

# ME 343 – Control Systems

Lecture 20  
October 9, 2009

## Root Locus – Phase lead compensator

$$D(s) = \frac{s + z}{s + p}, \quad p > z \quad \text{Phase lead COMPENSATOR}$$

Selecting  $z$  and  $p$  is a trial and error procedure. In general:

- The zero is placed in the neighborhood of the closed-loop natural frequency, as determined by rise-time or settling time requirements.
- The pole is placed at a distance 5 to 20 times the value of the zero location. The pole is fast enough to avoid modifying the dominant pole behavior.

The exact position of the pole  $p$  is a compromise between:

- Noise suppression (we want a small value for  $p$ )
- Compensation effectiveness (we want large value for  $p$ )

## Root Locus – Phase lead compensator

Example: FPE 5.28

## Root Locus – Phase lag compensator

$$D(s) = \frac{s + z}{s + p}, \quad p < z \quad \text{Phase lag COMPENSATOR}$$

Selecting  $z$  and  $p$  is a trial and error procedure. In general:

- The ratio zero/pole is chosen based on the error constant specification.
- We pick  $z$  and  $p$  small to avoid affecting the dominant dynamic of the system (to avoid modifying the part of the locus representing the dominant dynamics)
- Slow transient due to the small  $p$  is almost cancelled by a small  $z$ . The ratio zero/pole cannot be very big.

The exact position of  $z$  and  $p$  is a compromise between:

- Steady state error (we want a large value for  $z/p$ )
- The transient response (we want the pole  $p$  placed far from the origin)

## Root Locus – Phase lag compensator

Example: FPE 5.27