

ME242 – MECHANICAL ENGINEERING SYSTEMS

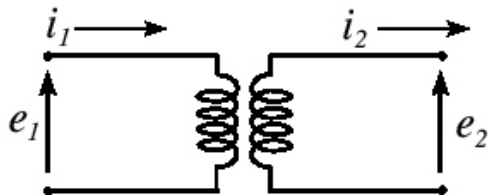
LECTURE 29:

- Systems with Ideal Machines

4.2

ELECTRICAL CIRCUITS

Electrical Transformer

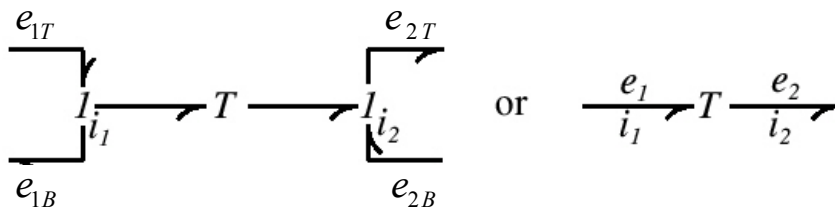


$$e_1 = T e_2$$

$$i_2 = T i_1$$

$$\begin{aligned} e_1 &= e_{1T} - e_{1B} \\ e_2 &= e_{2T} - e_{2B} \end{aligned}$$

usually : $e_{1B} = e_{2B} = 0$



ELECTRICAL CIRCUITS - TRANSFORMER

SYSTEM

modulus equals ratio of coil turns

does not transmit DC

poor performance at high frequencies

MODEL

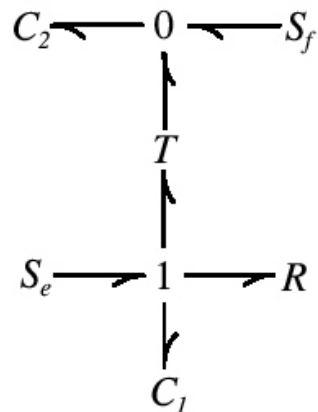
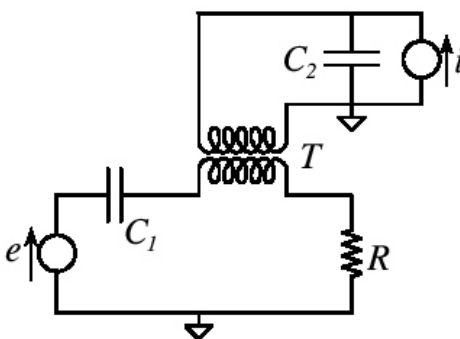
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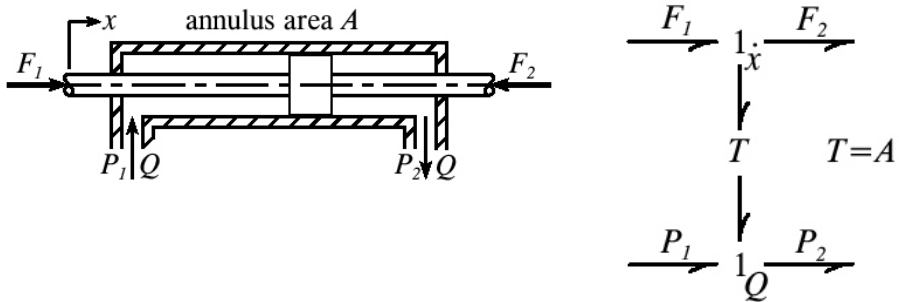
ELECTRICAL CIRCUITS

Example:



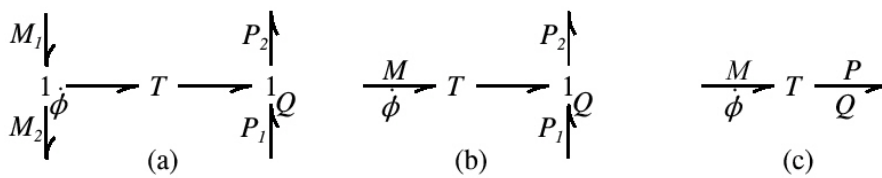
FLUID/MECHANICAL SYSTEMS

Positive Displacement Machine: Double-Rod-End Cylinder



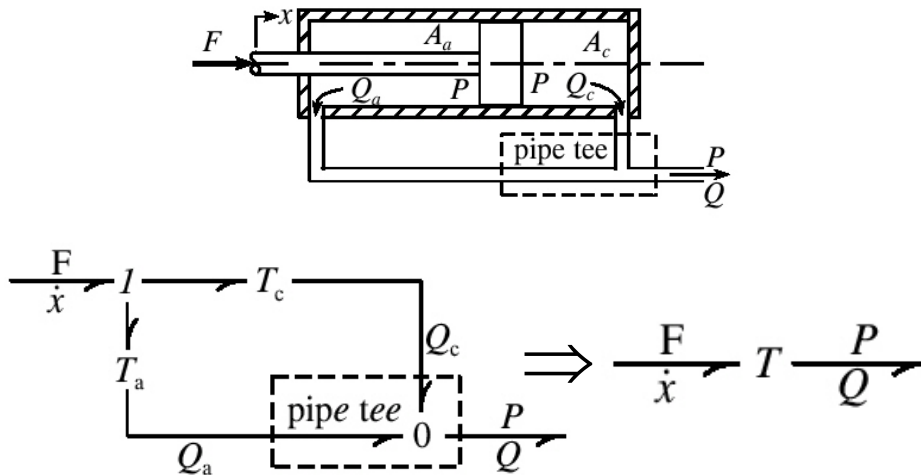
FLUID/MECHANICAL SYSTEMS

Positive Displacement Machine: Rotary Hydraulic Pump



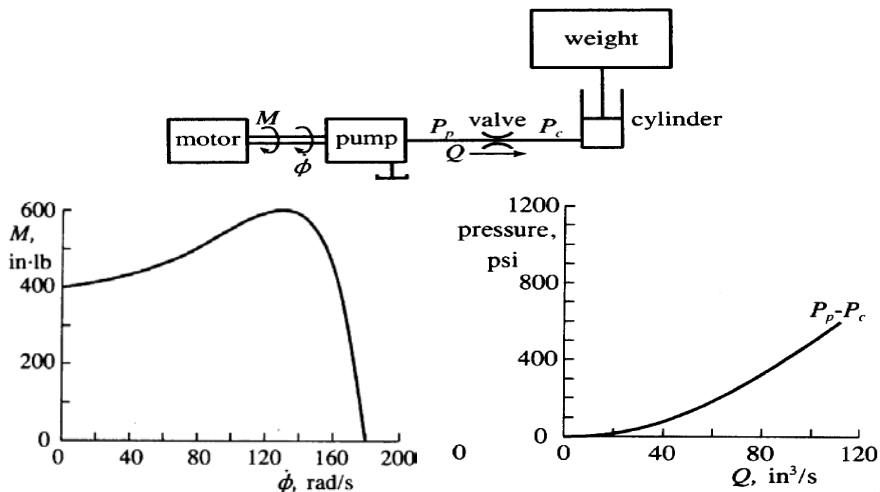
FLUID/MECHANICAL CIRCUITS

Example:



FLUID/MECHANICAL CIRCUITS

4.10 A motor drives a pump to supply a hydraulic cylinder that lifts a 3000-lb weight. The torque-speed characteristic of the motor is plotted on the next page. The displacement of the pump is $0.50 \text{ in}^3/\text{rad}$, and the area of the cylinder is 5.0 in^2 . The flow passes through a valve with the characteristic also plotted.



FLUID/MECHANICAL CIRCUITS

(a) Model the system with a bond graph, neglecting inertia, friction and leakage.

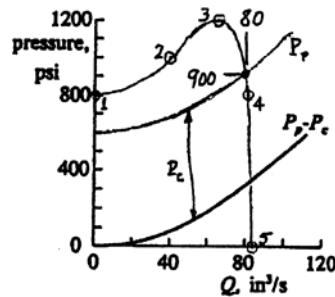
$$S \xrightarrow[\dot{\phi}]{M} T_p \xrightarrow[P_p]{P_p} \downarrow Q \xrightarrow[P_c]{P_c} T_c \xrightarrow[\dot{y}]{W=3000\text{ lb}} S_e$$

$$T_p = \frac{Q}{\dot{\phi}} = 0.50 \frac{\text{in}^3}{\text{rad}} \quad T_c = \frac{\dot{y}}{Q} = \frac{1}{5} = 0.2 \text{ in}^{-2}$$

(b) Determine the pressure P_c in the cylinder, and add it to the plotted pressure $P_p - P_c$ to get an effective load characteristic as seen by the pump.

$$P_c = \frac{W}{T_c}$$

$$= 600 \frac{\text{lb}}{\text{in}^2}$$

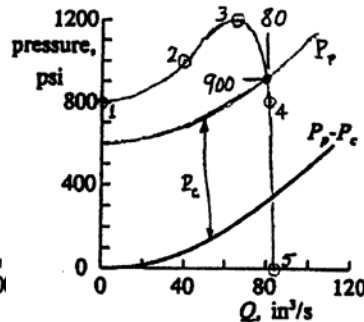
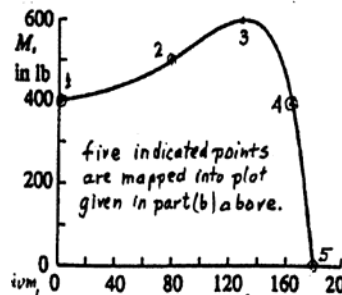


FLUID/MECHANICAL CIRCUITS

(c) Transform the given torque-speed motor characteristic to plot an equivalent pressure-flow source characteristic at the outlet of the pump on the same axes as the plot of part (b).

$$P_p = \frac{1}{T_p} M = 2M$$

$$Q = T_p \dot{\phi} = 0.5 \dot{\phi}$$



(d) Determine the equilibrium pressure P_p and flow Q , the speed at which the weight rises and the torque and angular velocity of the motor.

At equilibrium, $P_p = 900 \text{ psi}$; $Q = 80 \text{ in}^3/\text{s}$

$$\dot{y} = T_c Q = 16 \text{ in/s}; M = T_p P_p = 450 \text{ in lb}; \dot{\phi} = \frac{Q}{T_p} = 160 \text{ rad/s}$$