Homework (back by February 11th, 3 pm EST, to <u>ufother@clemson.edu</u> as well as to local instructor)

1. Consider the series of a Kelvin-Voigt model and a spring as 1st realistic representation of bulk viscoelasticity. Derive the following formula which holds for constant strain:

$$\sigma(t) = \frac{3 \cdot K_1 \cdot K_2}{K_1 + K_2} \cdot \varepsilon_0 + \frac{3 \cdot K_2 \cdot K_2}{K_1 + K_2} \cdot \varepsilon_0 \cdot e^{-t \cdot 3 \cdot (K_1 + K_2) / \eta_v}$$

(Start with the following consideration: both for the Kelvin-Voigt-model and the single spring, the stress is $\sigma(t)$. The strains are $\varepsilon_1(t)$ and $\varepsilon_2(t)$ which are also time-dependent. However, $\varepsilon_1(t) + \varepsilon_2(t) = \varepsilon_0$ at all times. If one replaces $\varepsilon_1(t) + \varepsilon_2(t)$ with expressions depending on $\sigma(t)$, one will arrive at a differential equation for $\sigma(t)$. Solving this equation will lead to the above formula.)

2. (follows on February 9th, 2010)