00 | 0.51 |
| -11 | 2.64 | 0.90 | 0.32 | 0.83 | 0.28 | 0.88 | 0.21 | 1.62 | 0.00 | 0.55 |
| -10 | 3.15 | 1.13 | 0.53 | 1.06 | 0.51 | 1.12 | 0.44 | 1.91 | 0.00 | 0.78 |
| -9 | 3.25 | 1.19 | 0.67 | 1.24 | 0.69 | 1.30 | 0.62 | 2.06 | 0.00 | 0.96 |
| -8 | 3.92 | 1.50 | 0.87 | 1.38 | 0.84 | 1.44 | 0.77 | 2.30 | 0.00 | 1.11 |
| -7 | 3.29 | 1.12 | 0.28 | 0.79 | 0.24 | 0.84 | 0.18 | 1.80 | 0.00 | 0.51 |
| -6 | 5.27 | 2.22 | 1.60 | 2.01 | 1.50 | 2.08 | 1.44 | 3.00 | 0.39 | 1.76 |
| -5 | 4.50 | 1.79 | 1.21 | 1.72 | 1.22 | 1.78 | 1.16 | 2.69 | 0.08 | 1.47 |
| -4 | 8.26 | 4.20 | 3.94 | 4.20 | 3.72 | 4.24 | 3.66 | 5.21 | 2.64 | 3.95 |
| -3 | 5.37 | 2.26 | 1.63 | 2.02 | 1.55 | 2.06 | 1.49 | 3.06 | 0.43 | 1.77 |
| -2 | 16.15 | 11.30 | 12.64 | 13.02 | 12.64 | 13.08 | 12.58 | 14.00 | 11.64 | 12.83 |
| -1 | 7.15 | 3.53 | 3.42 | 3.82 | 3.42 | 3.87 | 3.37 | 4.87 | 2.35 | 3.62 |
| 0 | | | | | | | | | | |
| 1 | 6.63 | 3.10 | 2.70 | 2.99 | 2.63 | 3.03 | 2.58 | 4.01 | 1.63 | 2.81 |
| 2 | 16.85 | 12.00 | 13.32 | 13.62 | 13.36 | 13.69 | 13.32 | 14.53 | 12.50 | 13.51 |
| 3 | 5.77 | 2.56 | 1.99 | 2.27 | 1.97 | 2.31 | 1.93 | 3.22 | 1.05 | 2.12 |
| 4 | 8.65 | 4.50 | 4.03 | 4.08 | 3.81 | 4.10 | 3.77 | 4.93 | 2.98 | 3.93 |
| 5 | 5.01 | 2.16 | 1.52 | 1.75 | 1.51 | 1.78 | 1.47 | 2.60 | 0.69 | 1.63 |
| 6 | 6.27 | 2.98 | 2.44 | 2.58 | 2.39 | 2.63 | 2.36 | 3.36 | 1.66 | 2.50 |
| 7 | 4.55 | 2.04 | 1.58 | 1.78 | 1.58 | 1.79 | 1.55 | 2.47 | 0.90 | 1.67 |
| 8 | 4.84 | 2.23 | 1.73 | 1.84 | 1.67 | 1.85 | 1.65 | 2.44 | 1.06 | 1.75 |
| 9 | 4.00 | 1.98 | 1.90 | 2.12 | 1.98 | 2.13 | 1.96 | 2.63 | 1.46 | 2.04 |
| 10 | 4.08 | 2.11 | 2.08 | 2.27 | 2.17 | 2.30 | 2.15 | 2.73 | 1.73 | 2.23 |

Supplementary Material Table 17 – Rate coefficients, $k_{He}^{\Delta J}$, for rotationally inelastic collisions of NaK $2(A)^1\Sigma^+(v = 0, J = 30)$ molecules with helium atoms, corrected for multiple collision effects (using $n_{He} = 2.95 \times 10^{17} \text{ cm}^{-3}$ and $n_K = 3.02 \times 10^{15} \text{ cm}^{-3}$). The zeroth, first through sixth, 99th, and 100th order (corrected) rate coefficients are given. The final values are the averages of the 5th and 6th iteration values.

| ΔJ | $k_{He}^{D \rightarrow C(0)}$ | $k_{He}^{D \rightarrow C(n)}$ for iteration n (in units of $10^{-11} \text{ cm}^3 \text{ s}^{-1}$) | | | | | | | | |
|------------|-------------------------------|---|---------|---------|---------|---------|---------|----------|-----------|-------|
| | | $n = 1$ | $n = 2$ | $n = 3$ | $n = 4$ | $n = 5$ | $n = 6$ | $n = 99$ | $n = 100$ | Final |
| -20 | 3.24 | 1.12 | 0.97 | 1.65 | 0.78 | 1.92 | 0.40 | 3.04 | 0.00 | 1.16 |
| -19 | 3.97 | 1.46 | 1.46 | 2.22 | 1.30 | 2.52 | 0.90 | 3.75 | 0.00 | 1.71 |
| -18 | 3.62 | 1.12 | 0.52 | 1.25 | 0.20 | 1.58 | 0.00 | 3.14 | 0.00 | 0.79 |
| -17 | 3.96 | 1.21 | 0.39 | 1.09 | 0.00 | 1.41 | 0.00 | 3.35 | 0.00 | 0.70 |
| -16 | 4.55 | 1.46 | 0.80 | 1.69 | 0.50 | 2.07 | 0.00 | 4.00 | 0.00 | 1.03 |
| -15 | 5.70 | 2.04 | 1.71 | 2.70 | 1.49 | 3.12 | 0.94 | 5.10 | 0.00 | 2.03 |
| -14 | 4.96 | 1.52 | 0.54 | 1.55 | 0.26 | 1.97 | 0.00 | 4.32 | 0.00 | 0.98 |
| -13 | 5.57 | 1.75 | 0.74 | 1.75 | 0.42 | 2.18 | 0.00 | 4.82 | 0.00 | 1.09 |
| -12 | 5.65 | 1.72 | 0.49 | 1.59 | 0.22 | 2.04 | 0.00 | 4.88 | 0.00 | 1.02 |
| -11 | 6.02 | 1.83 | 0.49 | 1.60 | 0.19 | 2.06 | 0.00 | 5.19 | 0.00 | 1.03 |
| -10 | 7.02 | 2.29 | 1.15 | 2.31 | 0.89 | 2.78 | 0.21 | 6.09 | 0.00 | 1.50 |
| -9 | 7.20 | 2.35 | 1.13 | 2.30 | 0.89 | 2.76 | 0.22 | 6.24 | 0.00 | 1.49 |
| -8 | 7.86 | 2.64 | 1.40 | 2.50 | 1.15 | 2.98 | 0.49 | 6.73 | 0.00 | 1.74 |
| -7 | 8.09 | 2.75 | 1.56 | 2.69 | 1.36 | 3.15 | 0.71 | 6.98 | 0.00 | 1.93 |
| -6 | 9.32 | 3.34 | 2.06 | 2.90 | 1.61 | 3.33 | 0.97 | 7.82 | 0.00 | 2.15 |
| -5 | 9.19 | 3.29 | 2.13 | 3.09 | 1.86 | 3.52 | 1.23 | 7.92 | 0.00 | 2.37 |
| -4 | 14.10 | 6.39 | 6.46 | 7.19 | 6.05 | 7.60 | 5.46 | 11.94 | 0.00 | 6.53 |
| -3 | 10.29 | 3.86 | 2.71 | 3.45 | 2.34 | 3.84 | 1.76 | 8.74 | 0.00 | 2.80 |
| -2 | 23.00 | 13.60 | 16.00 | 16.76 | 15.81 | 17.14 | 15.28 | 21.82 | 9.17 | 16.21 |
| -1 | 13.88 | 6.33 | 6.54 | 7.34 | 6.44 | 7.74 | 5.92 | 12.35 | 0.00 | 6.83 |
| 0 | | | | | | | | | | |
| 1 | 11.75 | 4.77 | 3.78 | 4.14 | 3.36 | 4.45 | 2.88 | 9.94 | 0.00 | 3.67 |
| 2 | 25.16 | 15.69 | 18.28 | 18.77 | 18.20 | 19.13 | 17.79 | 24.18 | 12.04 | 18.46 |
| 3 | 12.04 | 5.15 | 4.57 | 4.98 | 4.42 | 5.32 | 4.02 | 10.43 | 0.00 | 4.67 |
| 4 | 14.55 | 6.75 | 6.17 | 6.09 | 5.59 | 6.36 | 5.22 | 11.70 | 0.00 | 5.79 |
| 5 | 10.57 | 4.32 | 3.30 | 3.46 | 3.02 | 3.72 | 2.66 | 8.95 | 0.00 | 3.19 |
| 6 | 12.87 | 5.95 | 5.55 | 5.58 | 5.26 | 5.86 | 4.95 | 10.92 | 0.00 | 5.41 |
| 7 | 9.98 | 4.28 | 3.57 | 3.70 | 3.40 | 3.92 | 3.11 | 8.44 | 0.00 | 3.51 |
| 8 | 10.66 | 4.80 | 4.18 | 4.10 | 3.85 | 4.27 | 3.58 | 8.81 | 0.00 | 3.93 |
| 9 | 9.66 | 4.68 | 4.82 | 5.06 | 4.88 | 5.24 | 4.66 | 8.77 | 0.74 | 4.95 |
| 10 | 9.86 | 5.06 | 5.39 | 5.61 | 5.51 | 5.81 | 5.33 | 9.00 | 1.78 | 5.57 |

Supplementary Material Table 18 – Rate coefficients, $k_K^{\Delta J}$, for rotationally inelastic collisions of NaK $2(A)^1\Sigma^+(v = 0, J = 30)$ molecules with potassium atoms, corrected for multiple collision effects (using $n_{Ar} = 2.13 \times 10^{17} \text{ cm}^{-3}$ and $n_K = 2.12 \times 10^{15} \text{ cm}^{-3}$). The zeroth, first through sixth, 99th, and 100th order (corrected) rate coefficients are given. The final values are the averages of the 5th and 6th iteration values.

| ΔJ | $k_K^{D \rightarrow C(0)}$ | $k_K^{D \rightarrow C(n)}$ for iteration n (in units of $10^{-10} \text{ cm}^3 \text{ s}^{-1}$) | | | | | | | | |
|------------|----------------------------|--|---------|---------|---------|---------|---------|----------|-----------|-------|
| | | $n = 1$ | $n = 2$ | $n = 3$ | $n = 4$ | $n = 5$ | $n = 6$ | $n = 99$ | $n = 100$ | Final |
| -20 | 2.34 | 0.91 | 0.76 | 1.18 | 0.70 | 1.23 | 0.65 | 1.81 | 0.00 | 0.94 |
| -19 | 2.81 | 1.13 | 1.04 | 1.56 | 1.01 | 1.63 | 0.96 | 2.20 | 0.16 | 1.29 |
| -18 | 3.04 | 1.17 | 0.88 | 1.36 | 0.77 | 1.41 | 0.71 | 2.13 | 0.00 | 1.06 |
| -17 | 2.99 | 1.02 | 0.42 | 0.99 | 0.27 | 1.04 | 0.20 | 1.87 | 0.00 | 0.62 |
| -16 | 0.46 | 0.03 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| -15 | 3.63 | 1.25 | 0.55 | 1.30 | 0.48 | 1.38 | 0.40 | 2.27 | 0.00 | 0.89 |
| -14 | 4.44 | 1.66 | 1.08 | 1.83 | 1.03 | 1.90 | 0.95 | 2.91 | 0.00 | 1.43 |
| -13 | 4.05 | 1.34 | 0.36 | 1.24 | 0.31 | 1.32 | 0.22 | 2.37 | 0.00 | 0.77 |
| -12 | 5.32 | 1.97 | 1.14 | 2.01 | 1.08 | 2.10 | 0.99 | 3.32 | 0.00 | 1.54 |
| -11 | 4.69 | 1.56 | 0.41 | 1.43 | 0.40 | 1.50 | 0.31 | 2.67 | 0.00 | 0.91 |
| -10 | 6.12 | 2.22 | 1.03 | 1.93 | 0.92 | 2.02 | 0.82 | 3.47 | 0.00 | 1.42 |
| -9 | 5.08 | 1.66 | 0.21 | 1.27 | 0.19 | 1.33 | 0.10 | 2.71 | 0.00 | 0.72 |
| -8 | 8.60 | 3.58 | 2.69 | 3.62 | 2.62 | 3.74 | 2.52 | 5.18 | 0.85 | 3.13 |
| -7 | 6.80 | 2.53 | 1.37 | 2.51 | 1.45 | 2.59 | 1.36 | 3.89 | 0.00 | 1.98 |
| -6 | 11.36 | 5.13 | 4.21 | 4.95 | 3.97 | 5.06 | 3.87 | 6.61 | 2.19 | 4.46 |
| -5 | 6.98 | 2.50 | 0.87 | 1.90 | 0.85 | 1.97 | 0.76 | 3.58 | 0.00 | 1.36 |
| -4 | 17.97 | 9.77 | 9.73 | 10.29 | 9.34 | 10.37 | 9.24 | 11.96 | 7.58 | 9.81 |
| -3 | 8.59 | 3.38 | 1.91 | 2.87 | 1.88 | 2.92 | 1.79 | 4.43 | 0.09 | 2.36 |
| -2 | 30.94 | 21.64 | 24.07 | 24.79 | 24.00 | 24.91 | 23.92 | 26.39 | 22.40 | 24.41 |
| -1 | 9.85 | 4.18 | 3.02 | 3.92 | 3.03 | 3.98 | 2.96 | 5.54 | 1.34 | 3.47 |
| 0 | | | | | | | | | | |
| 1 | 10.35 | 4.50 | 3.35 | 4.14 | 3.35 | 4.19 | 3.28 | 5.72 | 1.76 | 3.73 |
| 2 | 33.01 | 23.67 | 26.13 | 26.71 | 26.12 | 26.81 | 26.06 | 28.17 | 24.75 | 26.43 |
| 3 | 9.19 | 3.80 | 2.36 | 3.06 | 2.38 | 3.11 | 2.32 | 4.54 | 0.92 | 2.71 |
| 4 | 19.23 | 10.78 | 10.45 | 10.65 | 10.08 | 10.70 | 10.01 | 11.99 | 8.75 | 10.35 |
| 5 | 8.02 | 3.23 | 1.75 | 2.36 | 1.78 | 2.40 | 1.73 | 3.65 | 0.49 | 2.07 |
| 6 | 13.09 | 6.52 | 5.64 | 5.93 | 5.48 | 6.01 | 5.43 | 7.16 | 4.33 | 5.72 |
| 7 | 7.33 | 3.09 | 2.00 | 2.51 | 2.03 | 2.51 | 1.99 | 3.57 | 0.96 | 2.25 |
| 8 | 9.70 | 4.61 | 3.72 | 3.98 | 3.60 | 4.01 | 3.55 | 4.94 | 2.64 | 3.78 |
| 9 | 6.72 | 3.20 | 2.94 | 3.45 | 3.11 | 3.47 | 3.09 | 4.26 | 2.31 | 3.28 |
| 10 | 8.01 | 4.18 | 4.12 | 4.49 | 4.24 | 4.53 | 4.21 | 5.21 | 3.54 | 4.37 |

Supplementary Material Table 19 – Rate coefficients, $k_{Ar}^{\Delta J}$, for rotationally inelastic collisions of NaK $2(A)^1\Sigma^+(v = 1, J = 26)$ molecules with argon atoms, corrected for multiple collision effects (using $n_{Ar} = 1.50 \times 10^{17} \text{ cm}^{-3}$ and $n_K = 1.48 \times 10^{15} \text{ cm}^{-3}$). The zeroth, first through sixth, 99th, and 100th order (corrected) rate coefficients are given. The final values are the averages of the 99th and 100th iteration values.

| ΔJ | $k_{Ar}^{D \rightarrow C(0)}$ | $k_{Ar}^{D \rightarrow C(n)}$ for iteration n (in units of $10^{-11} \text{ cm}^3 \text{ s}^{-1}$) | | | | | | | | |
|------------|-------------------------------|---|---------|---------|---------|---------|---------|----------|-----------|-------|
| | | $n = 1$ | $n = 2$ | $n = 3$ | $n = 4$ | $n = 5$ | $n = 6$ | $n = 99$ | $n = 100$ | Final |
| -17 | 0.93 | 0.41 | 0.34 | 0.45 | 0.37 | 0.44 | 0.38 | 0.41 | 0.41 | 0.41 |
| -16 | 1.13 | 0.50 | 0.41 | 0.54 | 0.44 | 0.52 | 0.45 | 0.48 | 0.48 | 0.48 |
| -15 | 1.27 | 0.55 | 0.42 | 0.57 | 0.45 | 0.55 | 0.46 | 0.50 | 0.50 | 0.50 |
| -14 | 1.59 | 0.72 | 0.59 | 0.75 | 0.62 | 0.73 | 0.64 | 0.68 | 0.68 | 0.68 |
| -13 | 1.32 | 0.50 | 0.19 | 0.35 | 0.21 | 0.33 | 0.23 | 0.27 | 0.27 | 0.27 |
| -12 | 1.75 | 0.73 | 0.43 | 0.61 | 0.46 | 0.58 | 0.48 | 0.53 | 0.53 | 0.53 |
| -11 | 1.76 | 0.72 | 0.43 | 0.64 | 0.48 | 0.61 | 0.50 | 0.55 | 0.55 | 0.55 |
| -10 | 2.16 | 0.91 | 0.55 | 0.75 | 0.59 | 0.72 | 0.61 | 0.66 | 0.66 | 0.66 |
| -9 | 2.27 | 0.99 | 0.70 | 0.93 | 0.76 | 0.90 | 0.79 | 0.84 | 0.84 | 0.84 |
| -8 | 3.09 | 1.45 | 1.13 | 1.36 | 1.20 | 1.34 | 1.22 | 1.27 | 1.27 | 1.27 |
| -7 | 2.58 | 1.10 | 0.67 | 0.89 | 0.71 | 0.86 | 0.73 | 0.79 | 0.79 | 0.79 |
| -6 | 4.06 | 1.98 | 1.53 | 1.71 | 1.54 | 1.69 | 1.56 | 1.62 | 1.62 | 1.62 |
| -5 | 3.36 | 1.55 | 1.17 | 1.40 | 1.22 | 1.38 | 1.24 | 1.30 | 1.30 | 1.30 |
| -4 | 6.61 | 3.75 | 3.39 | 3.48 | 3.31 | 3.45 | 3.33 | 3.38 | 3.38 | 3.38 |
| -3 | 4.12 | 2.00 | 1.60 | 1.78 | 1.61 | 1.76 | 1.63 | 1.69 | 1.69 | 1.69 |
| -2 | 14.69 | 11.50 | 12.34 | 12.54 | 12.39 | 12.53 | 12.41 | 12.47 | 12.47 | 12.47 |
| -1 | 5.52 | 3.05 | 2.93 | 3.12 | 2.95 | 3.10 | 2.97 | 3.03 | 3.03 | 3.03 |
| 0 | | | | | | | | | | |
| 1 | 5.42 | 2.96 | 2.79 | 2.97 | 2.80 | 2.95 | 2.82 | 2.88 | 2.88 | 2.88 |
| 2 | 14.90 | 11.76 | 12.60 | 12.76 | 12.61 | 12.74 | 12.62 | 12.68 | 12.68 | 12.68 |
| 3 | 4.46 | 2.25 | 1.93 | 2.11 | 1.93 | 2.09 | 1.95 | 2.01 | 2.01 | 2.01 |
| 4 | 6.88 | 4.15 | 4.04 | 4.16 | 4.00 | 4.13 | 4.02 | 4.07 | 4.07 | 4.07 |
| 5 | 3.50 | 1.64 | 1.26 | 1.47 | 1.29 | 1.45 | 1.31 | 1.37 | 1.37 | 1.37 |
| 6 | 1.60 | 0.42 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| 7 | 2.89 | 1.31 | 0.99 | 1.20 | 1.02 | 1.18 | 1.05 | 1.11 | 1.11 | 1.11 |
| 8 | 2.91 | 1.42 | 1.31 | 1.54 | 1.39 | 1.52 | 1.41 | 1.46 | 1.46 | 1.46 |
| 9 | 2.48 | 1.11 | 0.84 | 1.05 | 0.87 | 1.02 | 0.89 | 0.95 | 0.95 | 0.95 |
| 10 | 2.25 | 1.01 | 0.78 | 0.98 | 0.82 | 0.95 | 0.84 | 0.89 | 0.89 | 0.89 |
| 11 | 2.08 | 0.93 | 0.74 | 0.96 | 0.79 | 0.94 | 0.81 | 0.87 | 0.87 | 0.87 |
| 12 | 1.60 | 0.64 | 0.35 | 0.55 | 0.39 | 0.52 | 0.41 | 0.46 | 0.46 | 0.46 |
| 13 | 1.24 | 0.44 | 0.08 | 0.27 | 0.11 | 0.25 | 0.13 | 0.19 | 0.19 | 0.19 |
| 14 | 0.86 | 0.25 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| 15 | 0.94 | 0.31 | 0.00 | 0.15 | 0.00 | 0.13 | 0.02 | 0.07 | 0.07 | 0.07 |
| 16 | 1.21 | 0.51 | 0.39 | 0.57 | 0.45 | 0.56 | 0.47 | 0.51 | 0.51 | 0.51 |
| 17 | 1.13 | 0.47 | 0.35 | 0.53 | 0.40 | 0.51 | 0.42 | 0.46 | 0.46 | 0.46 |
| 18 | 0.93 | 0.36 | 0.20 | 0.34 | 0.22 | 0.32 | 0.24 | 0.27 | 0.27 | 0.27 |
| 19 | 0.88 | 0.34 | 0.17 | 0.29 | 0.18 | 0.28 | 0.19 | 0.23 | 0.23 | 0.23 |
| 20 | 0.70 | 0.25 | 0.04 | 0.14 | 0.03 | 0.12 | 0.04 | 0.08 | 0.08 | 0.08 |
| 21 | 0.78 | 0.31 | 0.15 | 0.24 | 0.14 | 0.22 | 0.15 | 0.18 | 0.18 | 0.18 |
| 22 | 0.76 | 0.35 | 0.34 | 0.44 | 0.37 | 0.43 | 0.38 | 0.40 | 0.40 | 0.40 |
| 23 | 0.93 | 0.50 | 0.55 | 0.64 | 0.57 | 0.63 | 0.58 | 0.61 | 0.61 | 0.61 |

Supplementary Material Table 20 – Rate coefficients, $k_{He}^{\Delta J}$, for rotationally inelastic collisions of NaK $2(A)^1\Sigma^+(v = 1, J = 26)$ molecules with helium atoms, corrected for multiple collision effects (using $n_{He} = 1.13 \times 10^{17} \text{ cm}^{-3}$ and $n_K = 2.92 \times 10^{14} \text{ cm}^{-3}$). The zeroth, first through sixth, 99th, and 100th order (corrected) rate coefficients are given. The final values are the averages of the 5th and 6th iteration values.

| ΔJ | $k_{He}^{D \rightarrow C(0)}$ | $k_{He}^{D \rightarrow C(n)}$ for iteration n (in units of $10^{-11} \text{ cm}^3 \text{ s}^{-1}$) | | | | | | | | |
|------------|-------------------------------|---|---------|---------|---------|---------|---------|----------|-----------|-------|
| | | $n = 1$ | $n = 2$ | $n = 3$ | $n = 4$ | $n = 5$ | $n = 6$ | $n = 99$ | $n = 100$ | Final |
| -17 | 2.11 | 0.87 | 0.71 | 1.02 | 0.78 | 1.01 | 0.78 | 1.31 | 0.48 | 0.89 |
| -16 | 3.79 | 1.78 | 1.65 | 1.93 | 1.71 | 1.94 | 1.70 | 2.25 | 1.39 | 1.82 |
| -15 | 2.32 | 0.85 | 0.38 | 0.71 | 0.40 | 0.70 | 0.40 | 1.07 | 0.02 | 0.55 |
| -14 | 4.80 | 2.20 | 1.85 | 2.15 | 1.88 | 2.16 | 1.87 | 2.55 | 1.48 | 2.01 |
| -13 | 2.80 | 1.02 | 0.41 | 0.78 | 0.42 | 0.77 | 0.41 | 1.22 | 0.00 | 0.59 |
| -12 | 5.30 | 2.26 | 1.47 | 1.73 | 1.41 | 1.75 | 1.40 | 2.20 | 0.94 | 1.57 |
| -11 | 3.70 | 1.50 | 1.09 | 1.57 | 1.18 | 1.57 | 1.17 | 2.06 | 0.68 | 1.37 |
| -10 | 7.00 | 3.26 | 2.69 | 3.02 | 2.70 | 3.06 | 2.68 | 3.55 | 2.19 | 2.87 |
| -9 | 3.82 | 1.45 | 0.78 | 1.25 | 0.80 | 1.24 | 0.79 | 1.78 | 0.24 | 1.02 |
| -8 | 8.65 | 4.20 | 3.60 | 3.88 | 3.53 | 3.93 | 3.51 | 4.46 | 2.98 | 3.72 |
| -7 | 4.35 | 1.70 | 1.05 | 1.59 | 1.11 | 1.59 | 1.10 | 2.18 | 0.50 | 1.34 |
| -6 | 11.26 | 5.91 | 5.50 | 5.72 | 5.34 | 5.76 | 5.32 | 6.32 | 4.76 | 5.54 |
| -5 | 4.23 | 1.53 | 0.56 | 1.08 | 0.56 | 1.08 | 0.55 | 1.72 | 0.00 | 0.82 |
| -4 | 15.10 | 8.74 | 8.72 | 8.86 | 8.45 | 8.90 | 8.43 | 9.47 | 7.86 | 8.66 |
| -3 | 5.24 | 2.12 | 1.45 | 2.03 | 1.50 | 2.04 | 1.49 | 2.69 | 0.83 | 1.76 |
| -2 | 24.13 | 17.15 | 18.74 | 19.04 | 18.66 | 19.09 | 18.64 | 19.65 | 18.08 | 18.87 |
| -1 | 5.78 | 2.43 | 1.84 | 2.42 | 1.87 | 2.43 | 1.86 | 3.10 | 1.18 | 2.15 |
| 0 | | | | | | | | | | |
| 1 | 5.91 | 2.48 | 1.85 | 2.41 | 1.84 | 2.42 | 1.83 | 3.10 | 1.14 | 2.12 |
| 2 | 24.82 | 17.90 | 19.60 | 19.91 | 19.47 | 19.93 | 19.46 | 20.48 | 18.90 | 19.69 |
| 3 | 5.58 | 2.25 | 1.52 | 2.09 | 1.51 | 2.10 | 1.50 | 2.78 | 0.81 | 1.80 |
| 4 | 16.58 | 10.39 | 11.14 | 11.52 | 11.09 | 11.55 | 11.08 | 12.08 | 10.52 | 11.31 |
| 5 | 5.35 | 2.13 | 1.38 | 1.96 | 1.37 | 1.96 | 1.36 | 2.62 | 0.67 | 1.66 |
| 6 | 4.78 | 1.43 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| 7 | 5.49 | 2.29 | 1.78 | 2.38 | 1.80 | 2.39 | 1.80 | 3.03 | 1.13 | 2.09 |
| 8 | 7.46 | 3.48 | 3.12 | 3.63 | 3.18 | 3.64 | 3.17 | 4.16 | 2.62 | 3.41 |
| 9 | 4.89 | 1.97 | 1.39 | 1.95 | 1.38 | 1.95 | 1.38 | 2.54 | 0.74 | 1.66 |
| 10 | 6.18 | 2.73 | 2.24 | 2.72 | 2.25 | 2.71 | 2.25 | 3.22 | 1.71 | 2.48 |
| 11 | 4.26 | 1.67 | 1.11 | 1.68 | 1.14 | 1.68 | 1.14 | 2.21 | 0.54 | 1.41 |
| 12 | 6.03 | 2.79 | 2.57 | 3.03 | 2.59 | 3.03 | 2.58 | 3.50 | 2.06 | 2.81 |
| 13 | 3.13 | 1.07 | 0.29 | 0.82 | 0.32 | 0.82 | 0.32 | 1.31 | 0.00 | 0.57 |
| 14 | 2.80 | 0.82 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.26 | 0.00 | 0.00 |
| 15 | 2.41 | 0.74 | 0.00 | 0.37 | 0.00 | 0.36 | 0.00 | 0.84 | 0.00 | 0.18 |
| 16 | 3.97 | 1.68 | 1.40 | 1.83 | 1.45 | 1.82 | 1.46 | 2.19 | 1.02 | 1.64 |
| 17 | 2.65 | 0.96 | 0.53 | 1.01 | 0.59 | 1.01 | 0.59 | 1.36 | 0.14 | 0.80 |
| 18 | 3.28 | 1.37 | 1.13 | 1.54 | 1.19 | 1.53 | 1.19 | 1.85 | 0.81 | 1.36 |
| 19 | 2.29 | 0.82 | 0.40 | 0.79 | 0.41 | 0.79 | 0.41 | 1.11 | 0.01 | 0.60 |
| 20 | 2.05 | 0.67 | 0.02 | 0.27 | 0.00 | 0.25 | 0.00 | 0.59 | 0.00 | 0.12 |
| 21 | 1.79 | 0.60 | 0.12 | 0.41 | 0.06 | 0.39 | 0.07 | 0.72 | 0.00 | 0.23 |
| 22 | 2.23 | 0.96 | 0.91 | 1.23 | 0.97 | 1.23 | 0.98 | 1.44 | 0.69 | 1.10 |
| 23 | 2.16 | 0.98 | 1.03 | 1.34 | 1.08 | 1.34 | 1.09 | 1.56 | 0.81 | 1.21 |

Supplementary Material Table 21 – Rate coefficients, $k_K^{\Delta J}$, for rotationally inelastic collisions of NaK $2(A)^1\Sigma^+(v = 1, J = 26)$ molecules with potassium atoms, corrected for multiple collision effects (using $n_{Ar} = 1.50 \times 10^{17} \text{ cm}^{-3}$ and $n_K = 1.48 \times 10^{15} \text{ cm}^{-3}$). The zeroth, first through sixth, 99th, and 100th order (corrected) rate coefficients are given. The final values are the averages of the 99th and 100th iteration values.

| ΔJ | $k_K^{D \rightarrow C(0)}$ | $k_K^{D \rightarrow C(n)}$ for iteration n (in units of $10^{-10} \text{ cm}^3 \text{ s}^{-1}$) | | | | | | | | |
|------------|----------------------------|--|-------|-------|-------|-------|-------|--------|---------|-------|
| | | $n=1$ | $n=2$ | $n=3$ | $n=4$ | $n=5$ | $n=6$ | $n=99$ | $n=100$ | Final |
| -17 | 2.32 | 1.13 | 1.12 | 1.45 | 1.23 | 1.42 | 1.26 | 1.34 | 1.34 | 1.34 |
| -16 | 2.00 | 0.81 | 0.49 | 0.83 | 0.57 | 0.78 | 0.60 | 0.69 | 0.69 | 0.69 |
| -15 | 1.81 | 0.61 | 0.00 | 0.27 | 0.00 | 0.21 | 0.00 | 0.09 | 0.09 | 0.09 |
| -14 | 2.78 | 1.12 | 0.61 | 1.05 | 0.71 | 0.99 | 0.75 | 0.86 | 0.86 | 0.86 |
| -13 | 2.74 | 1.03 | 0.32 | 0.78 | 0.41 | 0.72 | 0.46 | 0.58 | 0.58 | 0.58 |
| -12 | 3.28 | 1.24 | 0.33 | 0.80 | 0.41 | 0.74 | 0.46 | 0.58 | 0.58 | 0.58 |
| -11 | 3.66 | 1.48 | 0.77 | 1.32 | 0.90 | 1.25 | 0.96 | 1.09 | 1.09 | 1.09 |
| -10 | 5.04 | 2.19 | 1.40 | 1.95 | 1.53 | 1.89 | 1.58 | 1.72 | 1.72 | 1.72 |
| -9 | 4.82 | 2.07 | 1.35 | 1.93 | 1.46 | 1.85 | 1.52 | 1.67 | 1.67 | 1.67 |
| -8 | 6.89 | 3.17 | 2.21 | 2.71 | 2.26 | 2.65 | 2.32 | 2.47 | 2.47 | 2.47 |
| -7 | 6.25 | 2.88 | 2.20 | 2.84 | 2.36 | 2.77 | 2.42 | 2.58 | 2.58 | 2.58 |
| -6 | 11.83 | 6.51 | 5.98 | 6.46 | 6.01 | 6.42 | 6.07 | 6.23 | 6.23 | 6.23 |
| -5 | 5.96 | 2.48 | 1.22 | 1.82 | 1.30 | 1.74 | 1.37 | 1.54 | 1.54 | 1.54 |
| -4 | 17.89 | 10.93 | 10.48 | 10.77 | 10.29 | 10.69 | 10.34 | 10.50 | 10.50 | 10.50 |
| -3 | 7.50 | 3.43 | 2.36 | 3.02 | 2.52 | 2.96 | 2.58 | 2.76 | 2.76 | 2.76 |
| -2 | 34.31 | 27.02 | 28.79 | 29.27 | 28.86 | 29.24 | 28.91 | 29.06 | 29.06 | 29.06 |
| -1 | 7.11 | 3.06 | 1.57 | 2.12 | 1.59 | 2.03 | 1.65 | 1.83 | 1.83 | 1.83 |
| 0 | | | | | | | | | | |
| 1 | 10.07 | 5.32 | 4.85 | 5.54 | 5.04 | 5.48 | 5.10 | 5.28 | 5.28 | 5.28 |
| 2 | 35.17 | 28.14 | 29.92 | 30.36 | 29.93 | 30.30 | 29.98 | 30.13 | 30.13 | 30.13 |
| 3 | 7.00 | 3.05 | 1.70 | 2.27 | 1.74 | 2.18 | 1.80 | 1.98 | 1.98 | 1.98 |
| 4 | 18.81 | 12.35 | 12.54 | 12.96 | 12.53 | 12.90 | 12.59 | 12.73 | 12.73 | 12.73 |
| 5 | 5.89 | 2.45 | 1.18 | 1.77 | 1.24 | 1.68 | 1.31 | 1.48 | 1.48 | 1.48 |
| 6 | 4.10 | 1.19 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| 7 | 6.07 | 2.83 | 2.25 | 2.95 | 2.45 | 2.88 | 2.52 | 2.69 | 2.69 | 2.69 |
| 8 | 5.64 | 2.62 | 2.16 | 2.78 | 2.36 | 2.72 | 2.42 | 2.56 | 2.56 | 2.56 |
| 9 | 4.06 | 1.60 | 0.66 | 1.25 | 0.74 | 1.15 | 0.81 | 0.96 | 0.96 | 0.96 |
| 10 | 4.11 | 1.72 | 1.05 | 1.57 | 1.13 | 1.49 | 1.18 | 1.32 | 1.32 | 1.32 |
| 11 | 2.90 | 1.03 | 0.11 | 0.68 | 0.21 | 0.60 | 0.27 | 0.42 | 0.42 | 0.42 |
| 12 | 3.96 | 1.79 | 1.45 | 1.94 | 1.54 | 1.87 | 1.59 | 1.72 | 1.72 | 1.72 |
| 13 | 2.35 | 0.81 | 0.03 | 0.56 | 0.15 | 0.50 | 0.21 | 0.34 | 0.34 | 0.34 |
| 14 | 0.95 | 0.17 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| 15 | 1.84 | 0.60 | 0.00 | 0.37 | 0.00 | 0.30 | 0.03 | 0.15 | 0.15 | 0.15 |
| 16 | 1.75 | 0.59 | 0.03 | 0.38 | 0.07 | 0.33 | 0.11 | 0.21 | 0.21 | 0.21 |
| 17 | 1.70 | 0.59 | 0.09 | 0.48 | 0.16 | 0.44 | 0.20 | 0.31 | 0.31 | 0.31 |
| 18 | 2.46 | 1.14 | 1.04 | 1.41 | 1.14 | 1.37 | 1.18 | 1.27 | 1.27 | 1.27 |
| 19 | 1.83 | 0.73 | 0.41 | 0.74 | 0.47 | 0.70 | 0.51 | 0.60 | 0.60 | 0.60 |
| 20 | 1.33 | 0.44 | 0.00 | 0.14 | 0.00 | 0.09 | 0.00 | 0.00 | 0.00 | 0.00 |
| 21 | 1.22 | 0.41 | 0.00 | 0.16 | 0.00 | 0.11 | 0.00 | 0.02 | 0.02 | 0.02 |
| 22 | 2.00 | 1.07 | 1.17 | 1.41 | 1.23 | 1.39 | 1.26 | 1.33 | 1.33 | 1.33 |
| 23 | 1.83 | 0.98 | 1.06 | 1.27 | 1.10 | 1.24 | 1.13 | 1.19 | 1.19 | 1.19 |

Supplementary Material Table 22 – Rate coefficients, $k_{Ar}^{\Delta J}$, for rotationally inelastic collisions of NaK $2(A)^1\Sigma^+(v = 2, J = 44)$ molecules with argon atoms, corrected for multiple collision effects (using $n_{Ar} = 1.69 \times 10^{17} \text{ cm}^{-3}$ and $n_K = 1.65 \times 10^{14} \text{ cm}^{-3}$). The zeroth, first through sixth, 99th, and 100th order (corrected) rate coefficients are given. The final values are the averages of the 99th and 100th iteration values.

| ΔJ | $k_{Ar}^{D \rightarrow C(0)}$ | $k_{Ar}^{D \rightarrow C(n)}$ for iteration n (in units of $10^{-11} \text{ cm}^3 \text{ s}^{-1}$) | | | | | | | | |
|------------|-------------------------------|---|---------|---------|---------|---------|---------|----------|-----------|-------|
| | | $n = 1$ | $n = 2$ | $n = 3$ | $n = 4$ | $n = 5$ | $n = 6$ | $n = 99$ | $n = 100$ | Final |
| -17 | 0.93 | 0.44 | 0.44 | 0.56 | 0.48 | 0.55 | 0.49 | 0.52 | 0.52 | 0.52 |
| -16 | 0.73 | 0.27 | 0.11 | 0.23 | 0.14 | 0.22 | 0.15 | 0.18 | 0.18 | 0.18 |
| -15 | 0.85 | 0.29 | 0.03 | 0.16 | 0.05 | 0.14 | 0.06 | 0.10 | 0.10 | 0.10 |
| -14 | 1.09 | 0.41 | 0.18 | 0.32 | 0.21 | 0.31 | 0.22 | 0.26 | 0.26 | 0.26 |
| -13 | 1.28 | 0.49 | 0.22 | 0.39 | 0.26 | 0.37 | 0.27 | 0.32 | 0.32 | 0.32 |
| -12 | 1.65 | 0.68 | 0.43 | 0.61 | 0.47 | 0.59 | 0.48 | 0.53 | 0.53 | 0.53 |
| -11 | 1.90 | 0.81 | 0.57 | 0.76 | 0.62 | 0.74 | 0.63 | 0.69 | 0.69 | 0.69 |
| -10 | 2.27 | 0.98 | 0.69 | 0.87 | 0.72 | 0.85 | 0.73 | 0.79 | 0.79 | 0.79 |
| -9 | 2.36 | 1.01 | 0.69 | 0.88 | 0.72 | 0.86 | 0.74 | 0.80 | 0.80 | 0.80 |
| -8 | 3.21 | 1.53 | 1.27 | 1.46 | 1.31 | 1.45 | 1.32 | 1.38 | 1.38 | 1.38 |
| -7 | 3.03 | 1.36 | 1.02 | 1.22 | 1.06 | 1.21 | 1.07 | 1.14 | 1.14 | 1.14 |
| -6 | 4.14 | 2.02 | 1.64 | 1.79 | 1.63 | 1.78 | 1.64 | 1.71 | 1.71 | 1.71 |
| -5 | 3.83 | 1.82 | 1.48 | 1.67 | 1.50 | 1.65 | 1.51 | 1.58 | 1.58 | 1.58 |
| -4 | 6.58 | 3.71 | 3.48 | 3.57 | 3.39 | 3.55 | 3.41 | 3.47 | 3.47 | 3.47 |
| -3 | 4.83 | 2.47 | 2.25 | 2.44 | 2.27 | 2.43 | 2.28 | 2.36 | 2.36 | 2.36 |
| -2 | 14.03 | 10.73 | 11.64 | 11.83 | 11.67 | 11.82 | 11.68 | 11.75 | 11.75 | 11.75 |
| -1 | 5.15 | 2.60 | 2.27 | 2.42 | 2.23 | 2.40 | 2.24 | 2.32 | 2.32 | 2.32 |
| 0 | | | | | | | | | | |
| 1 | 6.04 | 3.36 | 3.33 | 3.54 | 3.36 | 3.53 | 3.38 | 3.45 | 3.45 | 3.45 |
| 2 | 13.83 | 10.47 | 11.37 | 11.56 | 11.40 | 11.56 | 11.42 | 11.48 | 11.48 | 11.48 |
| 3 | 4.84 | 2.41 | 2.09 | 2.27 | 2.08 | 2.25 | 2.10 | 2.17 | 2.17 | 2.17 |
| 4 | 6.68 | 3.74 | 3.52 | 3.63 | 3.45 | 3.61 | 3.46 | 3.53 | 3.53 | 3.53 |
| 5 | 3.89 | 1.80 | 1.42 | 1.63 | 1.45 | 1.61 | 1.46 | 1.54 | 1.54 | 1.54 |
| 6 | 4.21 | 2.00 | 1.56 | 1.73 | 1.56 | 1.71 | 1.57 | 1.64 | 1.64 | 1.64 |
| 7 | 3.10 | 1.35 | 0.94 | 1.17 | 0.99 | 1.15 | 1.01 | 1.08 | 1.08 | 1.08 |
| 8 | 3.42 | 1.59 | 1.29 | 1.51 | 1.34 | 1.50 | 1.36 | 1.42 | 1.42 | 1.42 |
| 9 | 2.48 | 1.02 | 0.61 | 0.83 | 0.66 | 0.81 | 0.68 | 0.74 | 0.74 | 0.74 |
| 10 | 2.54 | 1.08 | 0.68 | 0.87 | 0.71 | 0.85 | 0.72 | 0.78 | 0.78 | 0.78 |
| 11 | 2.12 | 0.87 | 0.51 | 0.70 | 0.55 | 0.68 | 0.56 | 0.62 | 0.62 | 0.62 |
| 12 | 2.33 | 1.05 | 0.82 | 1.01 | 0.87 | 0.99 | 0.88 | 0.93 | 0.93 | 0.93 |
| 13 | 1.99 | 0.87 | 0.64 | 0.79 | 0.65 | 0.77 | 0.67 | 0.71 | 0.71 | 0.71 |
| 14 | 1.79 | 0.77 | 0.54 | 0.68 | 0.55 | 0.66 | 0.56 | 0.61 | 0.61 | 0.61 |
| 15 | 1.90 | 0.97 | 0.98 | 1.12 | 1.02 | 1.11 | 1.03 | 1.07 | 1.07 | 1.07 |
| 16 | 1.48 | 0.69 | 0.62 | 0.75 | 0.65 | 0.73 | 0.66 | 0.70 | 0.70 | 0.70 |

Supplementary Material Table 23 – Rate coefficients, $k_{He}^{\Delta J}$, for rotationally inelastic collisions of NaK $2(A)^1\Sigma^+(v = 2, J = 44)$ molecules with helium atoms, corrected for multiple collision effects (using $n_{He} = 1.13 \times 10^{17} \text{ cm}^{-3}$ and $n_K = 2.92 \times 10^{14} \text{ cm}^{-3}$). The zeroth, first through sixth, 999th, and 1000th order (corrected) rate coefficients are given. The final values are the averages of the 999th and 1000th iteration values.

| ΔJ | $k_{He}^{D \rightarrow C(0)}$ | $k_{He}^{D \rightarrow C(n)}$ for iteration n (in units of $10^{-11} \text{ cm}^3 \text{ s}^{-1}$) | | | | | | | | |
|------------|-------------------------------|---|---------|---------|---------|---------|---------|-----------|------------|-------|
| | | $n = 1$ | $n = 2$ | $n = 3$ | $n = 4$ | $n = 5$ | $n = 6$ | $n = 999$ | $n = 1000$ | Final |
| -17 | 1.86 | 0.82 | 0.79 | 1.05 | 0.89 | 1.04 | 0.90 | 0.97 | 0.97 | 0.97 |
| -16 | 1.81 | 0.63 | 0.13 | 0.38 | 0.21 | 0.37 | 0.21 | 0.29 | 0.29 | 0.29 |
| -15 | 1.50 | 0.46 | 0.00 | 0.10 | 0.00 | 0.07 | 0.00 | 0.00 | 0.00 | 0.00 |
| -14 | 2.81 | 1.05 | 0.40 | 0.65 | 0.44 | 0.64 | 0.44 | 0.54 | 0.54 | 0.54 |
| -13 | 2.34 | 0.85 | 0.37 | 0.68 | 0.42 | 0.66 | 0.43 | 0.55 | 0.55 | 0.55 |
| -12 | 4.73 | 2.12 | 1.64 | 1.92 | 1.67 | 1.92 | 1.67 | 1.80 | 1.80 | 1.80 |
| -11 | 3.23 | 1.30 | 0.90 | 1.28 | 0.97 | 1.26 | 0.98 | 1.12 | 1.12 | 1.12 |
| -10 | 6.79 | 3.32 | 2.95 | 3.22 | 2.95 | 3.23 | 2.95 | 3.09 | 3.09 | 3.09 |
| -9 | 3.66 | 1.45 | 0.90 | 1.28 | 0.92 | 1.26 | 0.94 | 1.10 | 1.10 | 1.10 |
| -8 | 8.67 | 4.39 | 3.98 | 4.21 | 3.92 | 4.23 | 3.92 | 4.07 | 4.07 | 4.07 |
| -7 | 4.38 | 1.81 | 1.30 | 1.74 | 1.34 | 1.72 | 1.36 | 1.54 | 1.54 | 1.54 |
| -6 | 11.03 | 5.87 | 5.53 | 5.71 | 5.41 | 5.74 | 5.40 | 5.57 | 5.57 | 5.57 |
| -5 | 4.95 | 2.09 | 1.60 | 2.08 | 1.65 | 2.06 | 1.67 | 1.86 | 1.86 | 1.86 |
| -4 | 14.68 | 8.48 | 8.45 | 8.57 | 8.24 | 8.59 | 8.23 | 8.41 | 8.41 | 8.41 |
| -3 | 4.99 | 2.02 | 1.36 | 1.86 | 1.40 | 1.83 | 1.41 | 1.62 | 1.62 | 1.62 |
| -2 | 23.70 | 16.71 | 18.27 | 18.56 | 18.24 | 18.60 | 18.24 | 18.42 | 18.42 | 18.42 |
| -1 | 5.19 | 2.10 | 1.42 | 1.96 | 1.47 | 1.93 | 1.49 | 1.71 | 1.71 | 1.71 |
| 0 | | | | | | | | | | |
| 1 | 5.34 | 2.19 | 1.56 | 2.12 | 1.64 | 2.10 | 1.65 | 1.87 | 1.87 | 1.87 |
| 2 | 24.56 | 17.31 | 18.94 | 19.25 | 18.92 | 19.29 | 18.91 | 19.10 | 19.10 | 19.10 |
| 3 | 4.98 | 1.95 | 1.18 | 1.71 | 1.22 | 1.69 | 1.24 | 1.46 | 1.46 | 1.46 |
| 4 | 15.59 | 8.93 | 8.88 | 9.02 | 8.67 | 9.04 | 8.66 | 8.85 | 8.85 | 8.85 |
| 5 | 4.78 | 1.87 | 1.12 | 1.65 | 1.18 | 1.62 | 1.19 | 1.40 | 1.40 | 1.40 |
| 6 | 11.65 | 5.98 | 5.41 | 5.62 | 5.28 | 5.65 | 5.27 | 5.46 | 5.46 | 5.46 |
| 7 | 4.52 | 1.77 | 1.08 | 1.59 | 1.15 | 1.57 | 1.16 | 1.36 | 1.36 | 1.36 |
| 8 | 9.73 | 4.81 | 4.27 | 4.56 | 4.25 | 4.60 | 4.24 | 4.42 | 4.42 | 4.42 |
| 9 | 4.01 | 1.53 | 0.80 | 1.26 | 0.85 | 1.24 | 0.86 | 1.05 | 1.05 | 1.05 |
| 10 | 7.48 | 3.38 | 2.54 | 2.79 | 2.49 | 2.81 | 2.48 | 2.64 | 2.64 | 2.64 |
| 11 | 3.64 | 1.39 | 0.74 | 1.14 | 0.77 | 1.12 | 0.78 | 0.95 | 0.95 | 0.95 |
| 12 | 7.04 | 3.39 | 3.01 | 3.33 | 3.06 | 3.35 | 3.05 | 3.20 | 3.20 | 3.20 |
| 13 | 3.56 | 1.46 | 1.05 | 1.39 | 1.06 | 1.36 | 1.06 | 1.21 | 1.21 | 1.21 |
| 14 | 5.32 | 2.40 | 1.89 | 2.13 | 1.88 | 2.13 | 1.87 | 2.00 | 2.00 | 2.00 |
| 15 | 3.69 | 1.79 | 1.84 | 2.18 | 1.92 | 2.17 | 1.93 | 2.05 | 2.05 | 2.05 |
| 16 | 4.26 | 1.98 | 1.76 | 2.02 | 1.82 | 2.03 | 1.82 | 1.93 | 1.93 | 1.93 |

Supplementary Material Table 24 – Rate coefficients, $k_K^{\Delta J}$, for rotationally inelastic collisions of NaK $2(A)^1\Sigma^+(v = 2, J = 44)$ molecules with potassium atoms, corrected for multiple collision effects (using $n_{Ar} = 1.69 \times 10^{17} \text{ cm}^{-3}$ and $n_K = 1.65 \times 10^{14} \text{ cm}^{-3}$). The zeroth, first through sixth, 99th, and 100th order (corrected) rate coefficients are given. The final values are the averages of the 99th and 100th iteration values.

| ΔJ | $k_K^{D \rightarrow C(0)}$ | $k_K^{D \rightarrow C(n)}$ for iteration n (in units of $10^{-10} \text{ cm}^3 \text{ s}^{-1}$) | | | | | | | | |
|------------|----------------------------|--|---------|---------|---------|---------|---------|----------|-----------|-------|
| | | $n = 1$ | $n = 2$ | $n = 3$ | $n = 4$ | $n = 5$ | $n = 6$ | $n = 99$ | $n = 100$ | Final |
| -17 | 0.50 | 0.14 | 0.00 | 0.07 | 0.00 | 0.04 | 0.00 | 0.01 | 0.01 | 0.01 |
| -16 | 0.33 | 0.06 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| -15 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| -14 | 1.06 | 0.32 | 0.00 | 0.05 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| -13 | 1.28 | 0.41 | 0.00 | 0.17 | 0.00 | 0.10 | 0.00 | 0.02 | 0.02 | 0.02 |
| -12 | 2.44 | 1.03 | 0.61 | 1.02 | 0.74 | 0.96 | 0.79 | 0.87 | 0.87 | 0.87 |
| -11 | 1.96 | 0.71 | 0.06 | 0.52 | 0.21 | 0.45 | 0.27 | 0.35 | 0.35 | 0.35 |
| -10 | 3.55 | 1.60 | 1.09 | 1.59 | 1.24 | 1.52 | 1.30 | 1.40 | 1.40 | 1.40 |
| -9 | 2.63 | 1.00 | 0.21 | 0.76 | 0.41 | 0.68 | 0.47 | 0.56 | 0.56 | 0.56 |
| -8 | 3.81 | 1.53 | 0.43 | 0.90 | 0.49 | 0.82 | 0.55 | 0.67 | 0.67 | 0.67 |
| -7 | 2.37 | 0.74 | 0.00 | 0.04 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| -6 | 8.44 | 4.62 | 4.11 | 4.65 | 4.21 | 4.58 | 4.28 | 4.41 | 4.41 | 4.41 |
| -5 | 3.51 | 1.30 | 0.02 | 0.69 | 0.23 | 0.60 | 0.31 | 0.44 | 0.44 | 0.44 |
| -4 | 14.16 | 8.85 | 8.51 | 8.93 | 8.43 | 8.83 | 8.50 | 8.65 | 8.65 | 8.65 |
| -3 | 3.89 | 1.44 | 0.00 | 0.70 | 0.18 | 0.60 | 0.25 | 0.41 | 0.41 | 0.41 |
| -2 | 29.57 | 24.00 | 25.49 | 26.09 | 25.62 | 26.02 | 25.69 | 25.84 | 25.84 | 25.84 |
| -1 | 4.33 | 1.62 | 0.00 | 0.70 | 0.13 | 0.59 | 0.21 | 0.38 | 0.38 | 0.38 |
| 0 | | | | | | | | | | |
| 1 | 4.79 | 1.94 | 0.61 | 1.41 | 0.84 | 1.32 | 0.92 | 1.11 | 1.11 | 1.11 |
| 2 | 30.08 | 24.32 | 25.87 | 26.50 | 25.98 | 26.44 | 26.06 | 26.23 | 26.23 | 26.23 |
| 3 | 4.10 | 1.50 | 0.00 | 0.65 | 0.05 | 0.55 | 0.13 | 0.32 | 0.32 | 0.32 |
| 4 | 14.80 | 9.25 | 8.99 | 9.48 | 8.90 | 9.39 | 8.98 | 9.16 | 9.16 | 9.16 |
| 5 | 3.58 | 1.26 | 0.00 | 0.58 | 0.00 | 0.48 | 0.06 | 0.25 | 0.25 | 0.25 |
| 6 | 8.59 | 4.53 | 3.87 | 4.46 | 3.90 | 4.39 | 3.97 | 4.16 | 4.16 | 4.16 |
| 7 | 3.29 | 1.18 | 0.00 | 0.73 | 0.17 | 0.66 | 0.25 | 0.44 | 0.44 | 0.44 |
| 8 | 5.26 | 2.38 | 1.58 | 2.20 | 1.67 | 2.14 | 1.74 | 1.92 | 1.92 | 1.92 |
| 9 | 3.21 | 1.24 | 0.38 | 1.08 | 0.54 | 1.00 | 0.61 | 0.79 | 0.79 | 0.79 |
| 10 | 3.55 | 1.41 | 0.47 | 1.02 | 0.51 | 0.95 | 0.57 | 0.75 | 0.75 | 0.75 |
| 11 | 2.51 | 0.91 | 0.08 | 0.68 | 0.19 | 0.61 | 0.25 | 0.42 | 0.42 | 0.42 |
| 12 | 3.36 | 1.47 | 0.97 | 1.51 | 1.06 | 1.45 | 1.12 | 1.27 | 1.27 | 1.27 |
| 13 | 1.97 | 0.69 | 0.00 | 0.45 | 0.02 | 0.38 | 0.07 | 0.21 | 0.21 | 0.21 |
| 14 | 2.59 | 1.10 | 0.66 | 1.08 | 0.70 | 1.03 | 0.74 | 0.87 | 0.87 | 0.87 |
| 15 | 1.80 | 0.74 | 0.48 | 0.89 | 0.57 | 0.85 | 0.61 | 0.72 | 0.72 | 0.72 |
| 16 | 1.61 | 0.63 | 0.31 | 0.65 | 0.36 | 0.62 | 0.40 | 0.50 | 0.50 | 0.50 |

Supplementary Material Table 25 – Rate coefficients ($k_p^{\Delta J}$) in units of the radiative rate Γ and in units of cm^3s^{-1} [obtained by multiplying the fitted parameters ($k_p^{\Delta J}/\Gamma$) by $\Gamma = 2.82 \times 10^7 \text{ s}^{-1}$] for rotationally inelastic collisions of NaCs $2(A)^1\Sigma^+(v = 14, J = 32)$ molecules with argon and cesium atoms ($p = Ar$ and Cs). In this fit, the value of k_{Cs}^Q/Γ was allowed to vary freely.

| ΔJ | $k_{Ar}^{\Delta J}/\Gamma$ (10^{-18} cm^3) | $k_{Cs}^{\Delta J}/\Gamma$ (10^{-17} cm^3) | $k_{Ar}^{\Delta J}$ ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | $k_{Cs}^{\Delta J}$ ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
|------------|---|---|---|---|
| -4 | 0.77 ± 0.13 | 0.06 ± 0.06 | 2.16 ± 0.35 | 0.18 ± 0.17 |
| -3 | 0.88 ± 0.13 | 0.14 ± 0.07 | 2.47 ± 0.37 | 0.39 ± 0.21 |
| -2 | 1.63 ± 0.21 | 0.17 ± 0.11 | 4.61 ± 0.58 | 0.49 ± 0.30 |
| -1 | 3.57 ± 0.43 | 0.32 ± 0.21 | 10.06 ± 1.22 | 0.89 ± 0.60 |
| 0 | | | | |
| 1 | 3.33 ± 0.39 | 0.00 ± 0.14 | 9.38 ± 1.09 | 0.00 ± 0.40 |
| 2 | 1.89 ± 0.23 | 0.18 ± 0.12 | 5.34 ± 0.66 | 0.52 ± 0.33 |
| 3 | 1.03 ± 0.14 | 0.11 ± 0.07 | 2.92 ± 0.39 | 0.32 ± 0.19 |
| 4 | 0.79 ± 0.10 | 0.02 ± 0.03 | 2.21 ± 0.29 | 0.06 ± 0.10 |
| | k_{Ar}^Q/Γ (10^{-18} cm^3) | k_{Cs}^Q/Γ (10^{-17} cm^3) | k_{Ar}^Q ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | k_{Cs}^Q ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
| | 25.77 ± 4.47 | 2.24 ± 2.28 | 72.68 ± 12.61 | 6.32 ± 6.43 |

Supplementary Material Table 26 – Rate coefficients ($k_p^{\Delta J}$) in units of the radiative rate Γ and in units of cm^3s^{-1} [obtained by multiplying the fitted parameters ($k_p^{\Delta J}/\Gamma$) by $\Gamma = 2.82 \times 10^7 \text{ s}^{-1}$] for rotationally inelastic collisions of NaCs $2(A)^1\Sigma^+(v = 14, J = 32)$ molecules with argon and cesium atoms ($p = Ar$ and Cs). In this fit, the value of k_{Cs}^Q/Γ was allowed to vary between the limits $1 \times 10^{-17} \text{ cm}^3$ and $1 \times 10^{-15} \text{ cm}^3$.

| ΔJ | $k_{Ar}^{\Delta J}/\Gamma$ (10^{-18} cm^3) | $k_{Cs}^{\Delta J}/\Gamma$ (10^{-17} cm^3) | $k_{Ar}^{\Delta J}$ ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | $k_{Cs}^{\Delta J}$ ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
|------------|---|---|---|---|
| -4 | 0.77 ± 0.13 | 0.06 ± 0.06 | 2.17 ± 0.35 | 0.18 ± 0.17 |
| -3 | 0.88 ± 0.13 | 0.14 ± 0.07 | 2.48 ± 0.37 | 0.39 ± 0.21 |
| -2 | 1.64 ± 0.21 | 0.17 ± 0.11 | 4.63 ± 0.58 | 0.48 ± 0.30 |
| -1 | 3.58 ± 0.43 | 0.31 ± 0.21 | 10.11 ± 1.23 | 0.88 ± 0.60 |
| 0 | | | | |
| 1 | 3.34 ± 0.39 | 0.00 ± 0.14 | 9.41 ± 1.09 | 0.00 ± 0.40 |
| 2 | 1.90 ± 0.24 | 0.18 ± 0.12 | 5.37 ± 0.66 | 0.52 ± 0.33 |
| 3 | 1.04 ± 0.14 | 0.11 ± 0.07 | 2.94 ± 0.39 | 0.32 ± 0.19 |
| 4 | 0.79 ± 0.10 | 0.02 ± 0.03 | 2.23 ± 0.29 | 0.06 ± 0.10 |
| | k_{Ar}^Q/Γ (10^{-18} cm^3) | k_{Cs}^Q/Γ (10^{-17} cm^3) | k_{Ar}^Q ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | k_{Cs}^Q ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
| | 25.97 ± 4.50 | 2.21 ± 2.28 | 73.23 ± 12.69 | 6.23 ± 6.43 |

Supplementary Material Table 27 – Rate coefficients ($k_p^{\Delta J}$) in units of the radiative rate Γ and in units of cm^3s^{-1} [obtained by multiplying the fitted parameters ($k_p^{\Delta J}/\Gamma$) by $\Gamma = 2.82 \times 10^7 \text{ s}^{-1}$] for rotationally inelastic collisions of NaCs $2(A)^1\Sigma^+(v = 14, J = 32)$ molecules with argon and cesium atoms ($p = Ar$ and Cs). In this fit, the value of k_{Cs}^Q/Γ was fixed at 0.

| ΔJ | $k_{Ar}^{\Delta J}/\Gamma$ (10^{-18} cm^3) | $k_{Cs}^{\Delta J}/\Gamma$ (10^{-17} cm^3) | $k_{Ar}^{\Delta J}$ ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | $k_{Cs}^{\Delta J}$ ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
|------------|---|---|---|---|
| -4 | 0.75 ± 0.11 | 0.02 ± 0.04 | 2.11 ± 0.32 | 0.06 ± 0.11 |
| -3 | 0.88 ± 0.11 | 0.06 ± 0.02 | 2.49 ± 0.31 | 0.18 ± 0.06 |
| -2 | 1.60 ± 0.18 | 0.07 ± 0.02 | 4.52 ± 0.50 | 0.20 ± 0.07 |
| -1 | 3.50 ± 0.37 | 0.10 ± 0.05 | 9.88 ± 1.05 | 0.27 ± 0.13 |
| 0 | | | | |
| 1 | 2.85 ± 0.29 | 0.00 ± 0.03 | 8.05 ± 0.83 | 0.00 ± 0.09 |
| 2 | 1.86 ± 0.20 | 0.07 ± 0.03 | 5.25 ± 0.57 | 0.19 ± 0.08 |
| 3 | 1.01 ± 0.12 | 0.05 ± 0.02 | 2.84 ± 0.34 | 0.14 ± 0.05 |
| 4 | 0.74 ± 0.09 | 0.00 ± 0.01 | 2.08 ± 0.25 | 0.00 ± 0.04 |
| | k_{Ar}^Q/Γ (10^{-18} cm^3) | k_{Cs}^Q/Γ (10^{-17} cm^3) | k_{Ar}^Q ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | k_{Cs}^Q ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
| | 24.83 ± 3.80 | 0.00 (fixed) | 70.01 ± 10.72 | 0.00 (fixed) |

Supplementary Material Table 28 – Rate coefficients ($k_p^{\Delta J}$) in units of the radiative rate Γ and in units of cm^3s^{-1} [obtained by multiplying the fitted parameters ($k_p^{\Delta J}/\Gamma$) by $\Gamma = 2.82 \times 10^7 \text{ s}^{-1}$] for rotationally inelastic collisions of NaCs $2(A)^1\Sigma^+(v = 14, J = 32)$ molecules with argon and cesium atoms ($p = Ar$ and Cs). In this fit, the value of k_{Cs}^Q/Γ was fixed at $1.0 \times 10^{-16} \text{ cm}^3$.

| ΔJ | $k_{Ar}^{\Delta J}/\Gamma$ (10^{-18} cm^3) | $k_{Cs}^{\Delta J}/\Gamma$ (10^{-17} cm^3) | $k_{Ar}^{\Delta J}$ ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | $k_{Cs}^{\Delta J}$ ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
|------------|---|---|---|---|
| -4 | 0.73 ± 0.13 | 0.21 ± 0.05 | 2.06 ± 0.36 | 0.59 ± 0.13 |
| -3 | 0.75 ± 0.13 | 0.39 ± 0.03 | 2.13 ± 0.36 | 1.11 ± 0.08 |
| -2 | 1.54 ± 0.21 | 0.52 ± 0.03 | 4.35 ± 0.58 | 1.47 ± 0.08 |
| -1 | 3.36 ± 0.43 | 1.07 ± 0.05 | 9.48 ± 1.23 | 3.00 ± 0.14 |
| 0 | | | | |
| 1 | 3.43 ± 0.42 | 0.39 ± 0.07 | 9.68 ± 1.18 | 1.11 ± 0.19 |
| 2 | 1.79 ± 0.24 | 0.58 ± 0.03 | 5.05 ± 0.67 | 1.63 ± 0.09 |
| 3 | 0.98 ± 0.14 | 0.33 ± 0.02 | 2.76 ± 0.40 | 0.94 ± 0.06 |
| 4 | 0.78 ± 0.11 | 0.12 ± 0.02 | 2.21 ± 0.32 | 0.34 ± 0.07 |
| | k_{Ar}^Q/Γ (10^{-18} cm^3) | k_{Cs}^Q/Γ (10^{-17} cm^3) | k_{Ar}^Q ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | k_{Cs}^Q ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
| | 24.19 ± 4.49 | 10.00 (fixed) | 68.22 ± 12.66 | 28.20 (fixed) |

Supplementary Material Table 29 – Rate coefficients ($k_p^{\Delta J}$) in units of the radiative rate Γ and in units of cm^3s^{-1} [obtained by multiplying the fitted parameters ($k_p^{\Delta J}/\Gamma$) by $\Gamma = 2.82 \times 10^7 \text{ s}^{-1}$] for rotationally inelastic collisions of NaCs $2(A)^1\Sigma^+(v = 14, J = 32)$ molecules with argon and cesium atoms ($p = Ar$ and Cs). In this fit, the value of k_{Cs}^Q/Γ was fixed at $3.0 \times 10^{-16} \text{ cm}^3$.

| ΔJ | $k_{Ar}^{\Delta J}/\Gamma$ (10^{-18} cm^3) | $k_{Cs}^{\Delta J}/\Gamma$ (10^{-17} cm^3) | $k_{Ar}^{\Delta J}$ ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | $k_{Cs}^{\Delta J}$ ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
|------------|---|---|---|---|
| -4 | 0.69 ± 0.15 | 0.58 ± 0.06 | 1.94 ± 0.43 | 1.64 ± 0.16 |
| -3 | 0.55 ± 0.16 | 0.99 ± 0.04 | 1.56 ± 0.44 | 2.80 ± 0.13 |
| -2 | 1.40 ± 0.25 | 1.39 ± 0.04 | 3.94 ± 0.71 | 3.92 ± 0.11 |
| -1 | 3.04 ± 0.53 | 2.93 ± 0.06 | 8.58 ± 1.49 | 8.26 ± 0.17 |
| 0 | | | | |
| 1 | 3.64 ± 0.54 | 1.39 ± 0.09 | 10.26 ± 1.53 | 3.92 ± 0.24 |
| 2 | 1.63 ± 0.29 | 1.56 ± 0.04 | 4.60 ± 0.81 | 4.40 ± 0.12 |
| 3 | 0.89 ± 0.17 | 0.90 ± 0.03 | 2.50 ± 0.48 | 2.53 ± 0.09 |
| 4 | 0.78 ± 0.14 | 0.37 ± 0.04 | 2.20 ± 0.40 | 1.05 ± 0.11 |
| | k_{Ar}^Q/Γ (10^{-18} cm^3) | k_{Cs}^Q/Γ (10^{-17} cm^3) | k_{Ar}^Q ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | k_{Cs}^Q ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
| | 22.02 ± 5.57 | 30.00 (fixed) | 62.10 ± 15.72 | 84.60 (fixed) |

Supplementary Material Table 30 – Rate coefficients ($k_p^{\Delta J}$) in units of the radiative rate Γ and in units of cm^3s^{-1} [obtained by multiplying the fitted parameters ($k_p^{\Delta J}/\Gamma$) by $\Gamma = 2.82 \times 10^7 \text{ s}^{-1}$] for rotationally inelastic collisions of $\text{NaCs } 2(A)^1\Sigma^+(v = 14, J = 32)$ molecules with argon and cesium atoms ($p = \text{Ar}$ and Cs). In this fit, the value of k_{Cs}^0/Γ was fixed at $5.0 \times 10^{-16} \text{ cm}^3$.

| ΔJ | $k_{\text{Ar}}^{\Delta J}/\Gamma$ (10^{-18} cm^3) | $k_{\text{Cs}}^{\Delta J}/\Gamma$ (10^{-17} cm^3) | $k_{\text{Ar}}^{\Delta J}$ ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | $k_{\text{Cs}}^{\Delta J}$ ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
|------------|--|--|--|--|
| -4 | 0.67 ± 0.18 | 0.95 ± 0.06 | 1.88 ± 0.51 | 2.68 ± 0.18 |
| -3 | 0.42 ± 0.18 | 1.57 ± 0.06 | 1.18 ± 0.52 | 4.44 ± 0.17 |
| -2 | 1.31 ± 0.30 | 2.25 ± 0.05 | 3.68 ± 0.85 | 6.33 ± 0.13 |
| -1 | 2.85 ± 0.63 | 4.75 ± 0.07 | 8.04 ± 1.77 | 13.39 ± 0.20 |
| 0 | | | | |
| 1 | 3.83 ± 0.67 | 2.38 ± 0.11 | 10.81 ± 1.90 | 6.71 ± 0.30 |
| 2 | 1.54 ± 0.34 | 2.53 ± 0.05 | 4.34 ± 0.97 | 7.13 ± 0.15 |
| 3 | 0.83 ± 0.20 | 1.46 ± 0.04 | 2.33 ± 0.58 | 4.12 ± 0.11 |
| 4 | 0.79 ± 0.17 | 0.63 ± 0.05 | 2.22 ± 0.49 | 1.77 ± 0.14 |
| | k_{Ar}^0/Γ (10^{-18} cm^3) | k_{Cs}^0/Γ (10^{-17} cm^3) | k_{Ar}^0 ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | k_{Cs}^0 ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
| | 20.93 ± 6.76 | 50.00 (fixed) | 59.01 ± 19.07 | 141.00 (fixed) |

Supplementary Material Table 31 – Rate coefficients ($k_p^{\Delta J}$) in units of the radiative rate Γ and in units of cm^3s^{-1} [obtained by multiplying the fitted parameters ($k_p^{\Delta J}/\Gamma$) by $\Gamma = 2.82 \times 10^7 \text{ s}^{-1}$] for rotationally inelastic collisions of NaCs $2(A)^1\Sigma^+(v = 14, J = 32)$ molecules with argon and cesium atoms ($p = Ar$ and Cs). In this fit, the value of k_{Cs}^Q/Γ was fixed at $7.0 \times 10^{-16} \text{ cm}^3$.

| ΔJ | $k_{Ar}^{\Delta J}/\Gamma$ (10^{-18} cm^3) | $k_{Cs}^{\Delta J}/\Gamma$ (10^{-17} cm^3) | $k_{Ar}^{\Delta J}$ ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | $k_{Cs}^{\Delta J}$ ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
|------------|---|---|---|---|
| -4 | 0.67 ± 0.21 | 1.32 ± 0.07 | 1.88 ± 0.59 | 3.73 ± 0.21 |
| -3 | 0.30 ± 0.21 | 2.15 ± 0.08 | 0.84 ± 0.61 | 6.07 ± 0.22 |
| -2 | 1.27 ± 0.35 | 3.09 ± 0.06 | 3.58 ± 0.99 | 8.73 ± 0.16 |
| -1 | 2.77 ± 0.74 | 6.54 ± 0.08 | 7.81 ± 2.08 | 18.44 ± 0.23 |
| 0 | | | | |
| 1 | 4.09 ± 0.81 | 3.37 ± 0.13 | 11.53 ± 2.29 | 9.49 ± 0.36 |
| 2 | 1.50 ± 0.41 | 3.48 ± 0.06 | 4.24 ± 1.14 | 9.83 ± 0.18 |
| 3 | 0.80 ± 0.24 | 2.03 ± 0.05 | 2.27 ± 0.68 | 5.71 ± 0.14 |
| 4 | 0.82 ± 0.20 | 0.88 ± 0.07 | 2.31 ± 0.58 | 2.49 ± 0.18 |
| | k_{Ar}^Q/Γ (10^{-18} cm^3) | k_{Cs}^Q/Γ (10^{-17} cm^3) | k_{Ar}^Q ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | k_{Cs}^Q ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
| | 20.93 ± 8.09 | 70.00 (fixed) | 59.01 ± 22.83 | 197.40 (fixed) |

Supplementary Material Table 32 – Rate coefficients ($k_p^{\Delta J}$) in units of the radiative rate Γ and in units of cm^3s^{-1} [obtained by multiplying the fitted parameters ($k_p^{\Delta J}/\Gamma$) by $\Gamma = 2.82 \times 10^7 \text{ s}^{-1}$] for rotationally inelastic collisions of NaCs $2(A)^1\Sigma^+(v = 14, J = 32)$ molecules with argon and cesium atoms ($p = Ar$ and Cs). In this fit, the value of k_{Cs}^0/Γ was fixed at $10.0 \times 10^{-16} \text{ cm}^3$.

| ΔJ | $k_{Ar}^{\Delta J}/\Gamma$ (10^{-18} cm^3) | $k_{Cs}^{\Delta J}/\Gamma$ (10^{-17} cm^3) | $k_{Ar}^{\Delta J}$ ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | $k_{Cs}^{\Delta J}$ ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
|------------|---|---|---|---|
| -4 | 0.71 ± 0.26 | 1.87 ± 0.09 | 2.00 ± 0.74 | 5.28 ± 0.26 |
| -3 | 0.10 ± 0.27 | 3.04 ± 0.11 | 0.29 ± 0.78 | 8.58 ± 0.30 |
| -2 | 1.30 ± 0.44 | 4.36 ± 0.07 | 3.66 ± 1.25 | 12.29 ± 0.19 |
| -1 | 2.83 ± 0.93 | 9.20 ± 0.10 | 7.97 ± 2.61 | 25.94 ± 0.27 |
| 0 | | | | |
| 1 | 4.62 ± 1.05 | 4.84 ± 0.16 | 13.04 ± 2.95 | 13.64 ± 0.46 |
| 2 | 1.55 ± 0.51 | 4.91 ± 0.08 | 4.37 ± 1.45 | 13.85 ± 0.22 |
| 3 | 0.83 ± 0.30 | 2.87 ± 0.06 | 2.34 ± 0.86 | 8.10 ± 0.18 |
| 4 | 0.91 ± 0.26 | 1.26 ± 0.09 | 2.56 ± 0.73 | 3.55 ± 0.24 |
| | k_{Ar}^0/Γ (10^{-18} cm^3) | k_{Cs}^0/Γ (10^{-17} cm^3) | k_{Ar}^0 ($10^{-11} \text{ cm}^3\text{s}^{-1}$) | k_{Cs}^0 ($10^{-10} \text{ cm}^3\text{s}^{-1}$) |
| | 22.94 ± 10.44 | 100.00 (fixed) | 64.68 ± 29.44 | 282.00 (fixed) |