

ME242 – MECHANICAL ENGINEERING SYSTEMS

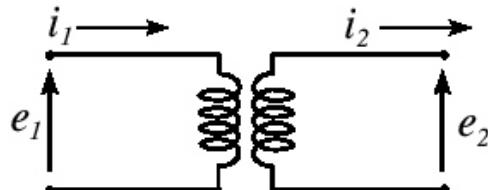
LECTURE 29:

- Systems with Ideal Machines

4.2

ELECTRICAL CIRCUITS

Electrical Transformer



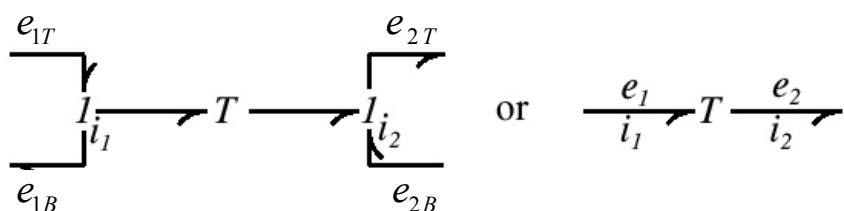
$$e_1 = Te_2$$

$$i_2 = Ti_1$$

$$e_1 = e_{1T} - e_{1B}$$

$$e_2 = e_{2T} - e_{2B}$$

usually : $e_{1B} = e_{2B} = 0$



ELECTRICAL CIRCUITS - TRANSFORMER

SYSTEM

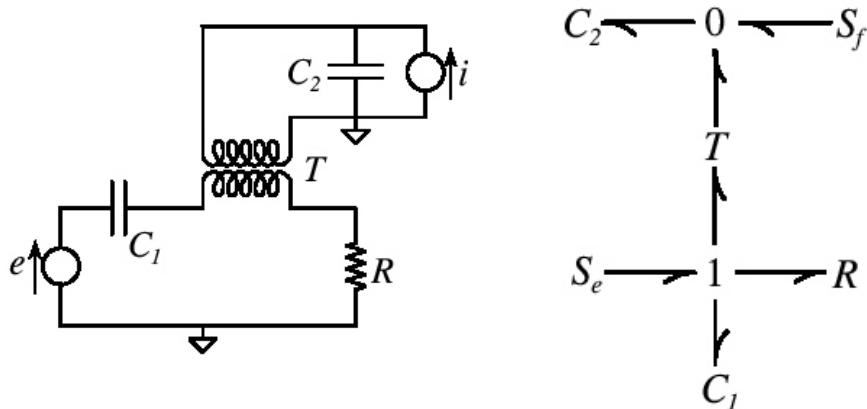
modulus equals ratio of coil turns
does not transmit DC
poor performance at high frequencies

MODEL

modulus equals ratio of coil turns
does transmit DC
good performance at high frequencies

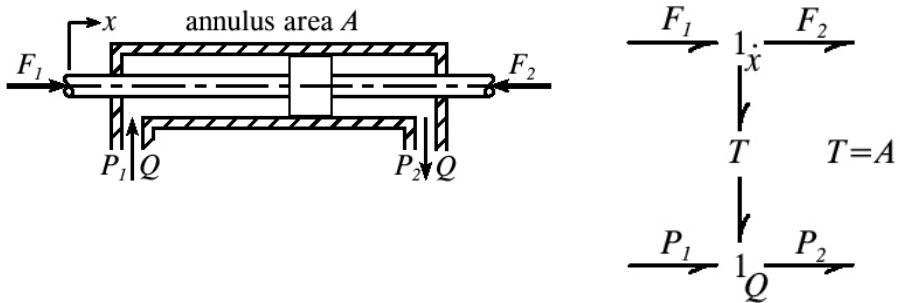
ELECTRICAL CIRCUITS

Example:



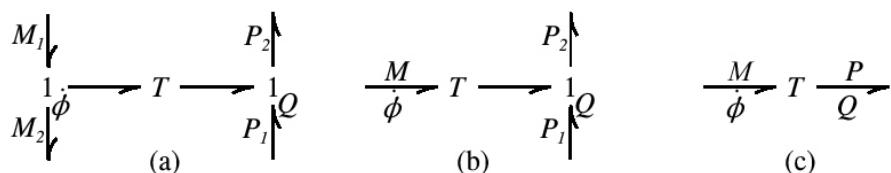
FLUID/MECHANICAL SYSTEMS

Positive Displacement Machine: Double-Rod-End Cylinder



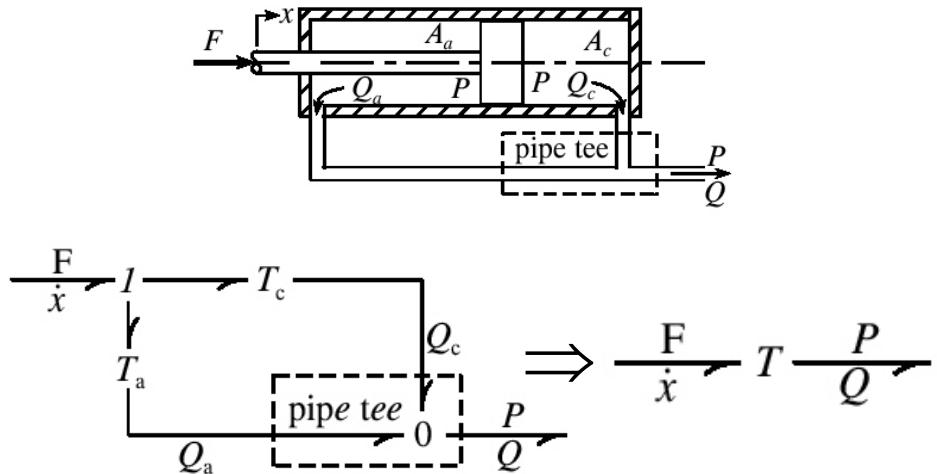
FLUID/MECHANICAL SYSTEMS

Positive Displacement Machine: Rotary Hydraulic Pump



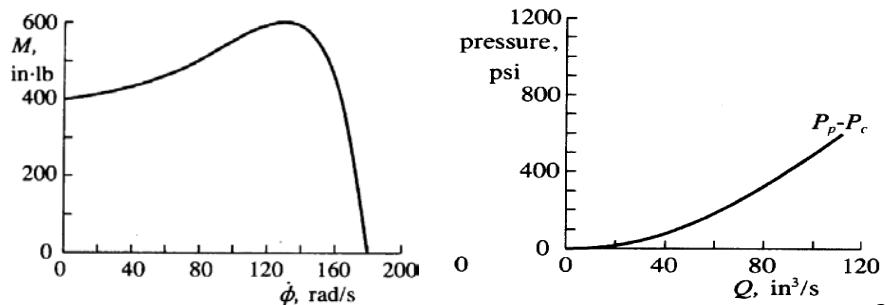
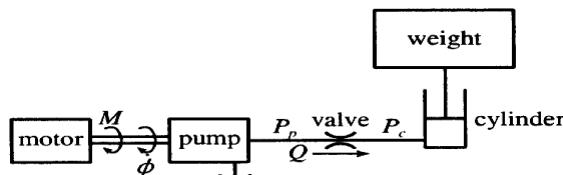
FLUID/MECHANICAL CIRCUITS

Example:



FLUID/MECHANICAL CIRCUITS

4.10 A motor drives a pump to supply a hydraulic cylinder that lifts a 3000-lb weight. The torque-speed characteristic of the motor is plotted on the next page. The displacement of the pump is $0.50 \text{ in}^3/\text{rad}$, and the area of the cylinder is 5.0 in^2 . The flow passes through a valve with the characteristic also plotted.



FLUID/MECHANICAL CIRCUITS

(a) Model the system with a bond graph, neglecting inertia, friction and leakage.

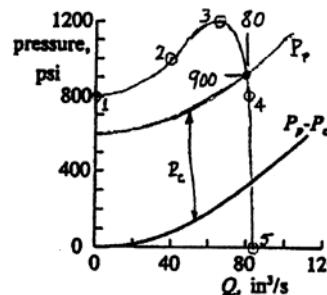
$$\begin{array}{c}
 S \xrightarrow[\dot{\phi}]{M} T_p \xrightarrow{P_p} \left\{ \begin{array}{l} Q \\ R \end{array} \right\} \xrightarrow{P_c} T_c \xrightarrow[\dot{y}]{W=3000 \text{ lb}} S_c
 \end{array}$$

$$T_p = \frac{Q}{\dot{\phi}} = 0.50 \frac{\text{in}^3}{\text{rad}}$$

$$T_c = \frac{\dot{y}}{Q} = \frac{1}{5} = 0.2 \text{ in}^{-2}$$

(b) Determine the pressure P_c in the cylinder, and add it to the plotted pressure $P_p - P_c$ to get an effective load characteristic as seen by the pump.

$$\begin{aligned}
 P_c &= \frac{W}{T_c} \\
 &= 600 \frac{\text{lb}}{\text{in}^2}
 \end{aligned}$$



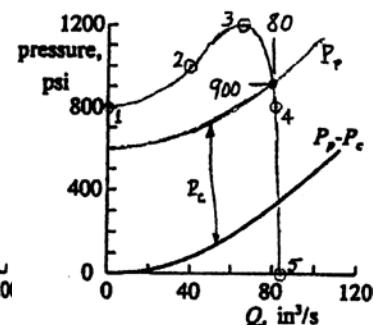
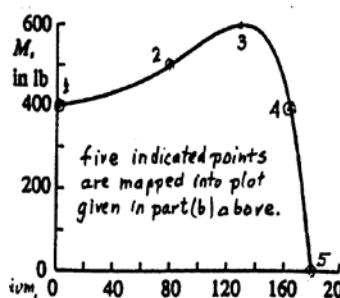
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FLUID/MECHANICAL CIRCUITS

(c) Transform the given torque-speed motor characteristic to plot an equivalent pressure-flow source characteristic at the outlet of the pump on the same axes as the plot of part (b).

$$\begin{aligned}
 P_p &= \frac{1}{T_p} M = 2M \\
 Q &= T_p \dot{\phi} = 0.5 \dot{\phi}
 \end{aligned}$$



(d) Determine the equilibrium pressure P_p and flow Q , the speed at which the weight rises and the torque and angular velocity of the motor.

At equilibrium, $P_p = 900 \text{ psi}$; $Q = 80 \text{ in}^3/\text{s}$

$$\dot{y} = T_c Q = 16 \text{ in/s}; M = T_p P_p = 450 \text{ in lb}; \dot{\phi} = \frac{Q}{T_p} = 160 \text{ rad/s}$$

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