

***US-China Winter School  
New Functionalities in Glass***

***Why Does Glass Break?***

***Some considerations of the mechanical  
properties of glass***

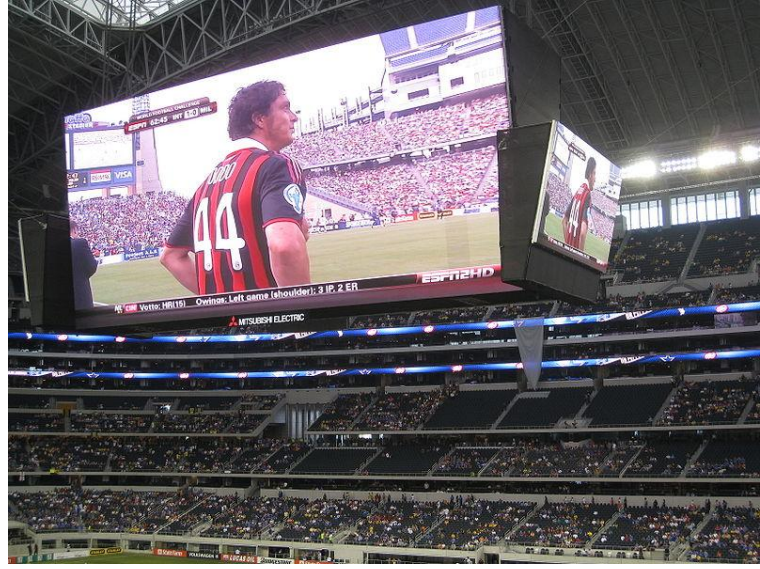
Richard K. Brow

Missouri University of Science & Technology

Department of Materials Science & Engineering

If glass was 100X stronger, what  
\*new\* applications would result?

# New applications will benefit from stronger glass.....



# Apple Store, 5<sup>th</sup> Ave., NYC



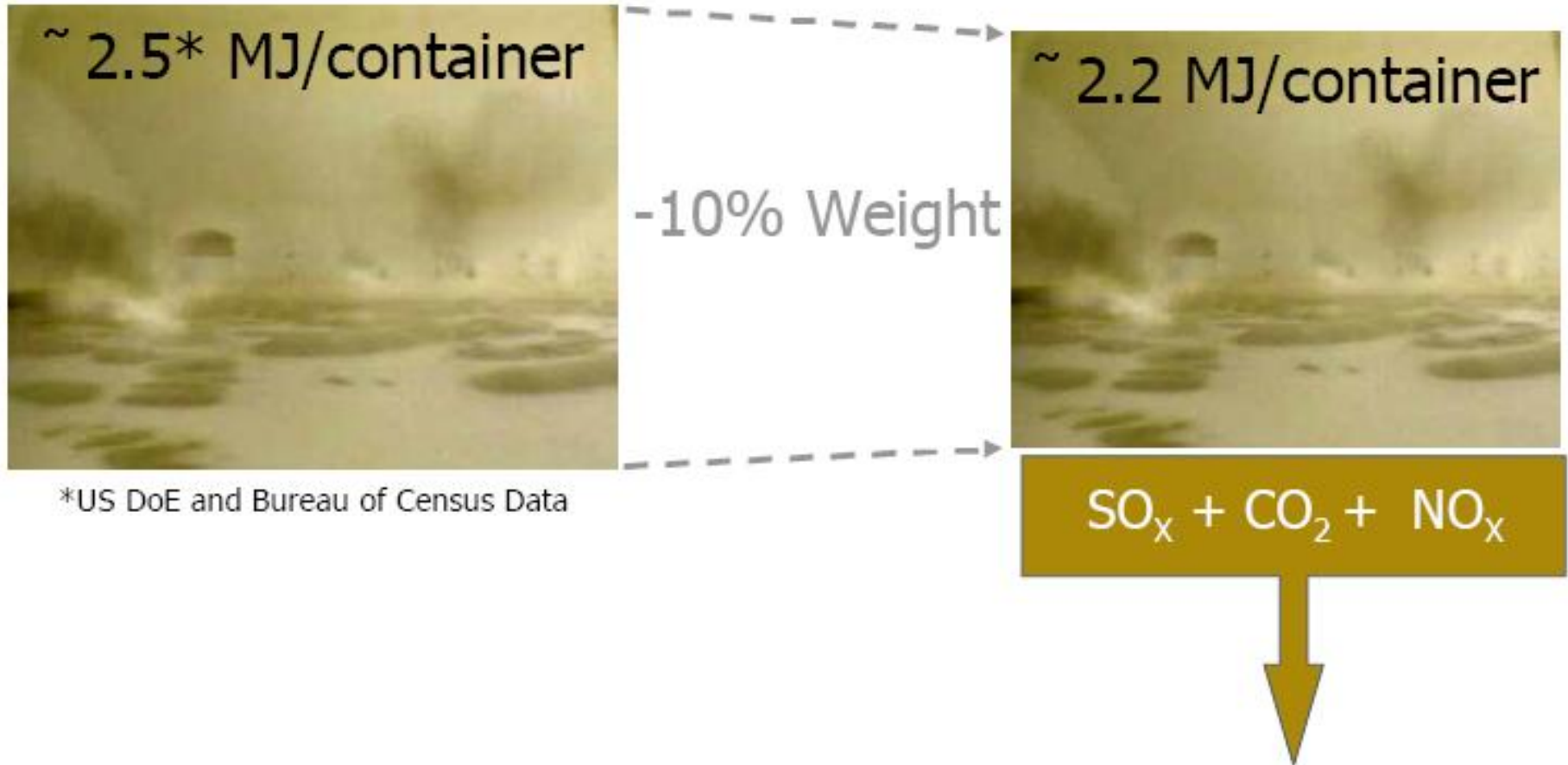
# Glasgow, Scotland





Train Station/Strasbourg, France

# Higher Strength $\Rightarrow$ Less Weight



\*US DoE and Bureau of Census Data

Emilio Spinosa, O-I, Vancouver, June 2009

# Strong glass comes in handy for other applications



# Our Outline

## 1. Background Information

- Elastic modulus
- Fracture mechanics and strength
- Fatigue
- Strengthening

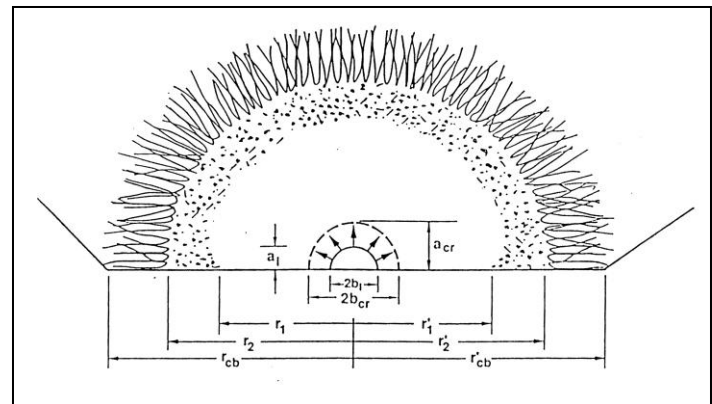
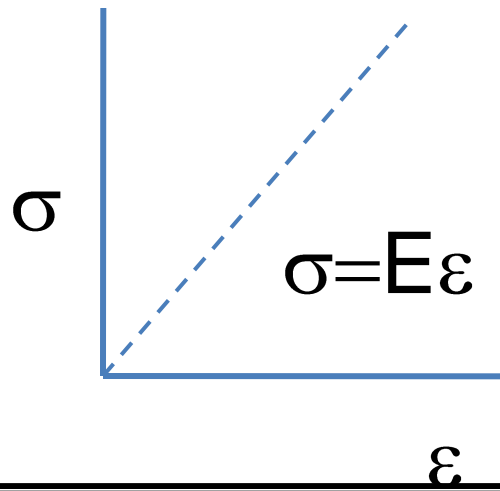
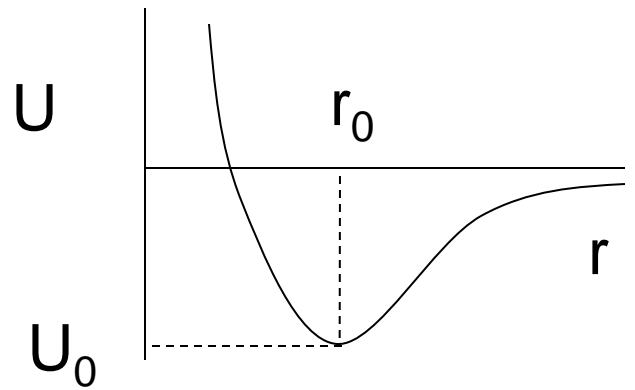
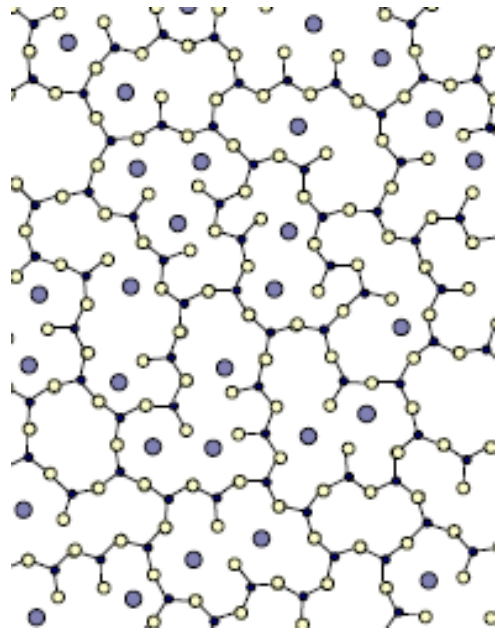
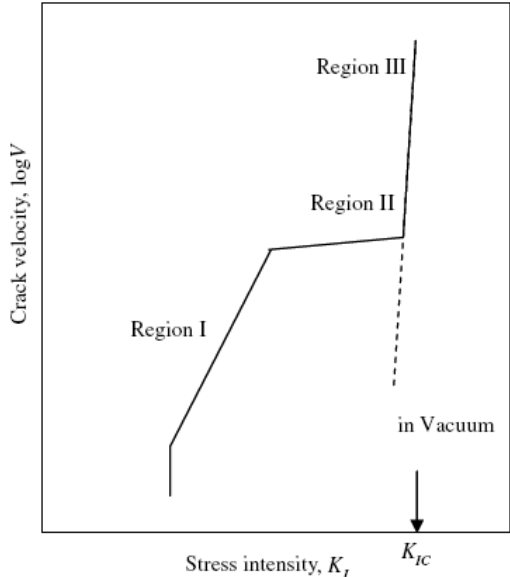
## 2. Two-point bend studies of pristine glass



## ***Some useful references:***

- A. Varshneya, “Fundamentals of Inorganic Glasses”, Society of Glass Technology (2006)- chap. 18
- “Elastic Properties and Short-to Medium-Range Order in Glasses”, Tanguy Rouxel, *J. Am. Ceram. Soc.*, **90** [10] 3019–3039 (2007)
- “Environmentally Enhanced Fracture of Glass: A Historical Perspective,” S. W. Frieman, S.M. Weiderhorn, and J.J. Mecholsky, *J. Am. Ceram. Soc.* **92**[7] 1371-1382 (2009)
- M. Ciccotti, “Stress-corrosion mechanisms in silicate glasses,” *J. Phys. D: Appl. Phys.* **42**, 214006 (2009).
- C. R. Kurkjian, P. K. Gupta, R. K. Brow, and N. Lower,” The intrinsic strength and fatigue of oxide glasses’, *J. Noncryst. Solids*, 316, 114 (2003).

# Can we connect mechanical performance to the molecular structure of glass?

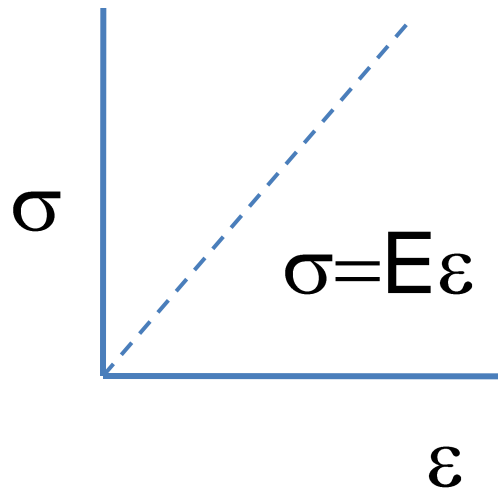
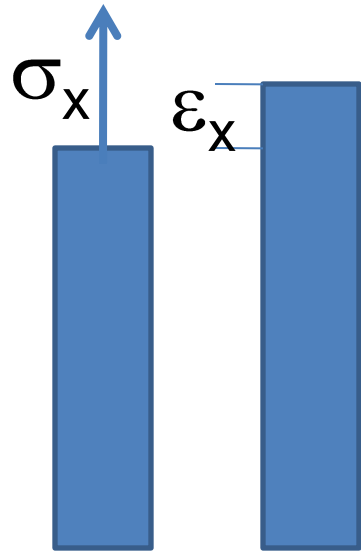


# Elastic Modulus

Definitions?

Why should we care about modulus?

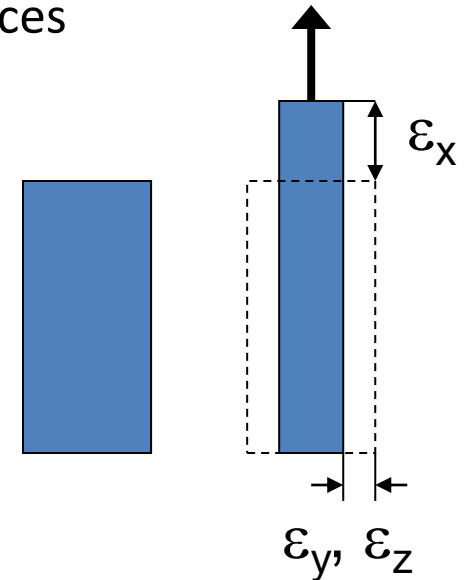
# Elastic Modulus- resistance to deflection



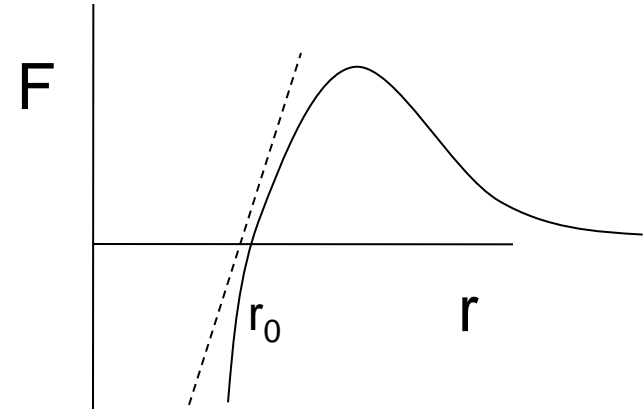
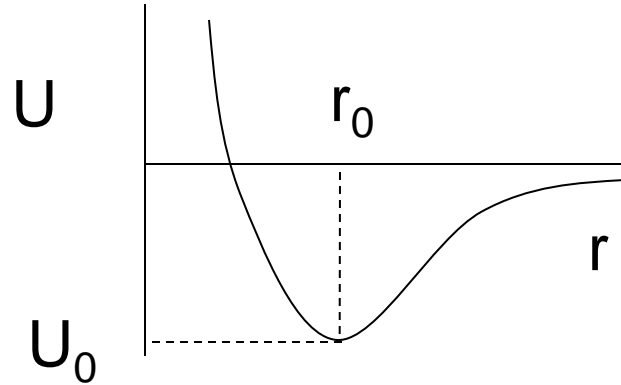
## Why is the elastic modulus of a glass important?

- Stiffer hard-drive disks (minimize deflection at high rpm's)
- Stiffer glass-fiber reinforces composites (larger wind-turbine blades)
- Reduce the thickness (and weight) of architectural glass)
- Increase the stiffness of glass-bearing structures (buildings, bio-glass scaffolds, etc.)
- Design glass or glass-ceramic matrices for aerospace applications

## Poisson's Ratio



# Elastic Modulus Is Related To The Strength of Nearest Neighbor Bonds



$$\text{Force} = F = - dU/dr$$

$$\text{Stiffness} = S_0 = \left( \frac{d^2U}{dr^2} \right)_{r=r_0}$$

$$\text{Elastic Modulus} = E = S / r_0$$

Elastic Modulus: Pascals =  $J/m^3$   
 a measure of the volume density  
 of strain energy ( $E \approx U_0/V_0$ )

Bulk Modulus:

$$K = V_0 \left. \frac{\partial^2 U}{\partial V^2} \right|_{V_0} = \frac{mn}{9V_0} U_0$$

From atomistic to continuum properties:

$$K = V_0 \left. \frac{\partial^2 U}{\partial V^2} \right|_{V_0} = \frac{mn}{9V_0} U_0$$

Multi-component glasses:

$$\left\langle \frac{U_0}{V_0} \right\rangle = \sum f_i \Delta H_{ai} / \left[ \sum f_i M_i / \rho_i \right]$$

$$\Delta H_{ai} = x \Delta H_f^0(A) + y \Delta H_f^0(B) - \Delta H_f^0(A_x B_y)$$

$\rho_i$ : density

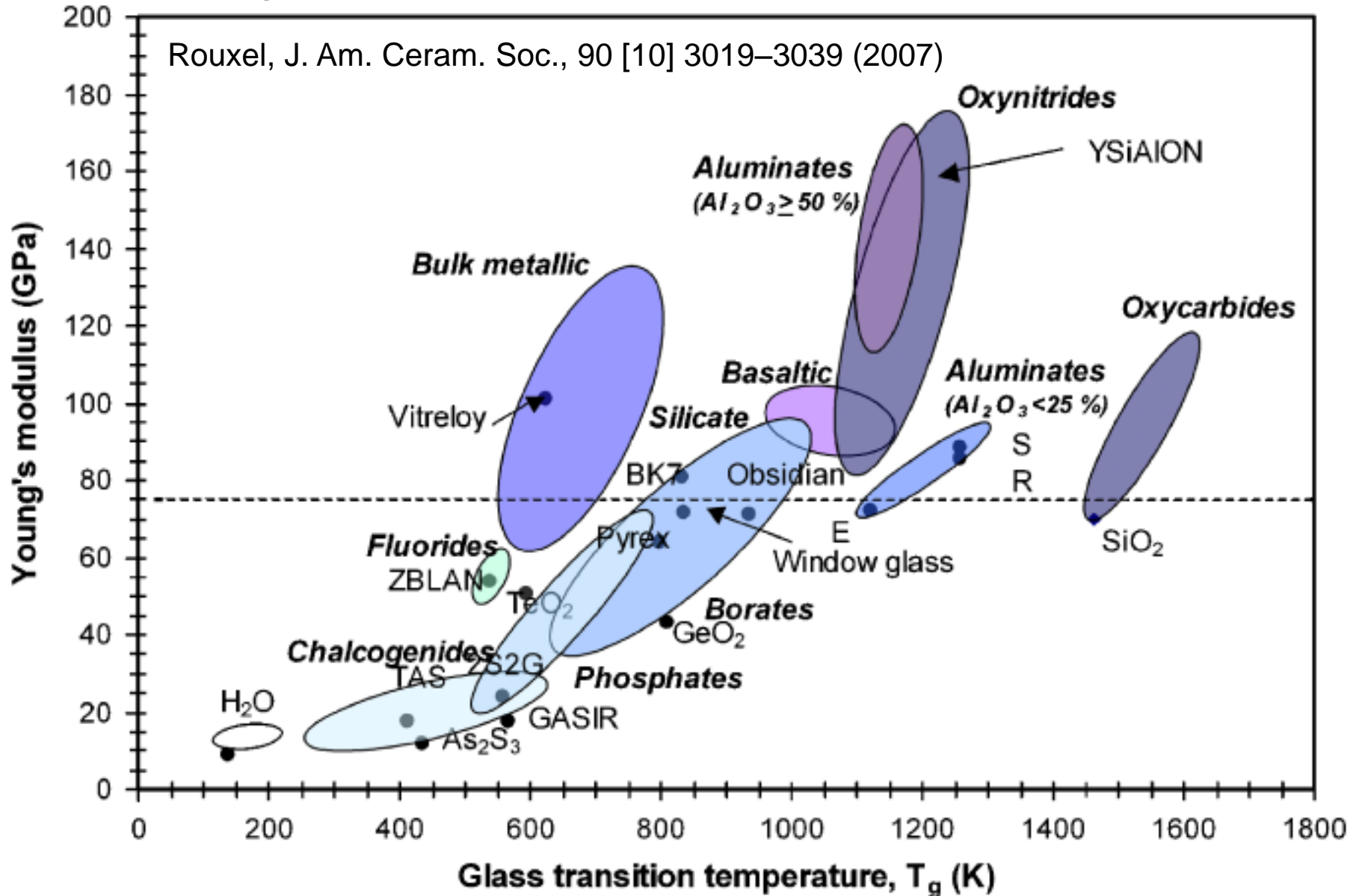
$f_i$ : molar fraction of  $i^{\text{th}}$  component

$M_i$ : molar mass of  $i^{\text{th}}$  component

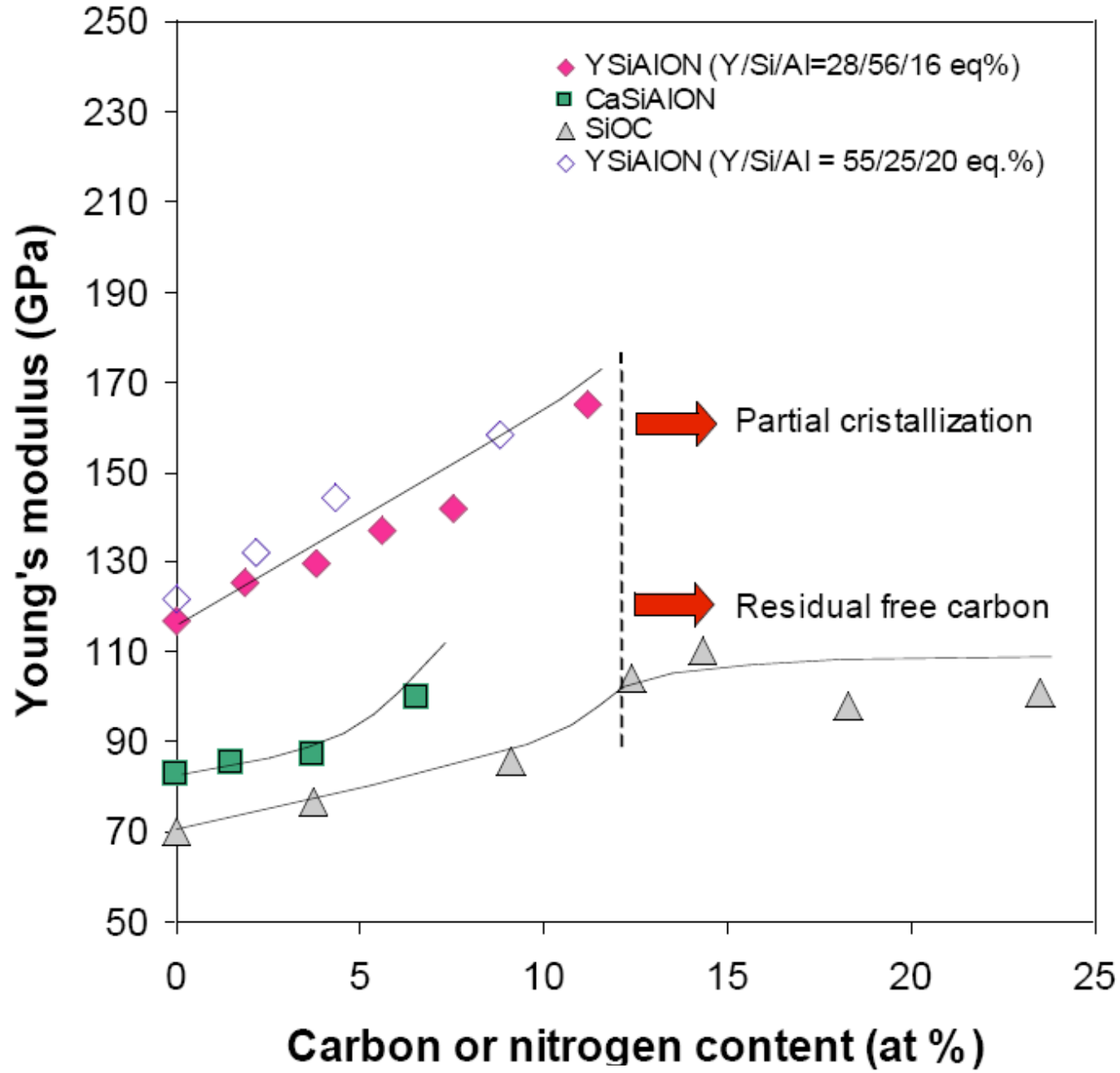
$\Delta H_{ai}$ : enthalpy of  $i^{\text{th}}$  component (Born-Haber cycle)

# E and $T_g$ are related within a composition class

Rouxel, J. Am. Ceram. Soc., 90 [10] 3019–3039 (2007)



More cross-links:  
greater E

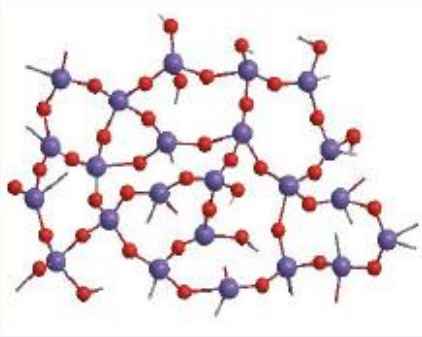


Rouxel, J. Am. Ceram. Soc., 90 [10] 3019–3039 (2007)



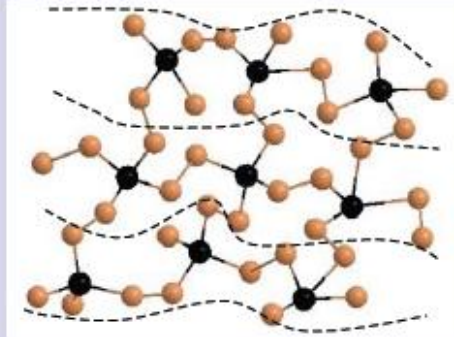
# Poisson's ratio appears to be sensitive to structure: packing density and 'network dimensionality'

a-SiO<sub>2</sub>



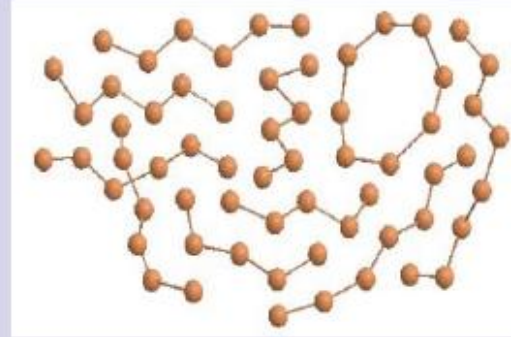
$\nu \approx 0.16$   
3D

GeSe<sub>4</sub>



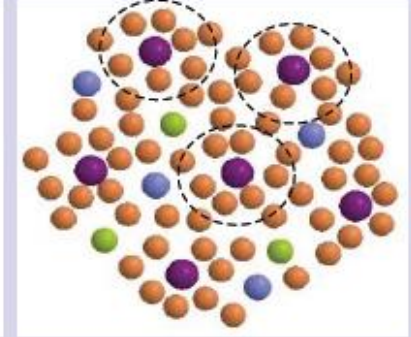
$\nu \approx 0.286$   
2D

a-Se

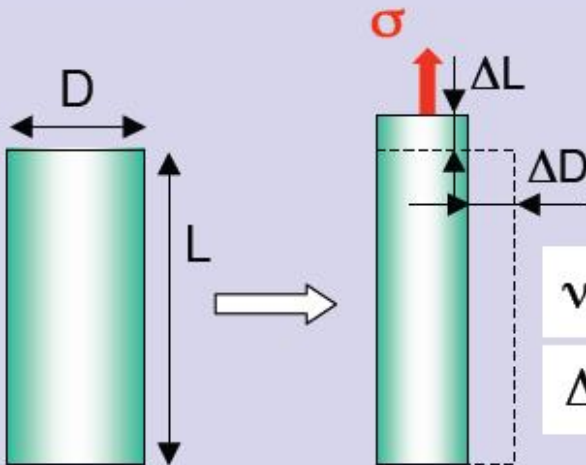


$\nu \approx 0.323$   
1D

Zr<sub>55</sub>Cu<sub>30</sub>Al<sub>10</sub>Ni<sub>5</sub>

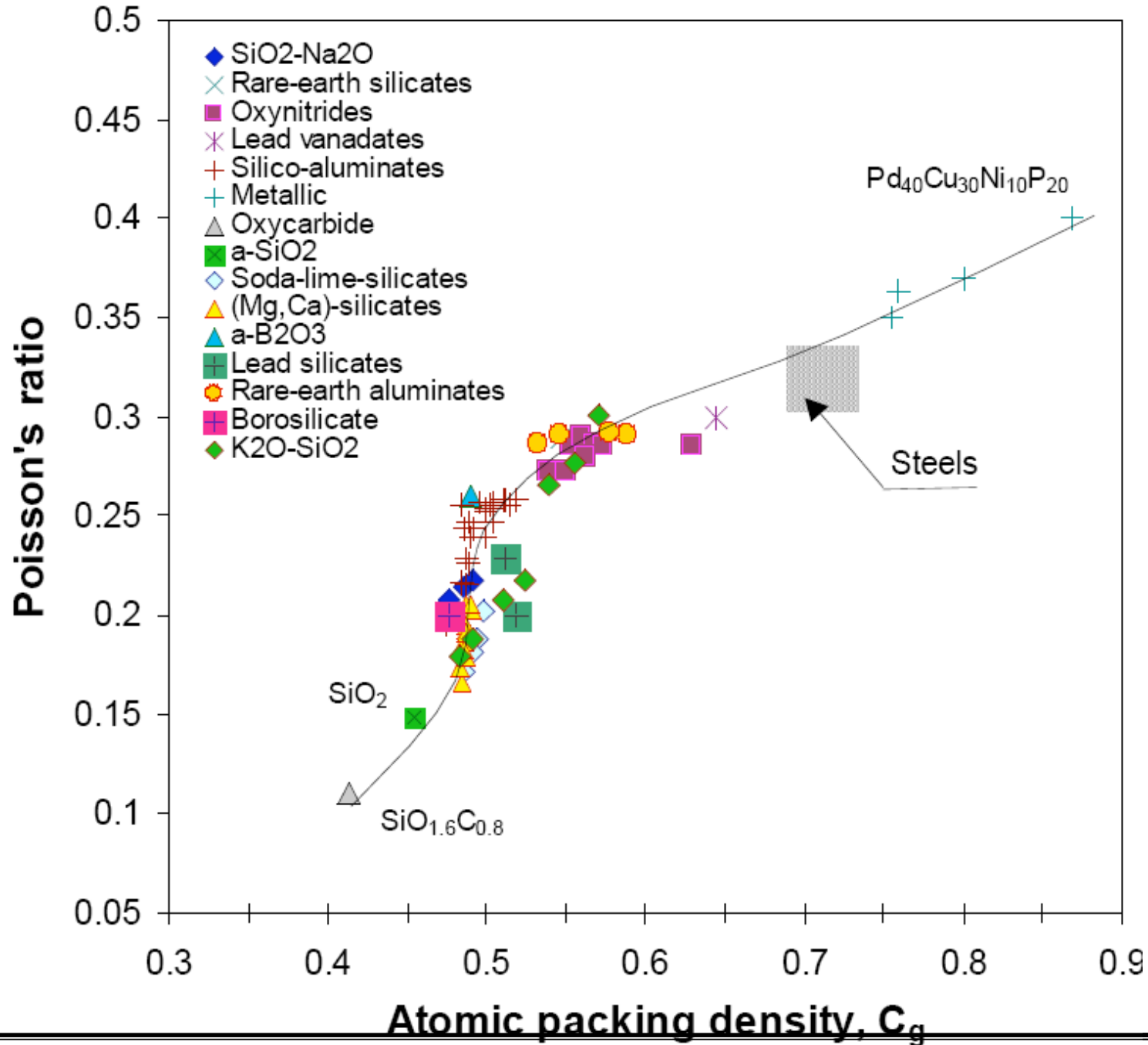


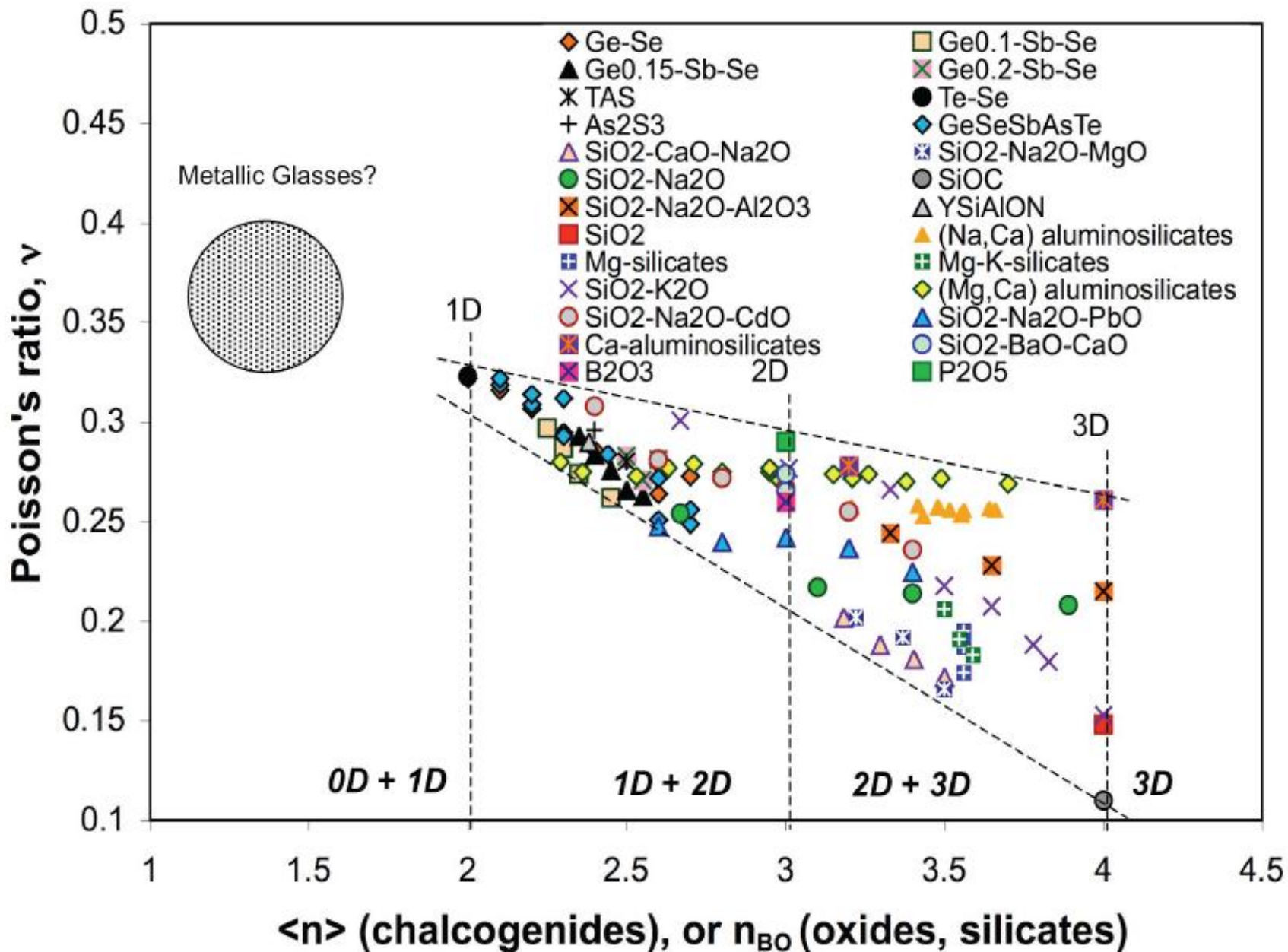
$\nu \approx 0.37$   
0D?



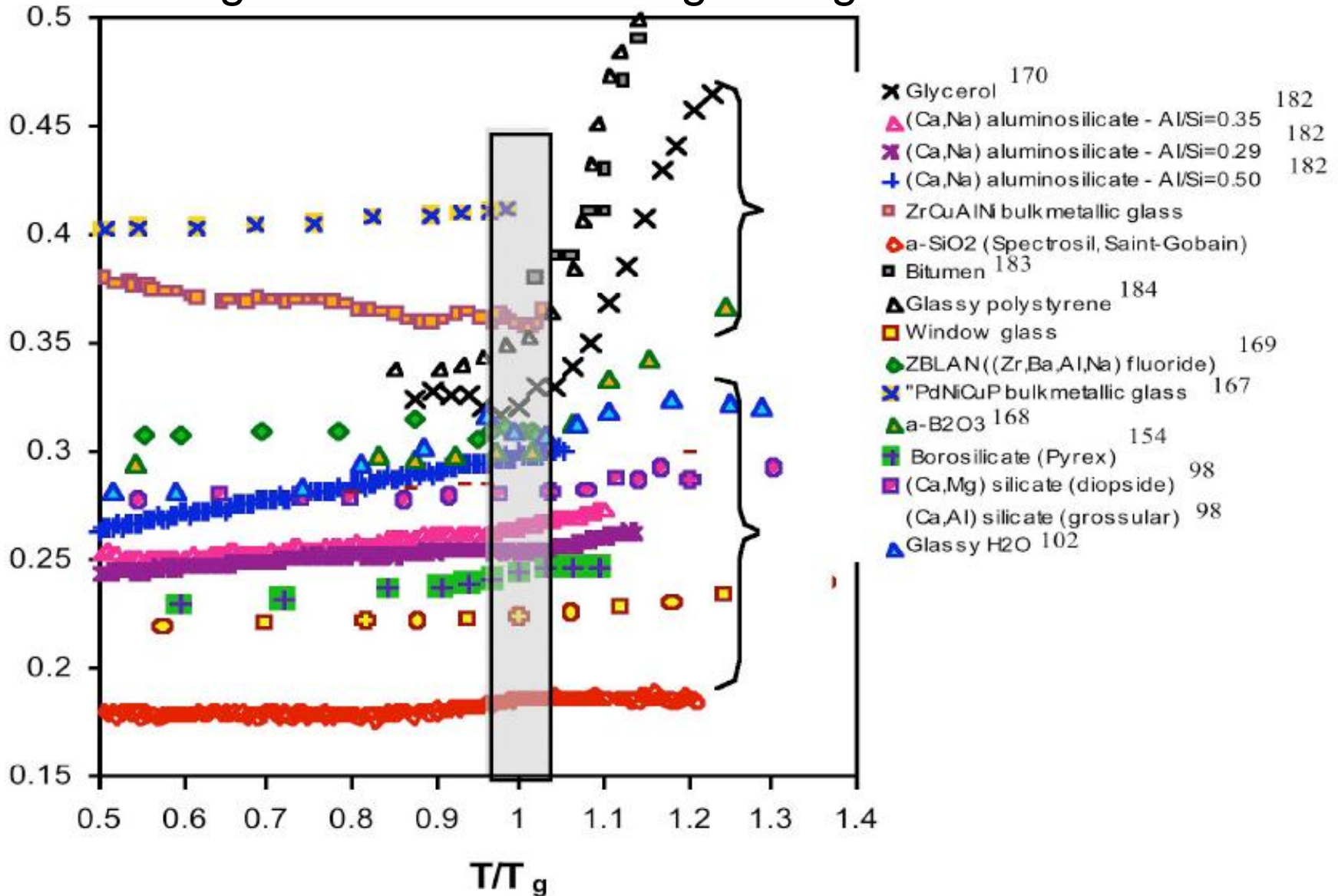
$$\nu = -\epsilon_t / \epsilon_l = -L / D \times \Delta D / \Delta L$$

$$\Delta V / V = \text{Trace } \epsilon = (1 - 2\nu) \sigma / E$$





The temperature-dependence of the Poisson's ratio may indicate changes in structure through the glass transition



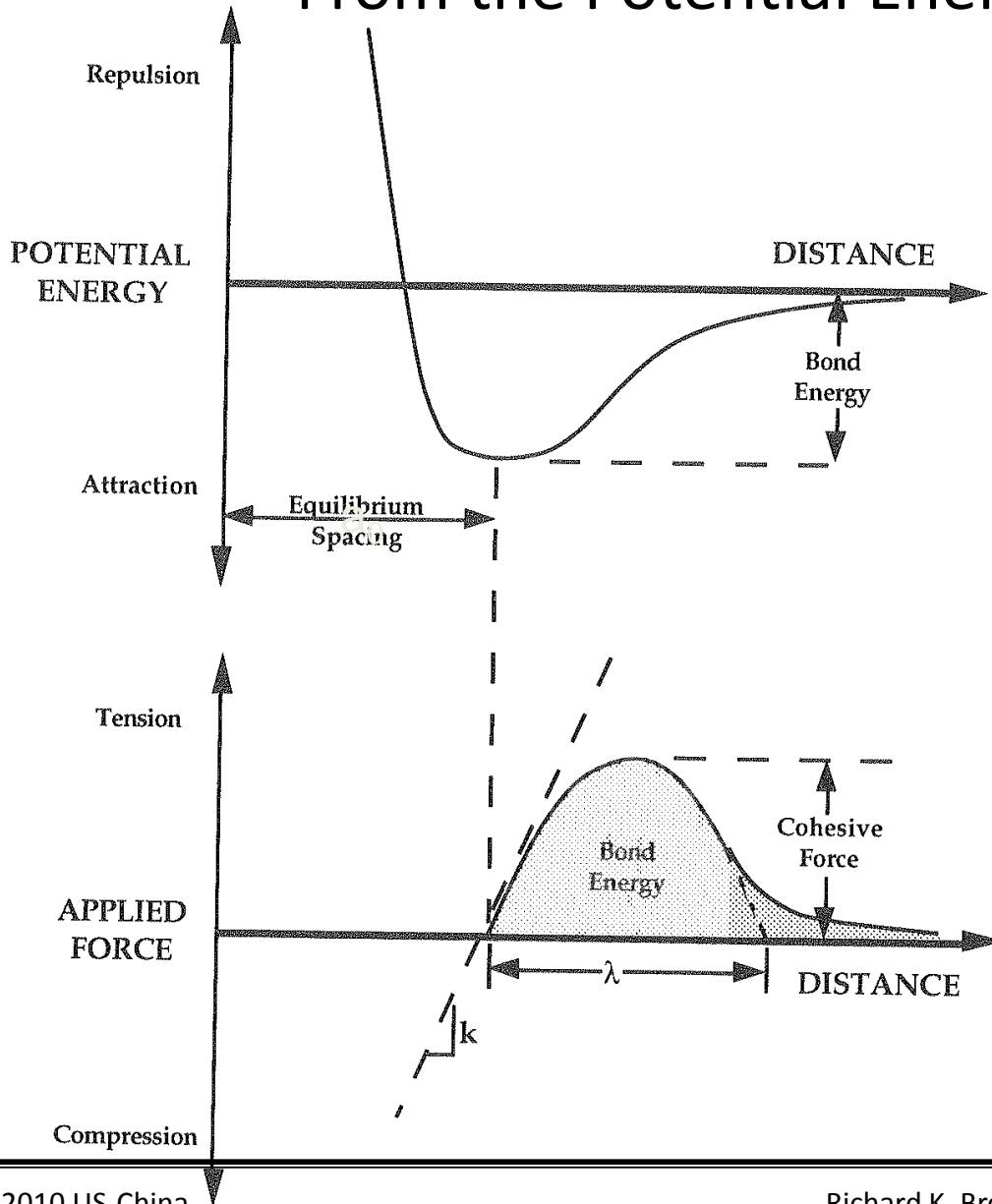
## Summary: Elasticity

- There is a limited correlation between  $E$  and  $T_g$  within compositional series, but not necessarily between compositional types
- High elastic moduli are favored by structural disorder and atomic packing seems to be more important than bond strength
- Poisson's ratio ( $\nu$ ) correlates with atomic packing density and with network dimensionality (polymerization)
- The temperature dependence of elastic properties above  $T_g$  may be related to “fragile” and “strong” viscosity behavior.

# Glass Strength

What factors determine the strength of glass?

# Theoretical Strength Can Be Estimated From the Potential Energy Curve (Orowan)



$$\sigma_m = \lambda E / \pi a_0$$

$$2\gamma_f = \sigma_m \int \sin(\pi x / \lambda) dx = \lambda \sigma_m / \pi$$

$$\sigma_m = [\gamma_f E / a_0]^{1/2}$$

If  $E = 70 \text{ GPa}$ ,  $\gamma_f = 3.5 \text{ J/m}^2$  and  $a_0 = 0.2 \text{ nm}$ , then

$$\sigma_m = 35 \text{ GPa} !$$

How does the addition of  $\text{Na}_2\text{O}$  affect the Young's modulus and fracture surface energy of silica glass? Consider what Prof. Pantano discussed the other day....



# Practical strengths are significantly less than the theoretical strengths:

Common glass products	~14-70 MPa
Freshly drawn glass rods	~70-140 MPa
Abraded glass rods	~14-35 MPa
Wet, scored glass rods	~3-7 MPa
Armored glass	~350-500 MPa
Handled glass fibers	~350-700 MPa
Freshly drawn glass fibers	~700-2100 MPa
Most metals, including steels	~140-350 MPa

C. E. Inglis (1913): flaws acted as stress concentrators

A.A Griffith (1921): critical flaws determine strength

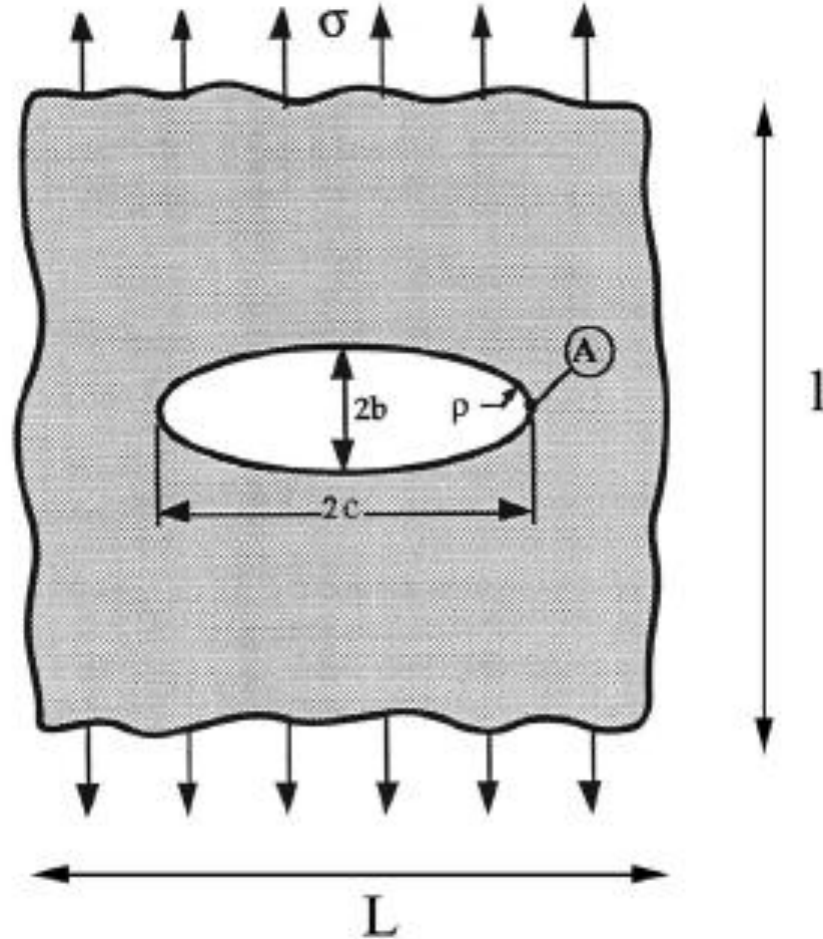
*Stress enhancement by flaws  
with length  $2c$  and radius  $\rho$ :*

$$\sigma_{yy} \approx 2 \sigma_a (c/\rho)^{1/2}$$

*Calculated strength with  
critical flaw  $c^*$ :*

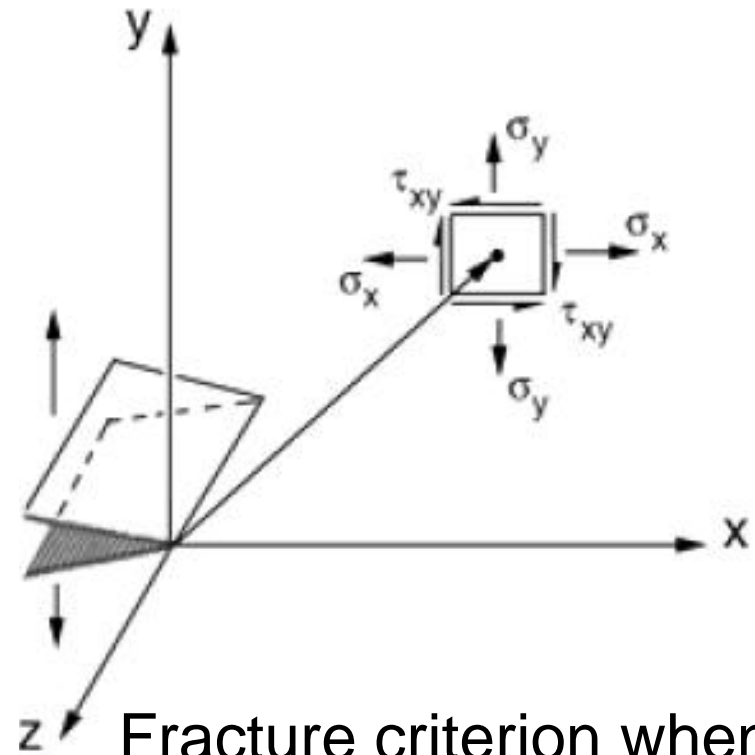
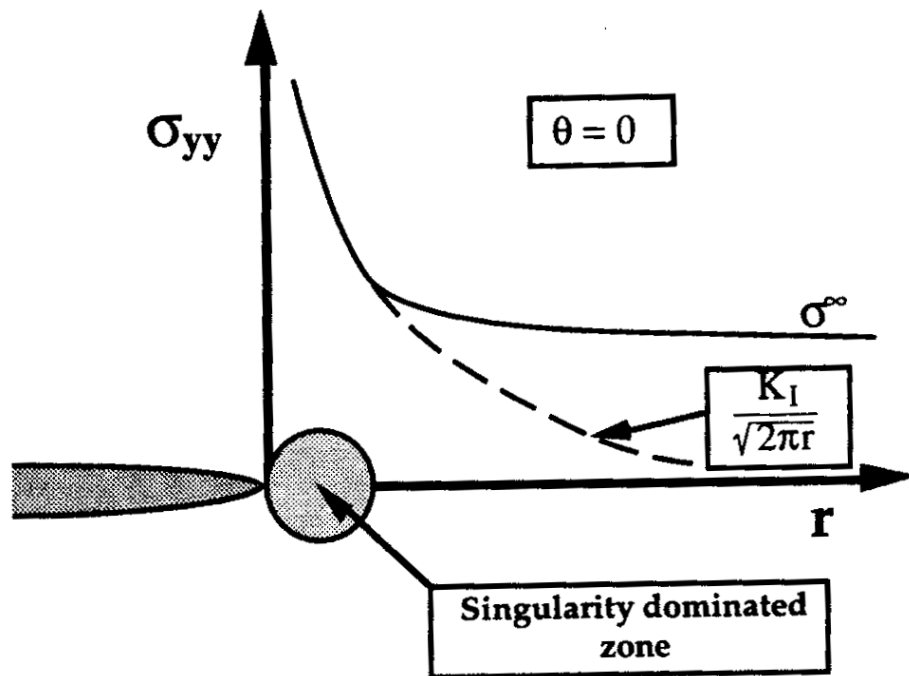
$$\sigma_f = [2 \gamma_f E / \pi c^*]^{1/2}$$

If  $E = 70 \text{ GPa}$ , and  $\gamma_f = 3.5 \text{ J/m}^2$   
Then a crack of 100 microns will  
result in a failure stress of  $\approx 25 \text{ MPa}$



Fracture mechanics allow the evaluation of stresses in the vicinity of a propagating

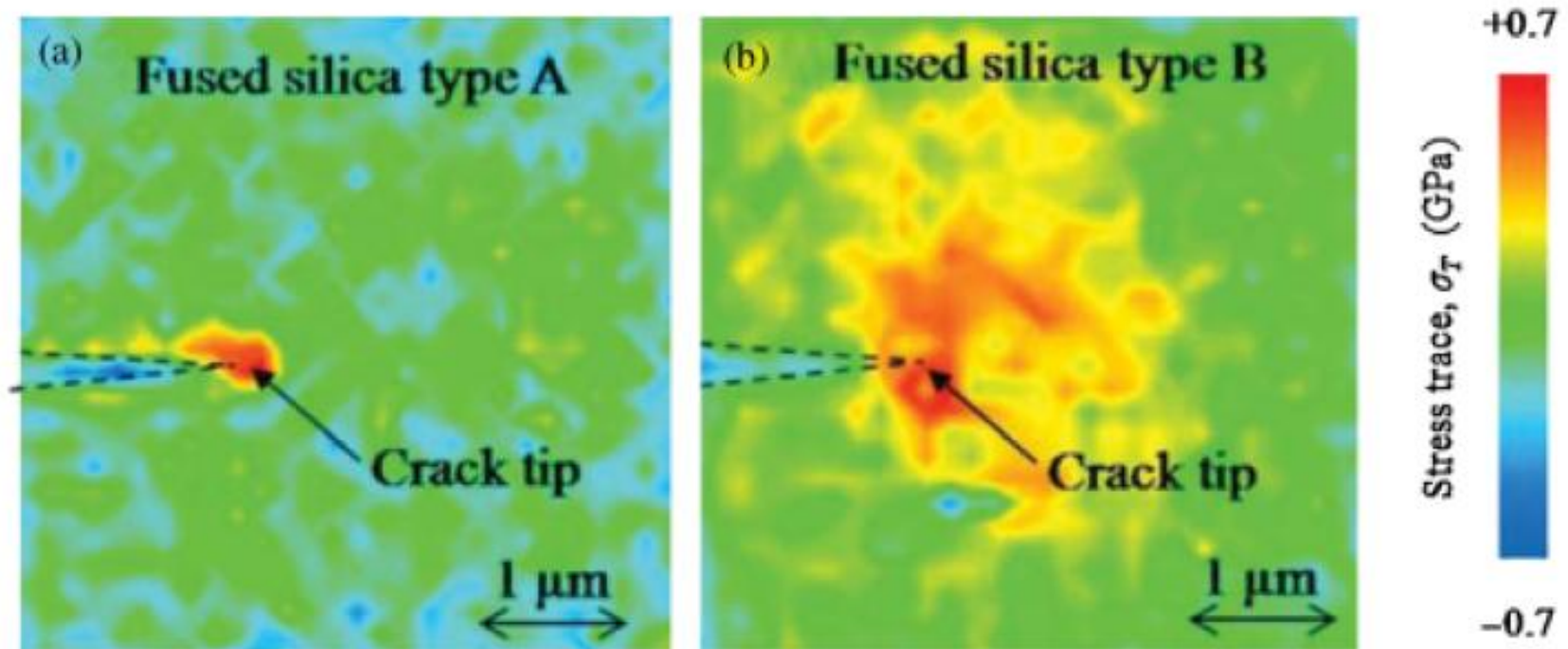
$$\sigma_{ij} = [K / (2 \pi r)^{1/2}] f_{ij} (\theta)$$



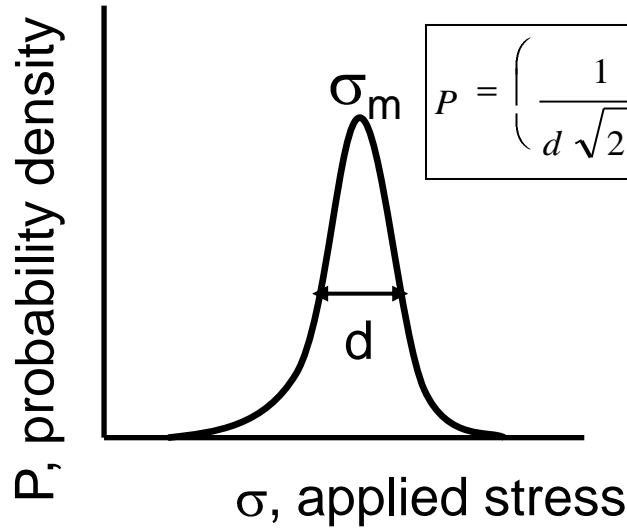
Fracture criterion when stress intensity exceeds the strain energy release rate (depends on  $E$ ,  $\gamma_f$ )

$$K_{Ic} = \sigma_a (\pi c)^{1/2}$$

Cathodoluminescence measurements of stress distributions around crack tips  
(Pezzotti and Leto, 2007)

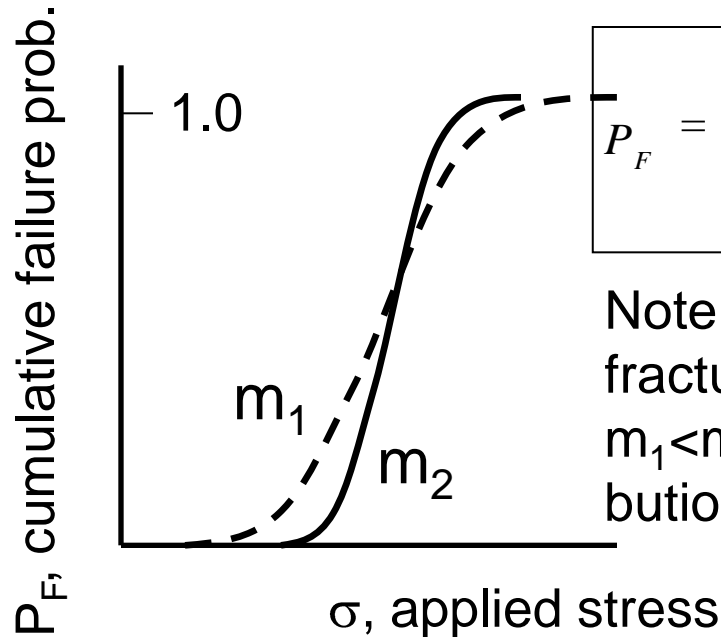
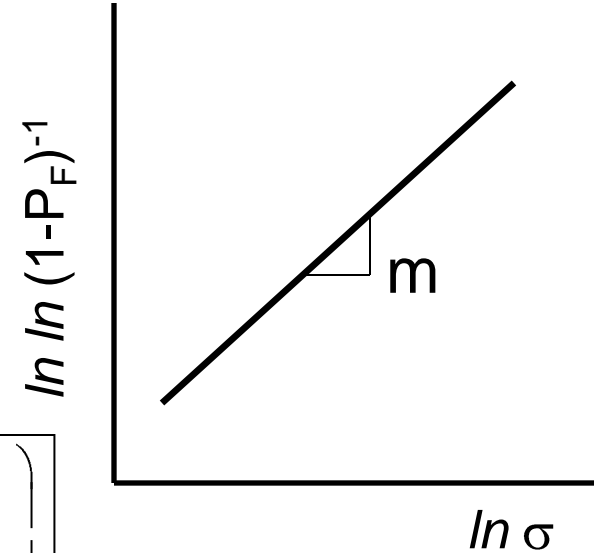
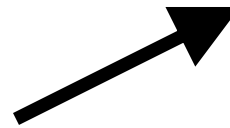


# An aside: Weibull Statistics



$$P = \left( \frac{1}{d \sqrt{2\pi}} \right) \exp \left( \frac{-(\sigma - \sigma_m)^2}{2d^2} \right)$$

$$\ln \left[ \ln \left( \frac{1}{1 - P_F} \right) \right] = m \ln \sigma - \ln \sigma_0$$



$$P_F = 1 - \exp \left( - \left( \frac{\sigma}{\sigma_0} \right)^m \right)$$

Note: same 'average' fracture strength, but  $m_1 < m_2$  (broader distribution of strengths).

# Room temperature tensile tests of pristine silica fibers drawn and tested in vacuum- bimodal distribution

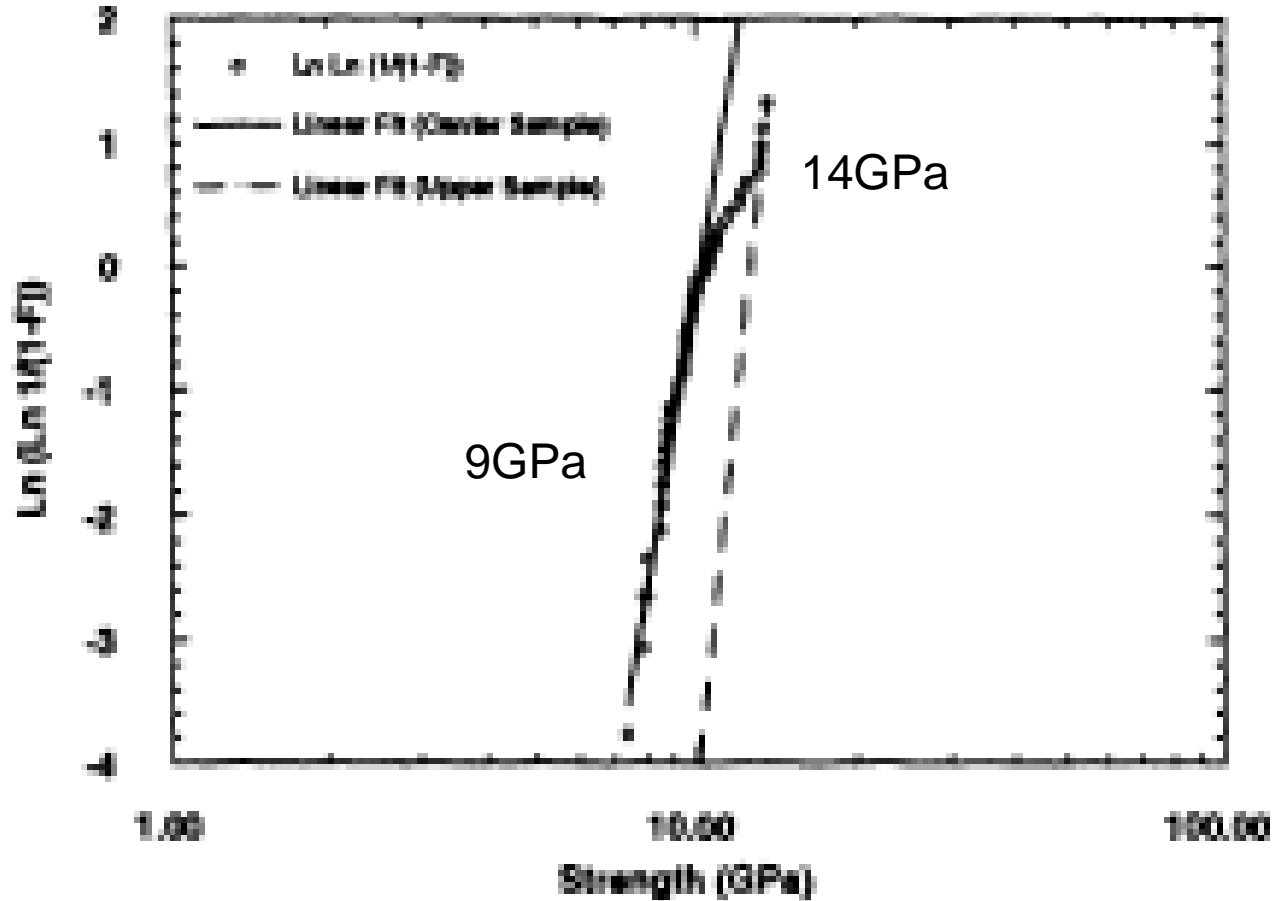
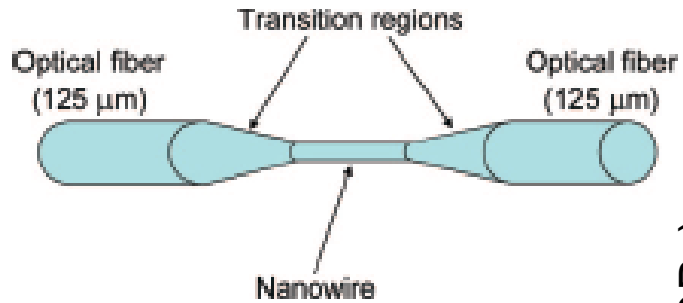


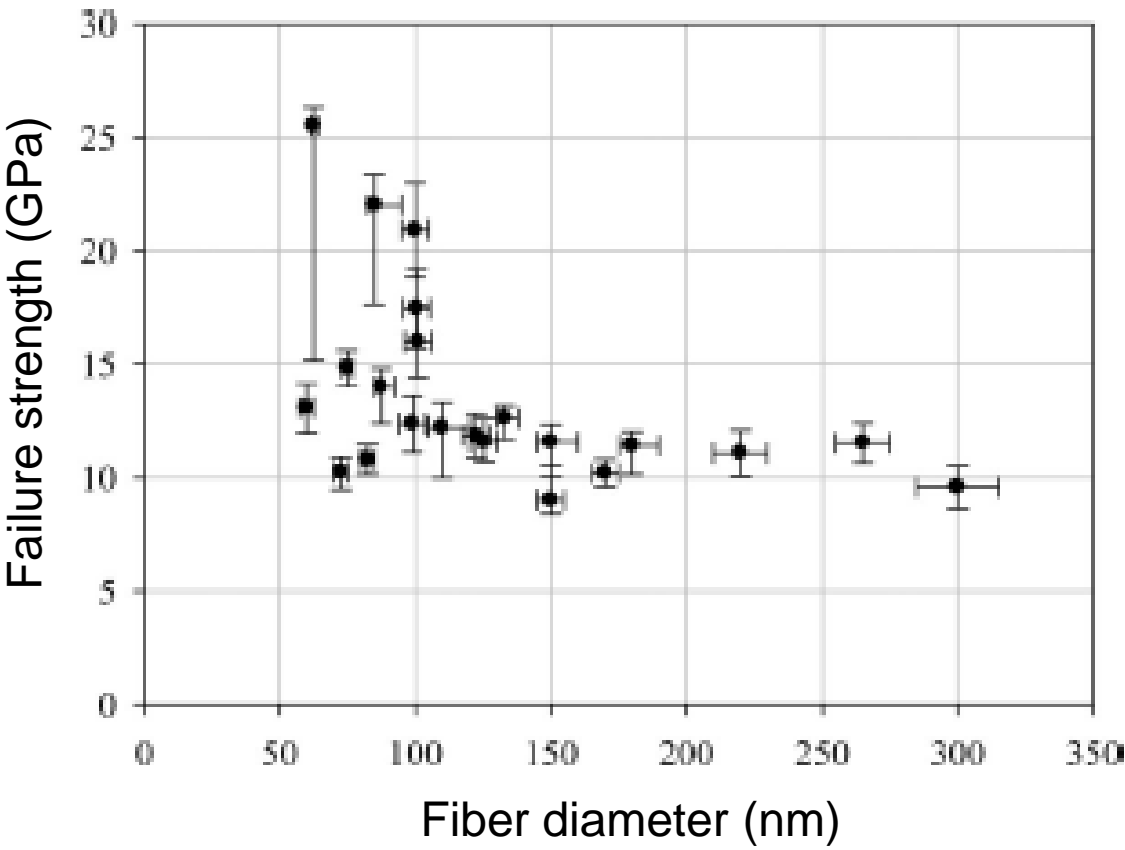
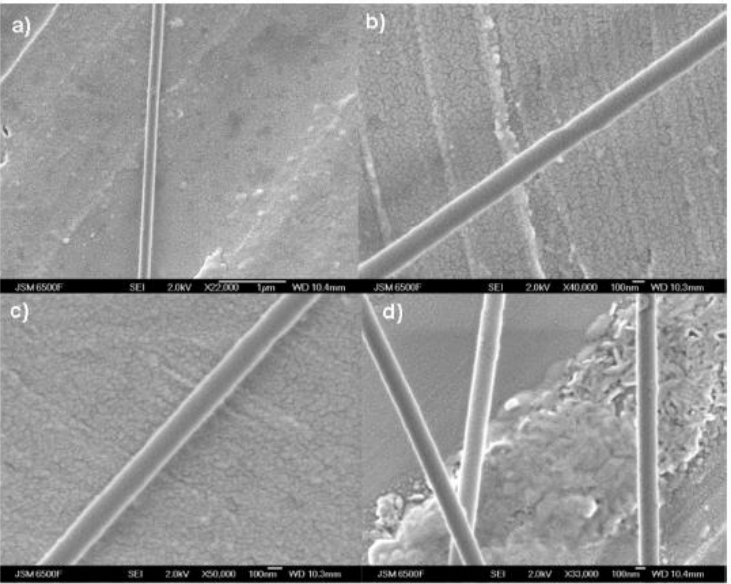
Figure 2 Strength distributions for T-08

Smith and Michalske, 1992

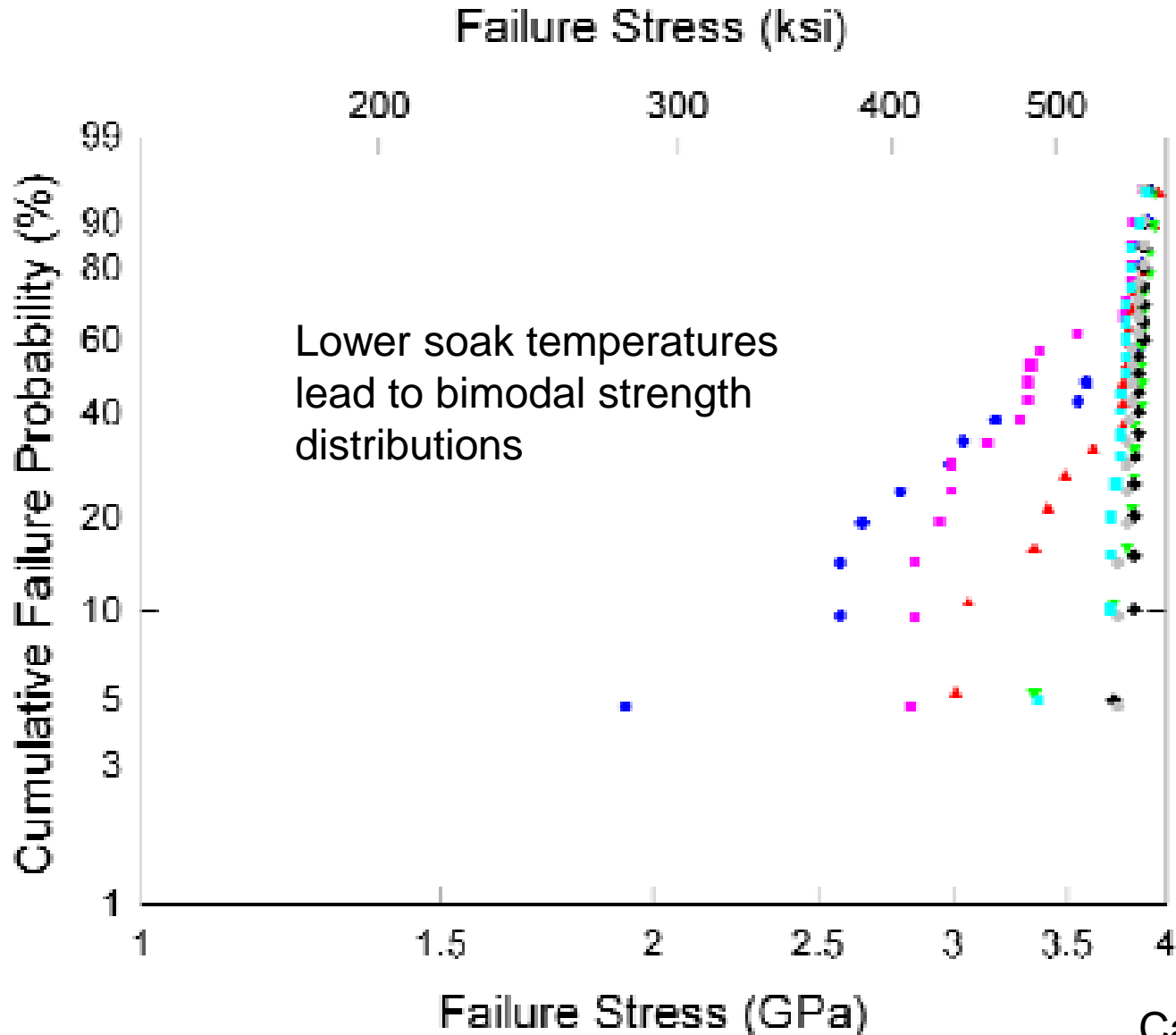
The Ultimate Strength of Glass Silica Nanowires, G. Brambilla and DN Payne, Nano Letters, 9[2] 831 (2009)



Flame-attenuation of optical fibers

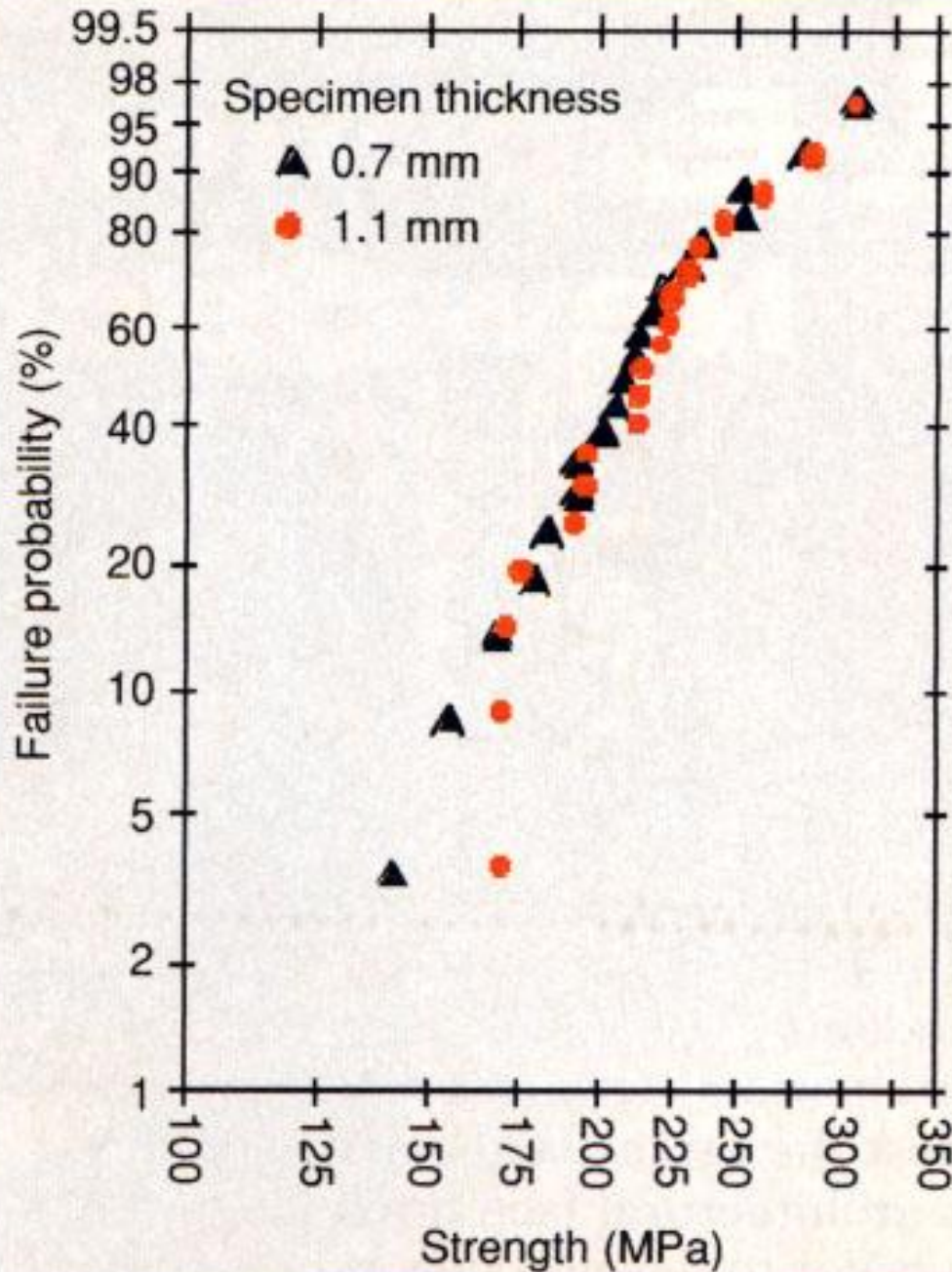


# E-glass fibers (tensile tests, in air)



Cameron, 1968

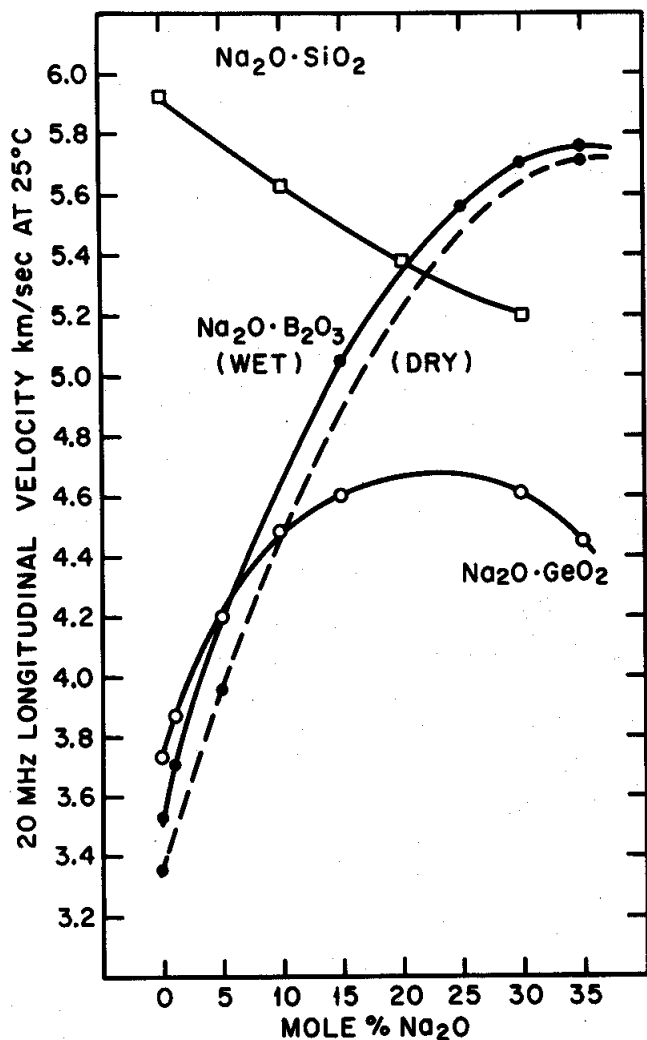




Concentric ring tests,  
 abraded Corning glass 1737,  
 two different thicknesses.

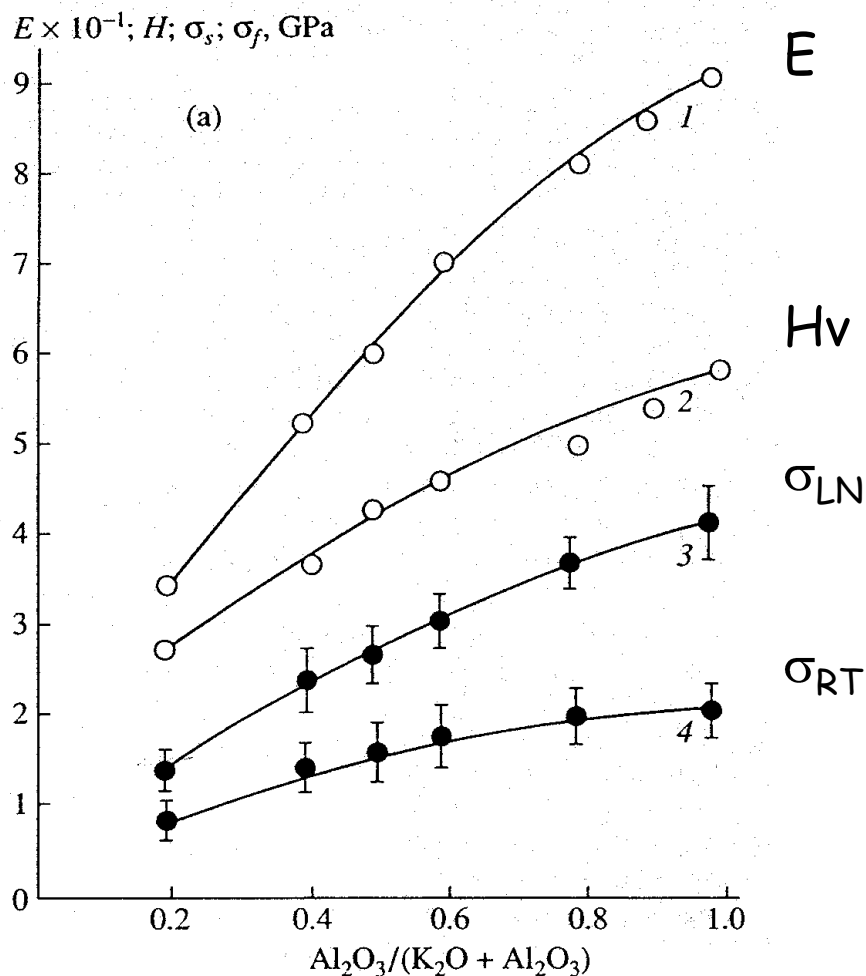
Gulati, et al., *Ceramic Bulletin*,  
 83[5] 14, 2004

# Mechanical properties depend on glass structure



## K/Al-metaphosphate glasses

Baikova, et al. *Glass Phys. Chem.*, 21[2] (1995) 115.



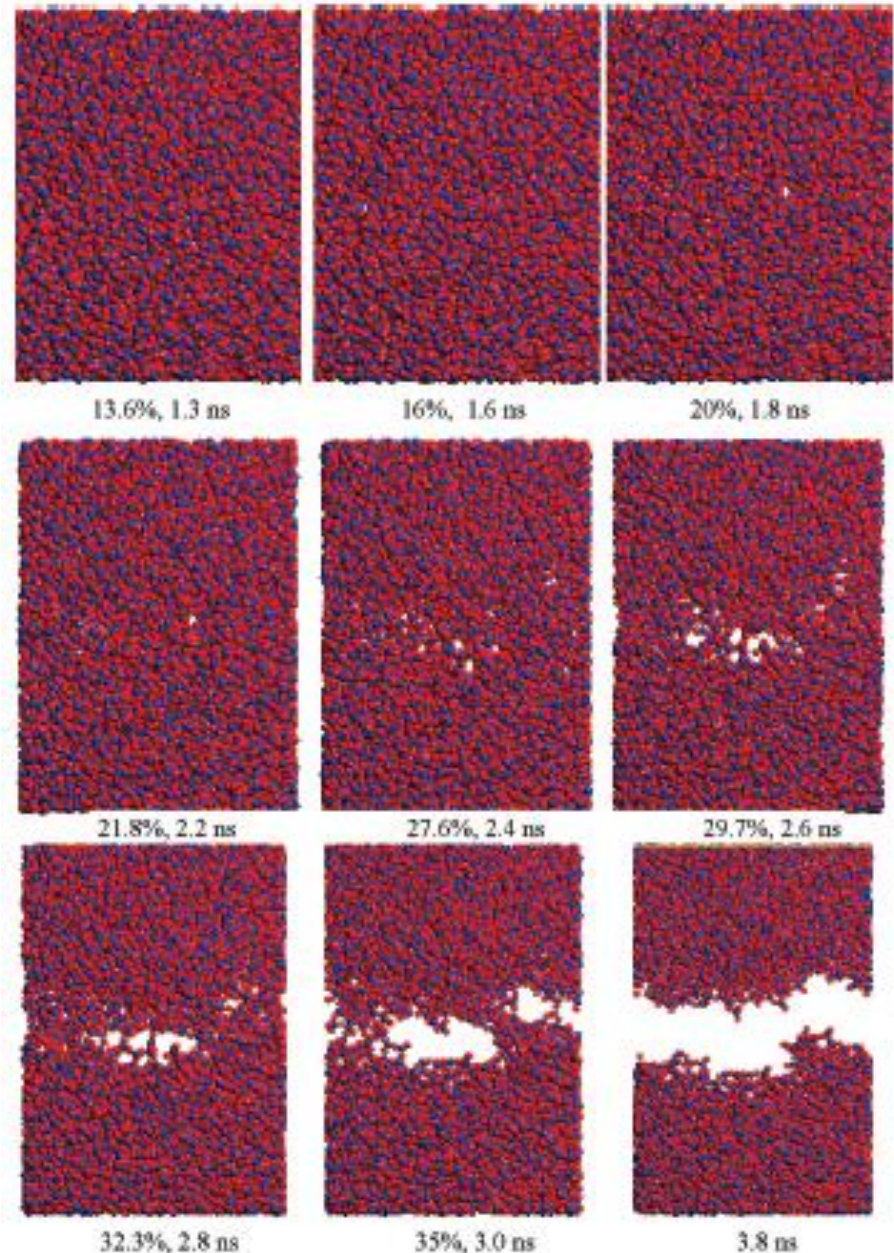
**Table 2.** Mechanical characteristics of inorganic glasses in three oxide systems

Glass no.	Chemical composition	Strength in liquid nitrogen $\sigma$ , GPa	Hardness $H$ , GPa	Young's modulus $E$ , GPa	Ultimate elastic strain $\epsilon = \sigma/E$ , %
Borate glasses					
1	$B_2O_3$	1.2	1.7	22	5.5
2	$15Na_2O \cdot 85B_2O_3$	2.7	3.9	52	5.2
3	$33Na_2O \cdot 67B_2O_3$	3.0	4.9	73	4.1
Silicate glasses					
4	$SiO_2$	12.0	8.5	73(100*)	12.0*
5	$33Na_2O \cdot 67SiO_2$	3.5	3.7	60	5.8
6	$12.5Na_2O \cdot 12.5Al_2O_3 \cdot 75SiO_2$	8.3	5.4	72	11.5
7	$16.5Na_2O \cdot 16.5Al_2O_3 \cdot 67SiO_2$	8.4	5.5	73	11.6
8	$25Na_2O \cdot 25Al_2O_3 \cdot 50SiO_2$	8.5	6.0	74	11.4
9	$14.5MgO \cdot 14.5Al_2O_3 \cdot 71SiO_2$	10.4	6.4	95	10.9
10	$6TiO_2 \cdot 94SiO_2$	7.5	6.5	68	11.0
Phosphate glasses					
11	$16.5Cs_2O \cdot 16.5Al_2O_3 \cdot 67P_2O_5$	1.6	3.5	50	3.2
12	$16.5Rb_2O \cdot 16.5Al_2O_3 \cdot 67P_2O_5$	2.4	3.8	55	4.4
13	$16.5K_2O \cdot 16.5Al_2O_3 \cdot 67P_2O_5$	2.5	4.1	59	4.2
14	$16.5Na_2O \cdot 16.5Al_2O_3 \cdot 67P_2O_5$	3.0	4.5	68	4.4
15	$16.5Li_2O \cdot 16.5Al_2O_3 \cdot 67P_2O_5$	3.4	4.9	74	4.6
16	$27.5Al_2O_3 \cdot 67.5P_2O_5$	4.0	5.7	89	4.5
17	$17.5Al_2O_3 \cdot 15ZnO \cdot 67.5P_2O_5$	5.7	5.5	81	7.0

\* The parameter obtained with due regard for the increase in the Young's modulus with an increase in the strain [17].

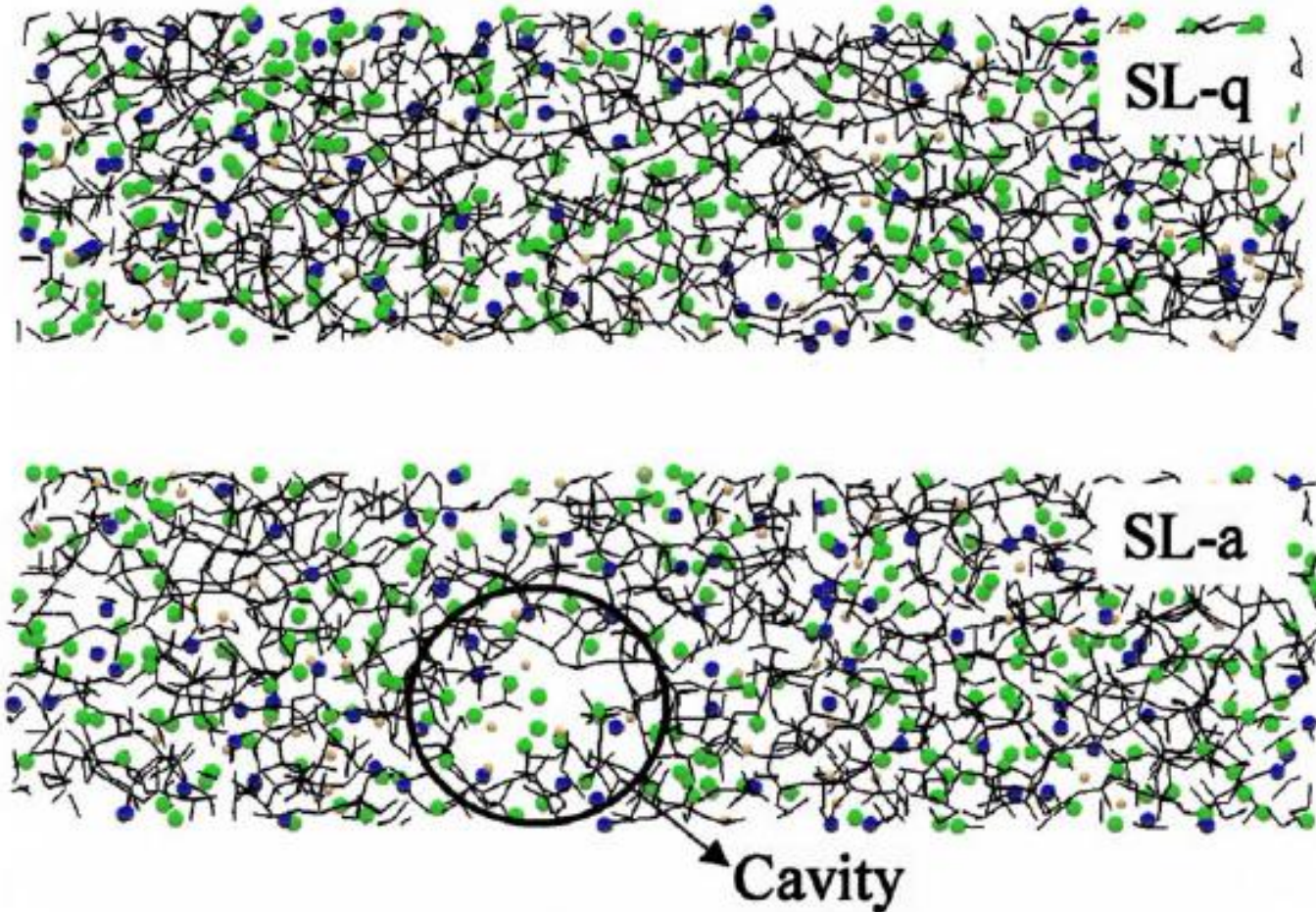
Pukh et al., 2005

MD Simulations of fracture reveal the development of cavities that coalesce to form the failure site



Pedone et al., 2008

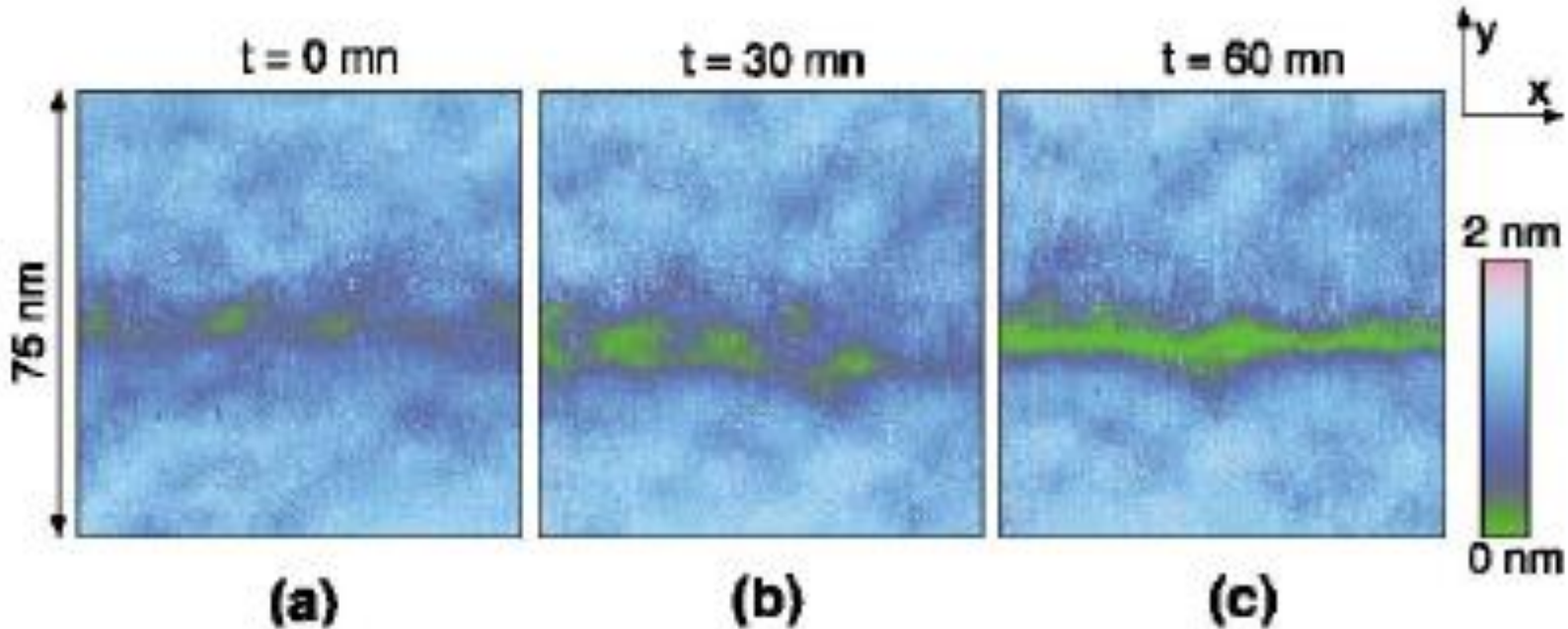
# Quenched and annealed soda-lime glasses at 5GPa tension



S. Ito and T. Taniguchi, JNCS (2004)

# There may be experimental evidence for cavitation near the tips of slow-moving cracks

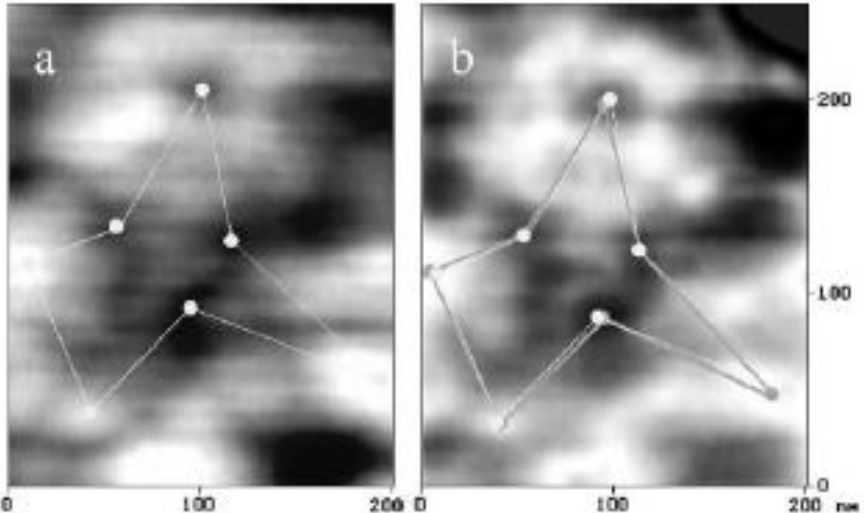
Aluminosilicate glass,  $10^{-11}$  m/s, 45% RH, AFM Images



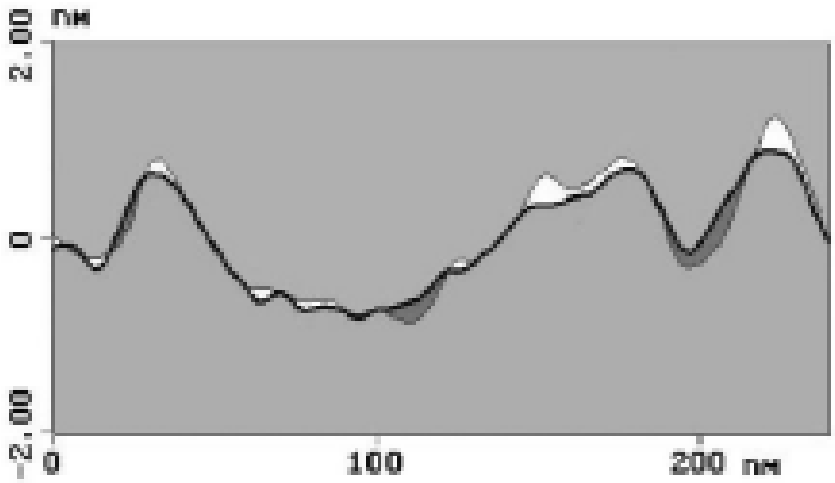
Célarié, et al., PRL (2003)

Formation of 'nano-cavities' interpreted as evidence for 'nano-ductile' fracture of glass!

# 'Nano-ductility' interpretation is not universal



'Post-mortem' AFM analyses of the opposing fracture surfaces show no evidence for the formation of nano-cavities



Note the relatively rough surface

Guin and Wiederhorn, PRL (2004)

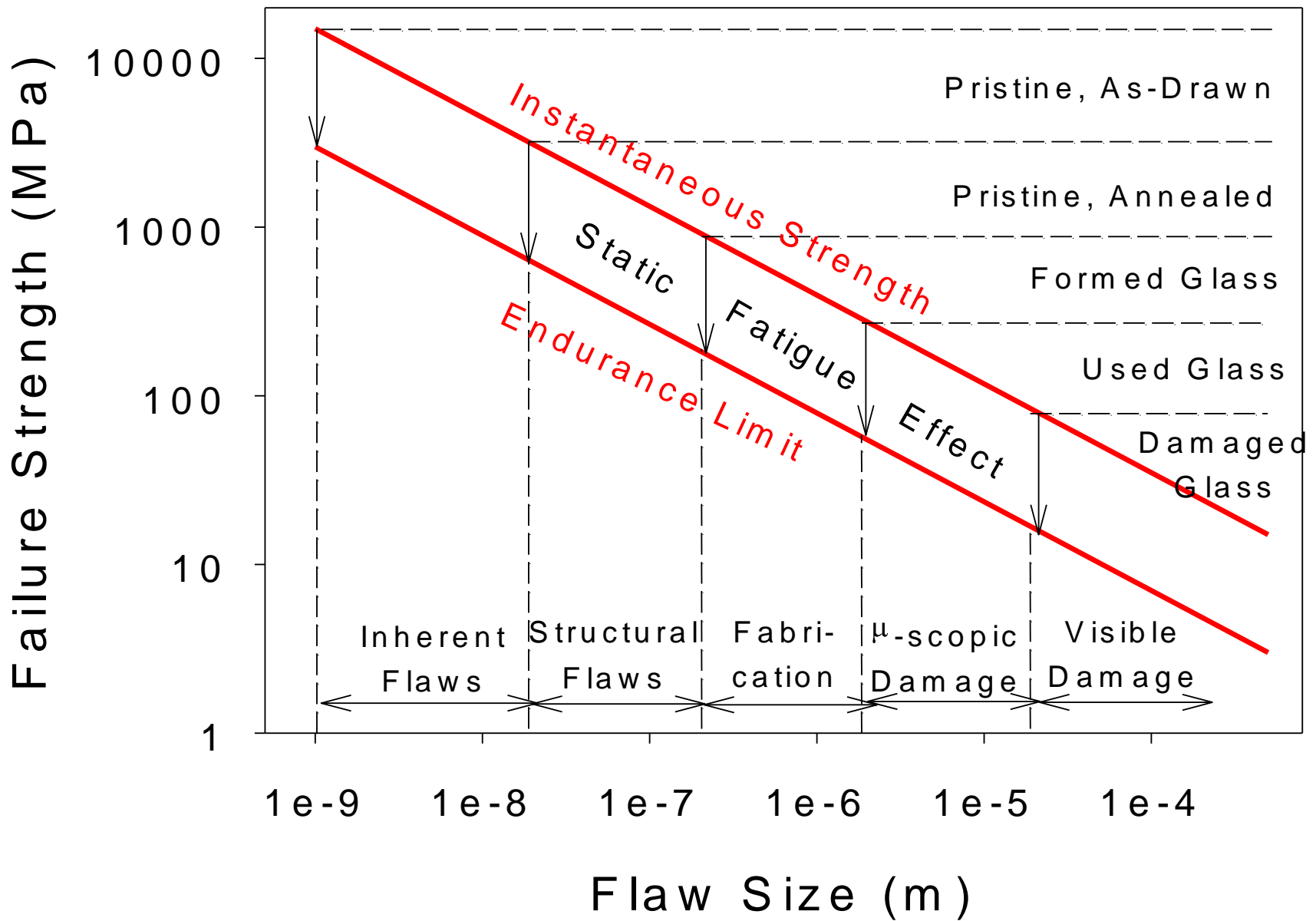
# Fatigue



# An example of fatigue in glass



<http://www.youtube.com/watch?v=r8q-R9ZISac>



After Mould (1967)

# Stress Corrosion: source for static fatigue- the reduction in strength with time

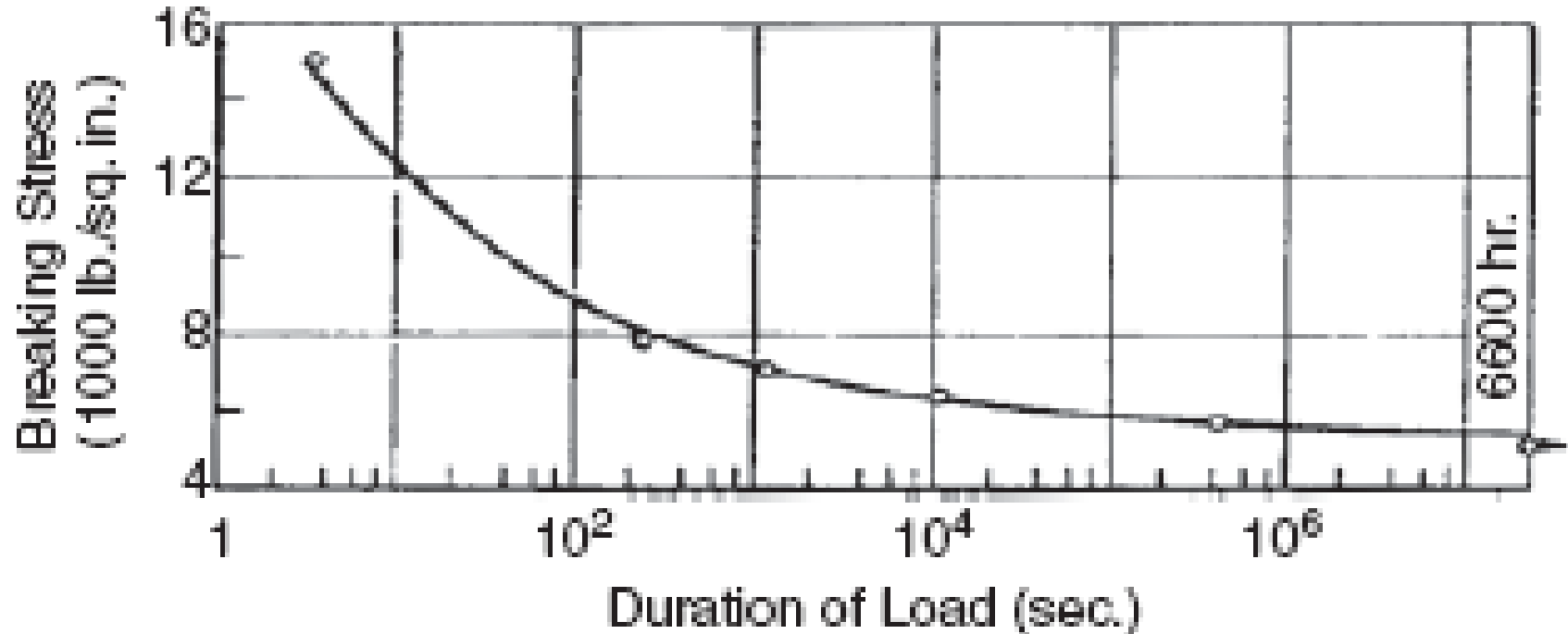
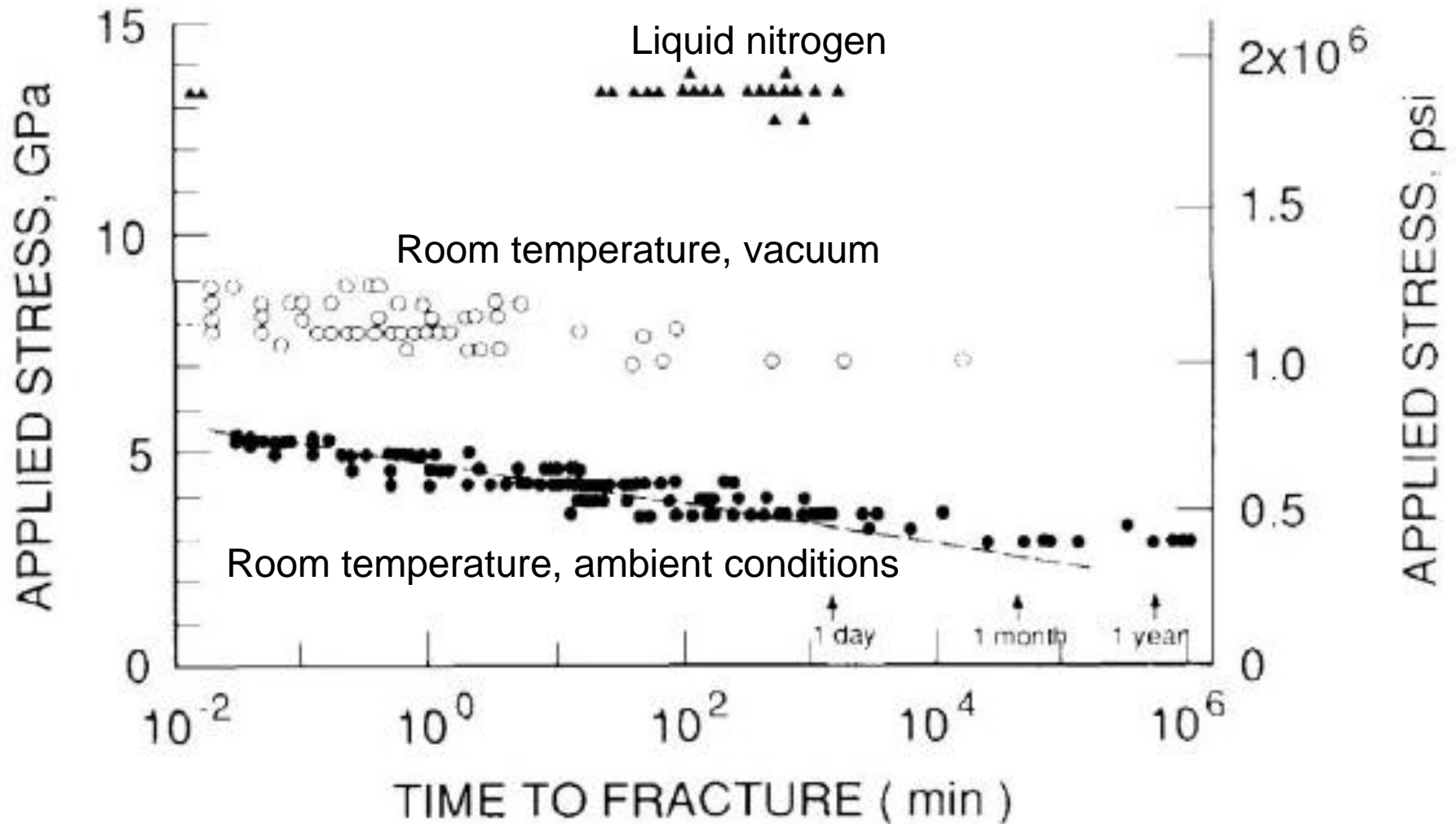
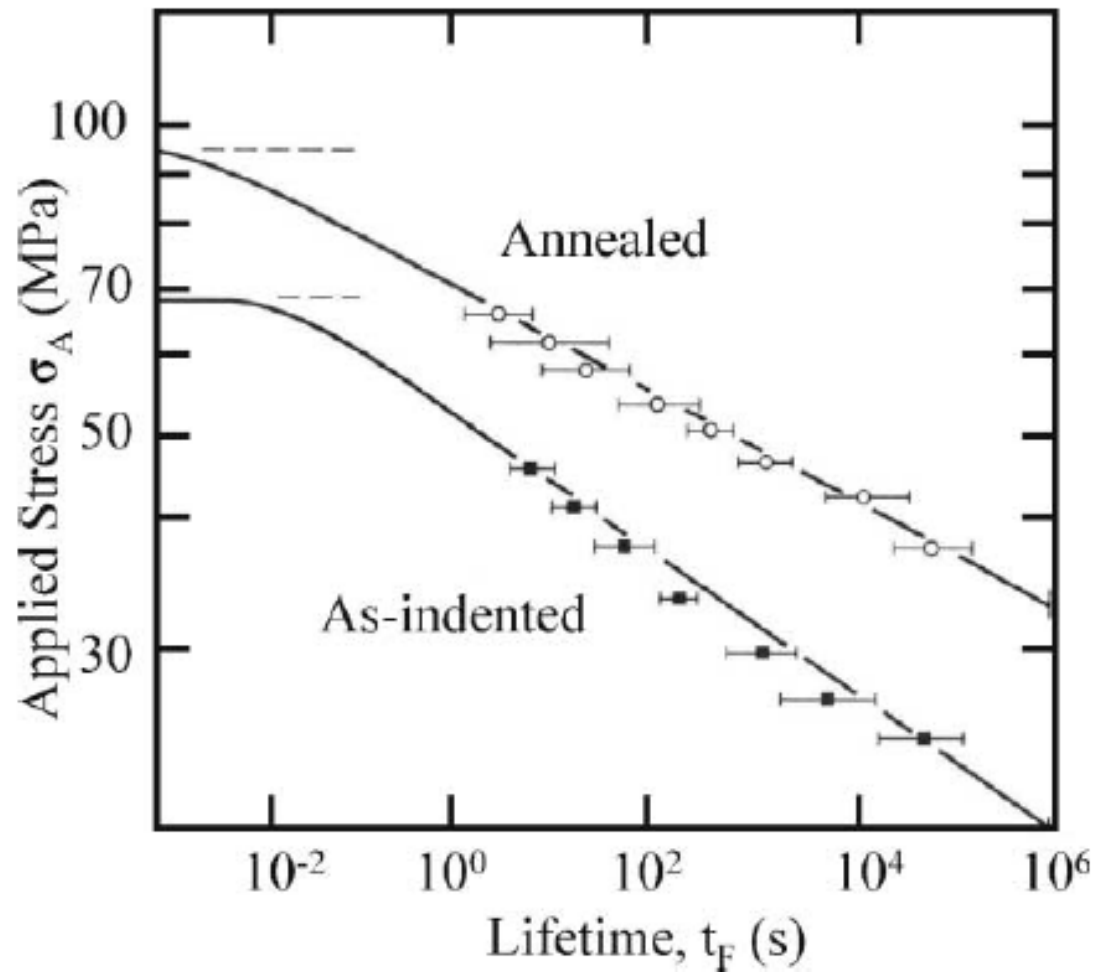


Fig. 1. Stress-time characteristics of glass, from bending tests on 1/4 in. diameter soda-lime-silicate rods. Taken from Shand.<sup>1</sup>

# Fatigue data on silica fibers

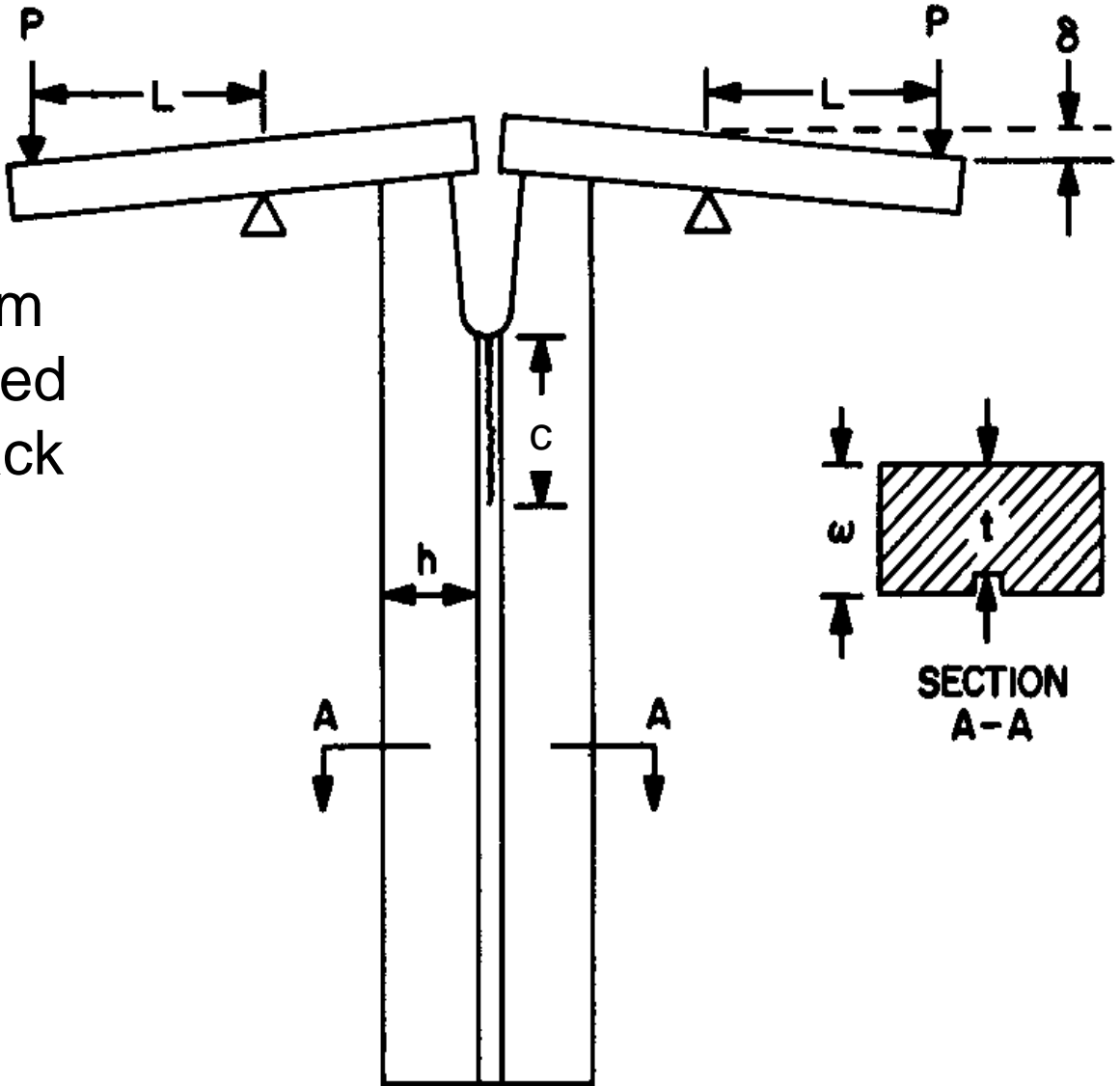


35. B. A. Proctor, I. Whitney, and J. W. Johnson, Proc Roy Soc A297, 534 (1967).



Note: residual stresses increase susceptibility to static fatigue

Fig. 10. Increased susceptibility to static fatigue due to indentation residual stresses. Vickers-indented soda-lime glass (load: 5 N), tested in water (from [25]).

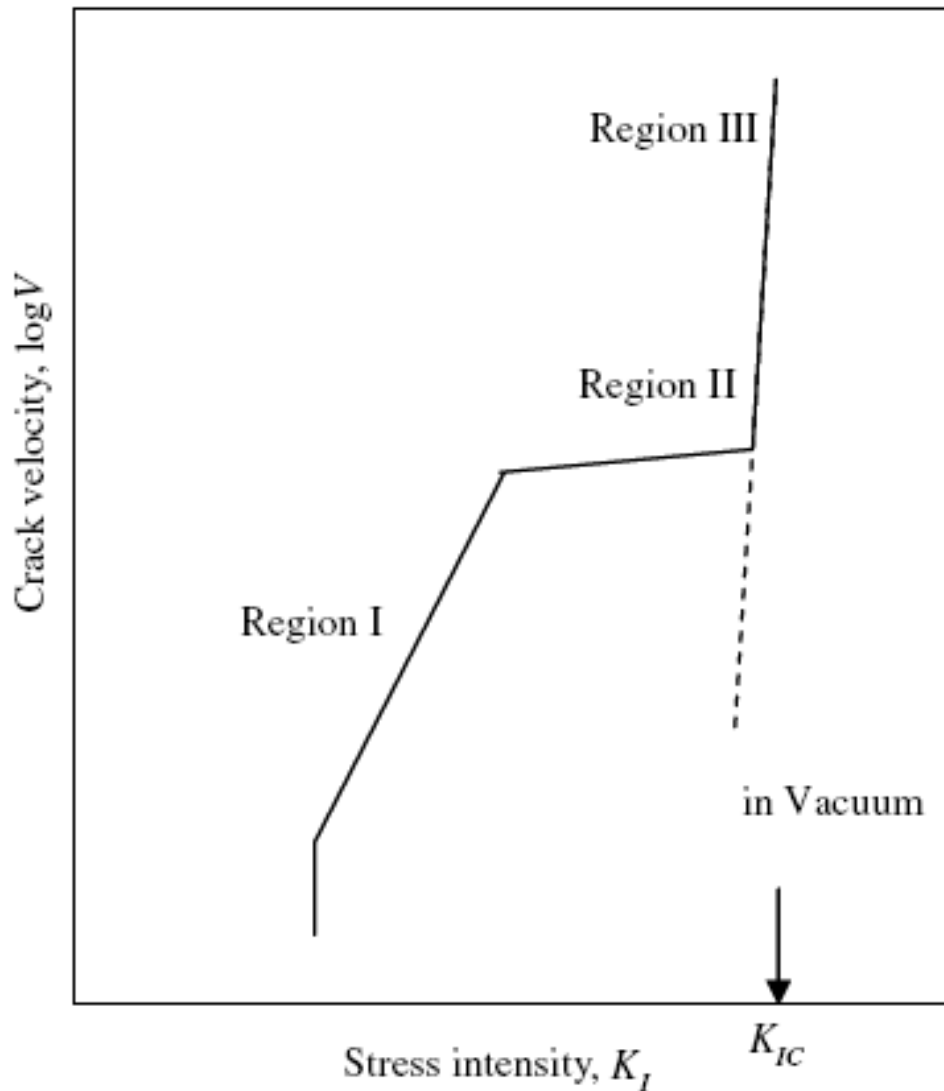


Double-Cantilever Beam (DCB) used for controlled stress intensity and crack velocity experiments

$$V=dc/dt$$

$$K=P^2/f(\text{geometry})$$

S. W. Freiman, D. R. Mulville and P. W. Mast, J. Mater. Sci., 8[11] 1573 (1973).



Crack propagation kinetics depend on the stress intensity

Region I: stress-corrosion

Region II: diffusion-limited

Region III: rapid fracture ( $K_{IC}$ )

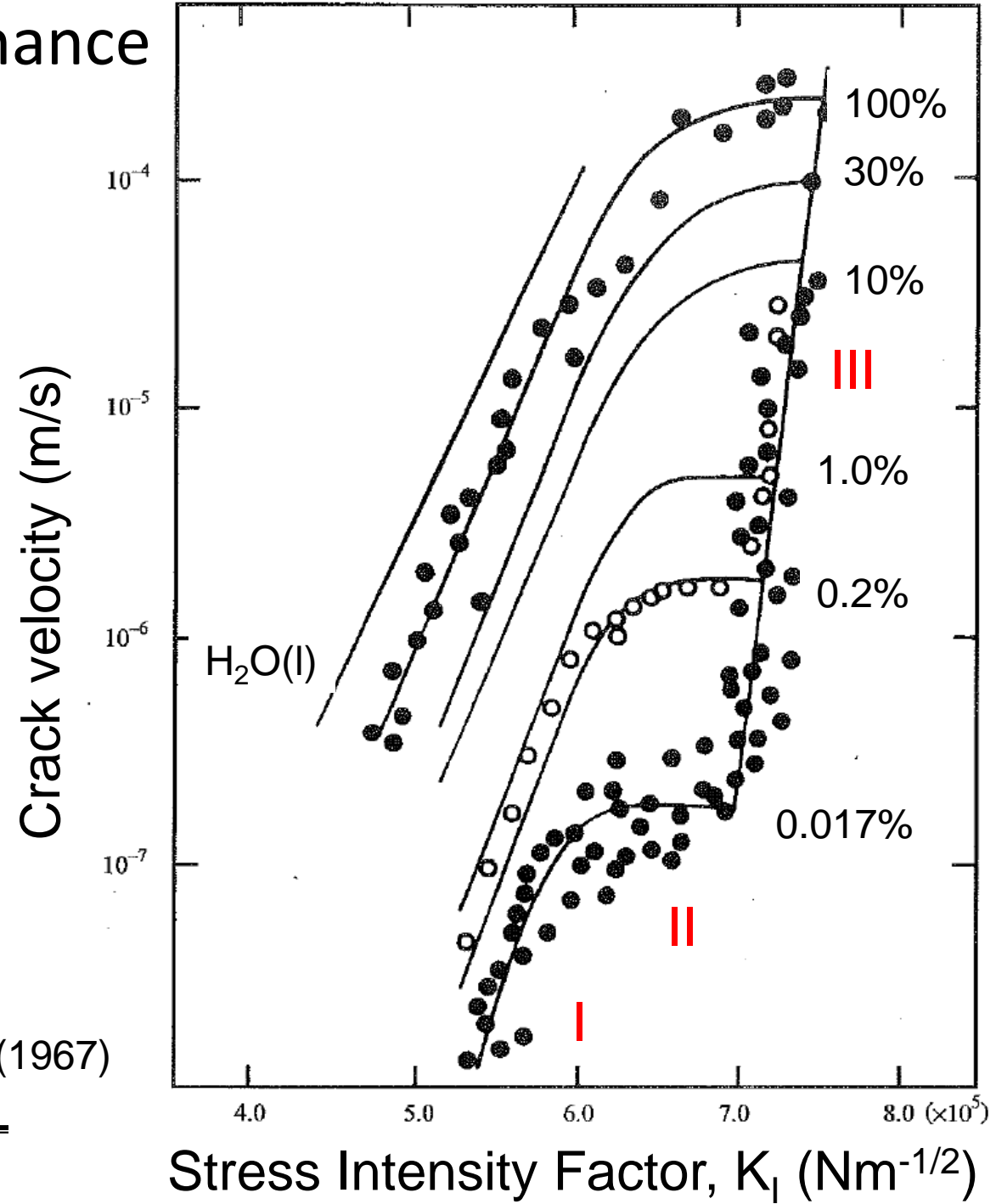
Region 0: propagation threshold

Fig. 1. The schematic of the  $K_I$ - $V$  curve for soda-lime-silicate glasses.  $K_{IC}$  is the critical stress intensity, i.e., fracture toughness. The dashed line shows the  $K_I$ - $V$  curve in a vacuum.

# Water and stress enhance crack growth in glass

## Region I: stress-corrosion

$v = AK_I^n$ , where  $n$  is the 'stress corrosion susceptibility factor'



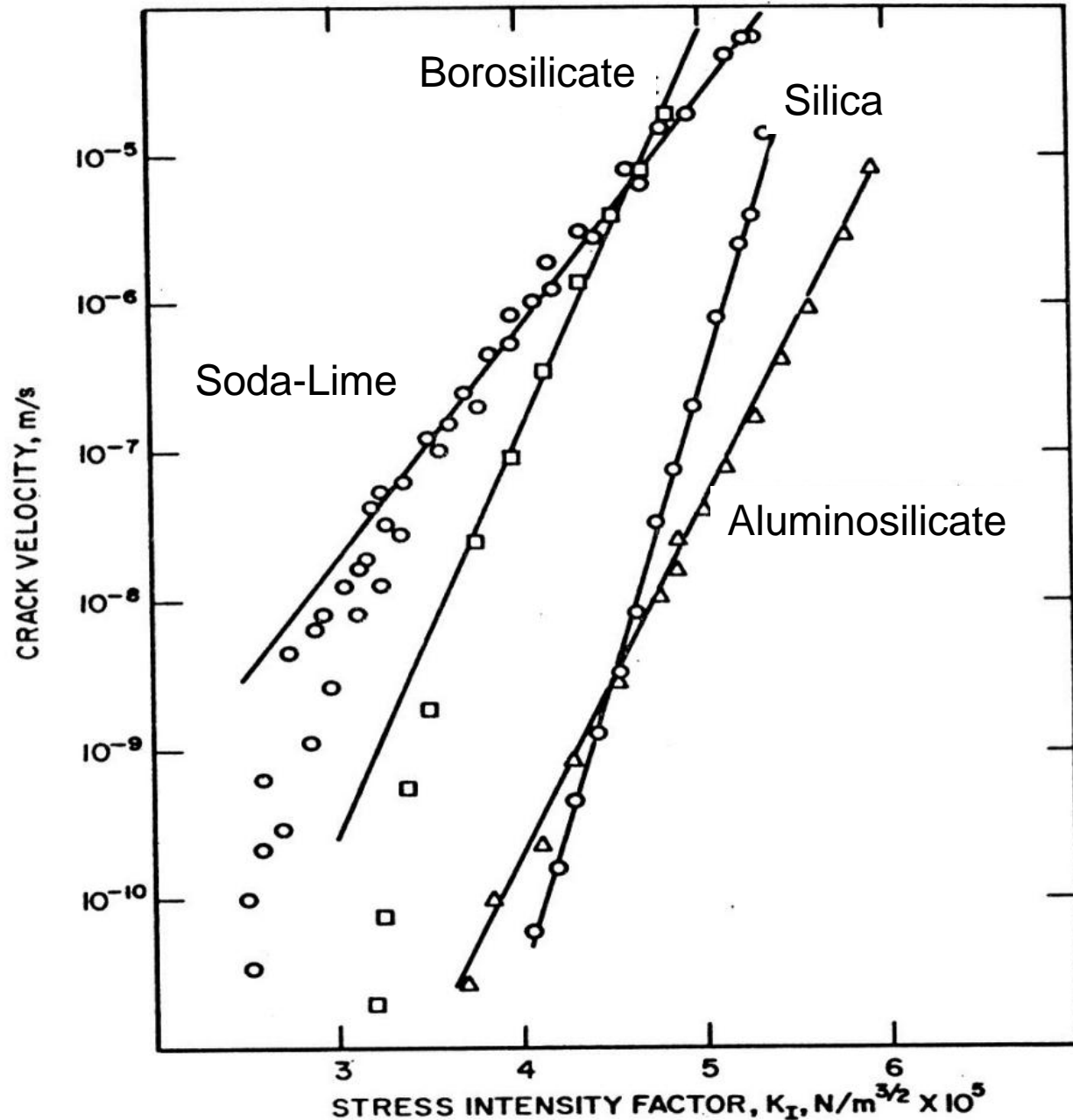
SM Wiederhorn, JACerS, 50 407 (1967)



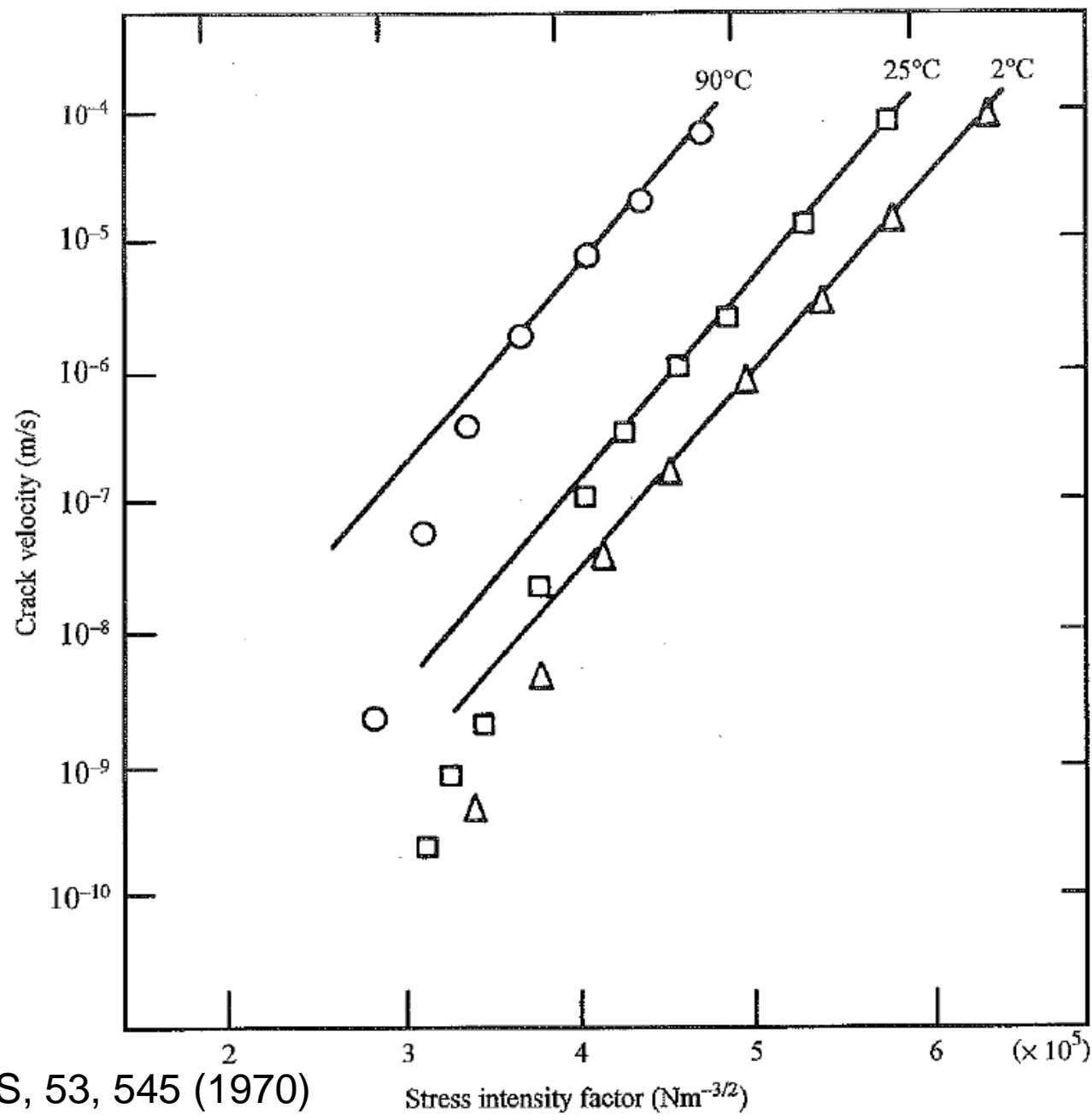
# Compositional-dependence of $v$ - $K$ behavior in Region I

Different glasses are more or less susceptible to fatigue effects –

*We do not understand this compositional dependence!*



# Temperature-dependence of v-K behavior in Region I



Wiederhorn and Bolz, JACerS, 53, 545 (1970)

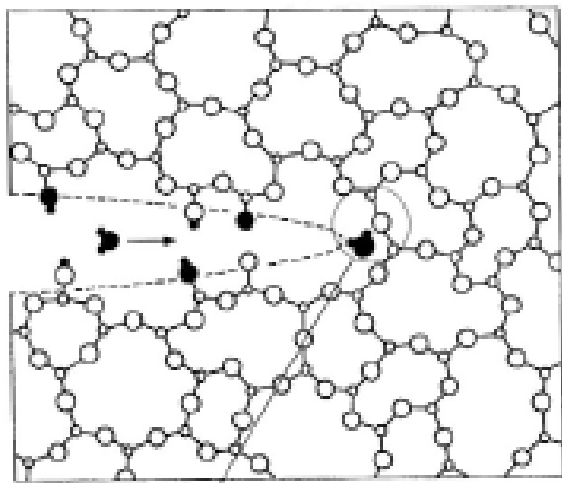
# Slow crack growth is a thermally activated process

Chemical rate theory has been used to explain the exponential form of the  $V - K_I$  curves:

$$V = V_0 \exp( - E + bK_I / RT )$$

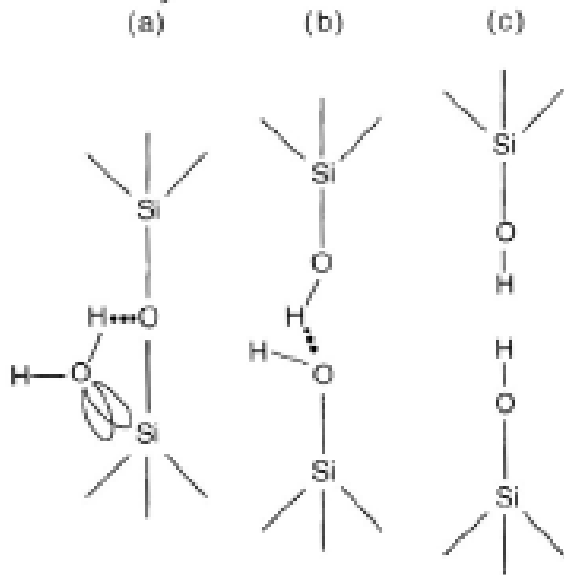
where  $V_0$  is a constant,  $E$  is the activation energy for the reaction,  $R$  is the gas constant,  $T$  is the temperature, and  $b$  is proportional to the activation volume for the crack growth process,  $\Delta V^*$ .

Wiederhorn, et al., JACerS, 1974



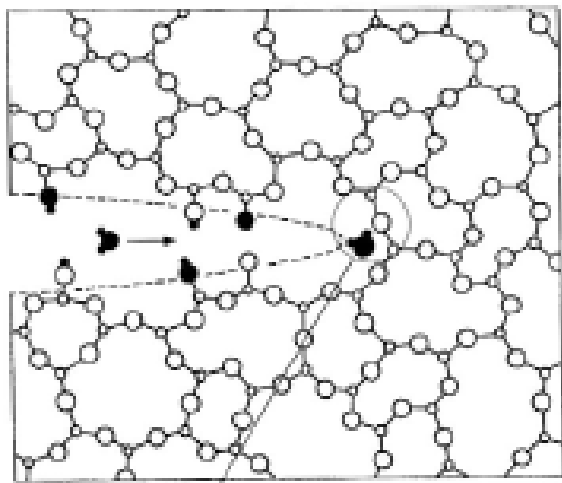
## Stress-corrosion in silicate glass:

- a. Adsorption** of a water molecule on a strained siloxane bond at a crack tip;
- b. Reaction** based on proton and electron transfer;
- c. Separation** of silanol groups after rupture of the hydrogen bond.



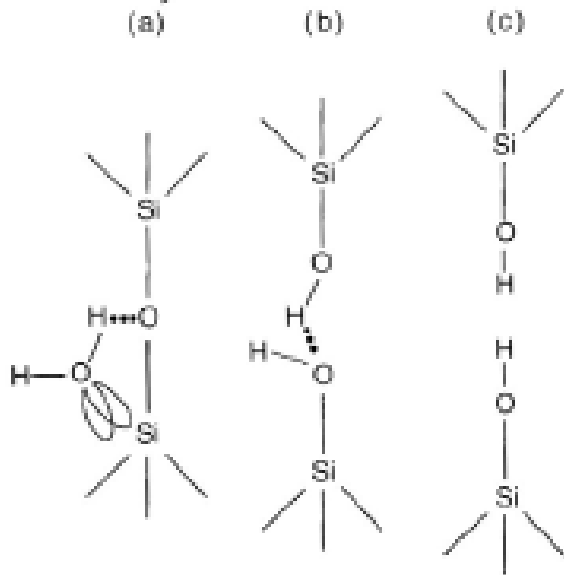
Net result: extension of the crack length by one tetrahedral unit

*Michalske et Bunker, J. Appl. Phys. (1984)*



## Stress-corrosion in silicate glass:

- Reactive molecules can donate both protons and electrons to the ruptured siloxane bond;
- Reactive molecules are small enough to reach the crack tip ( $<0.5$  nm).



Water, ammonia, hydrazine ( $\text{H}_2\text{N}-\text{NH}_2$ ),  
formamide ( $\text{CH}_3\text{NO}$ )

*Michalske et Bunker, J. Appl. Phys. (1984)*

# Other 'crack-tip chemistries' lead to strength increasing with time

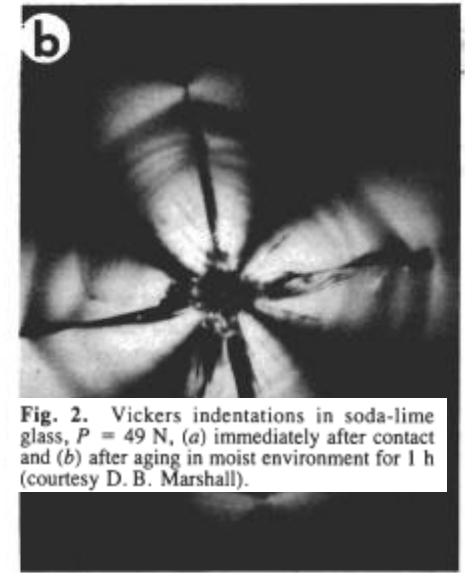
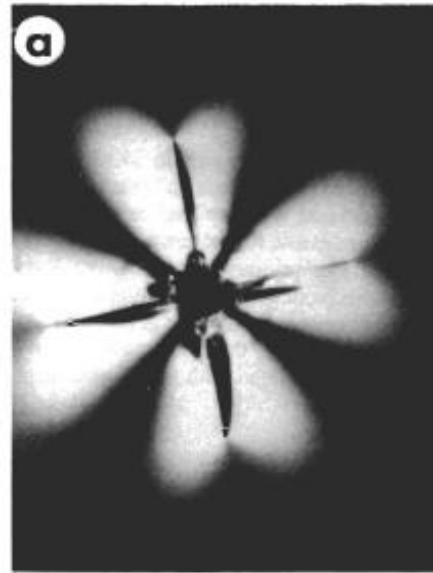
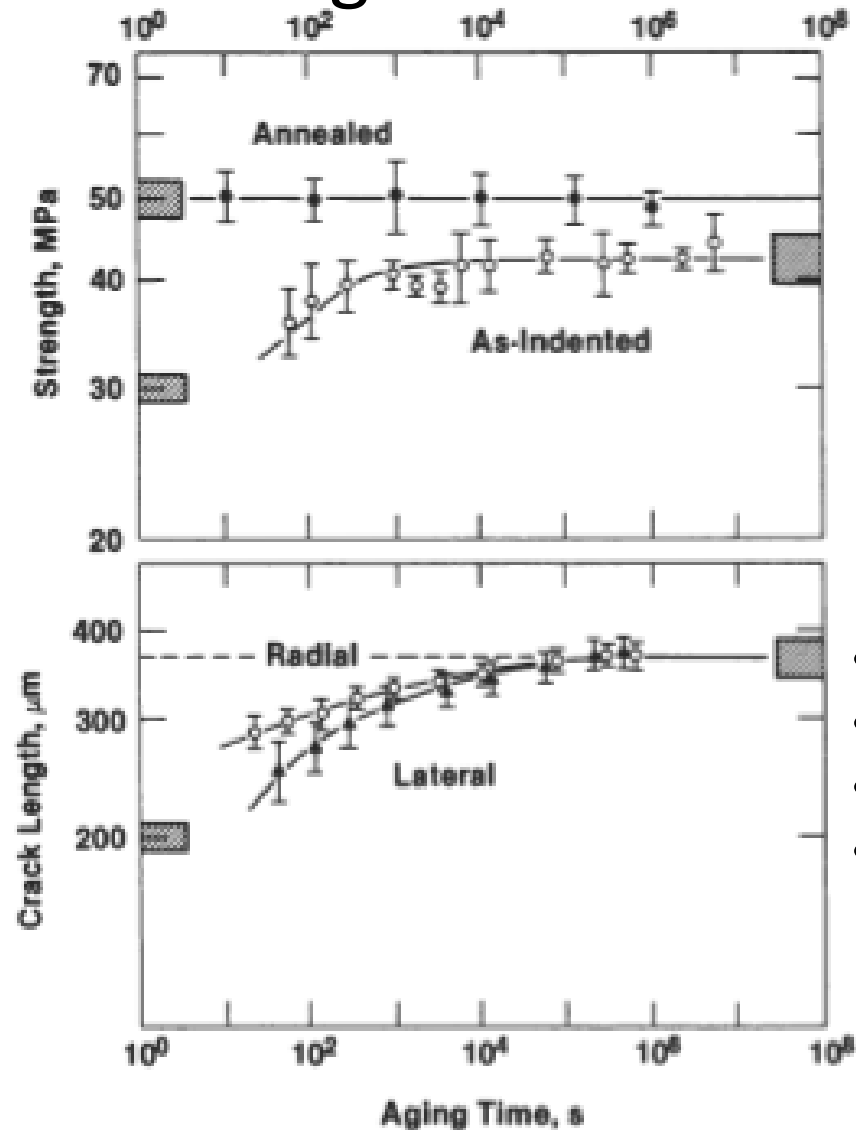
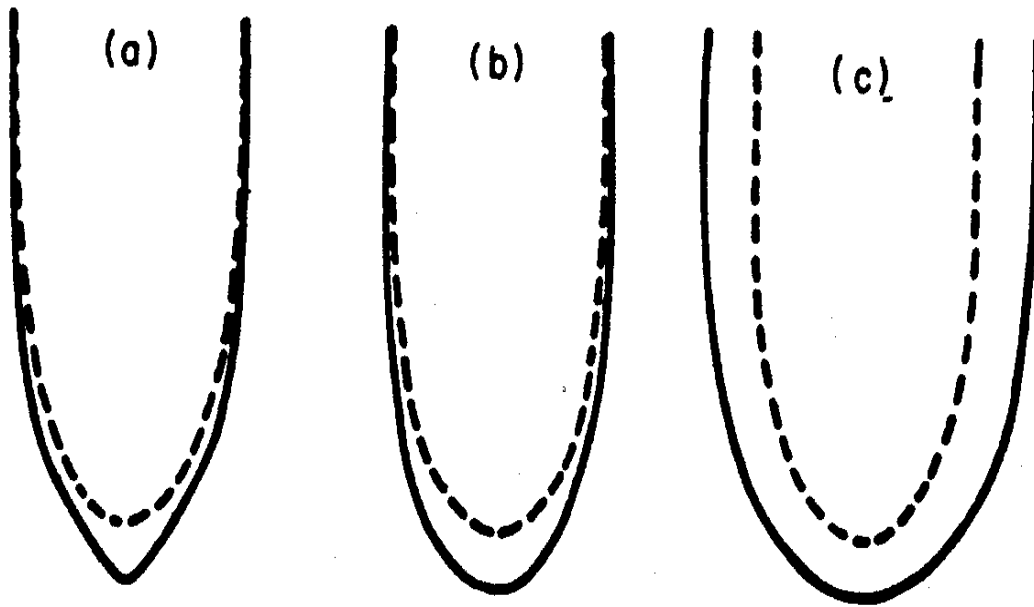


Fig. 2. Vickers indentations in soda-lime glass,  $P = 49$  N, (a) immediately after contact and (b) after aging in moist environment for 1 h (courtesy D. B. Marshall).

- Controlled flaws (Vicker's indents) in S-L-S
- Aging in different environments
- Tensile tests in inert conditions (silicone oil)
- May be due to stress release- not crack geometry?

Lawn et al., JACerS, 68[1] 25 (1985)

# Crack-tip sharpness depends on glass structure and corrosion conditions



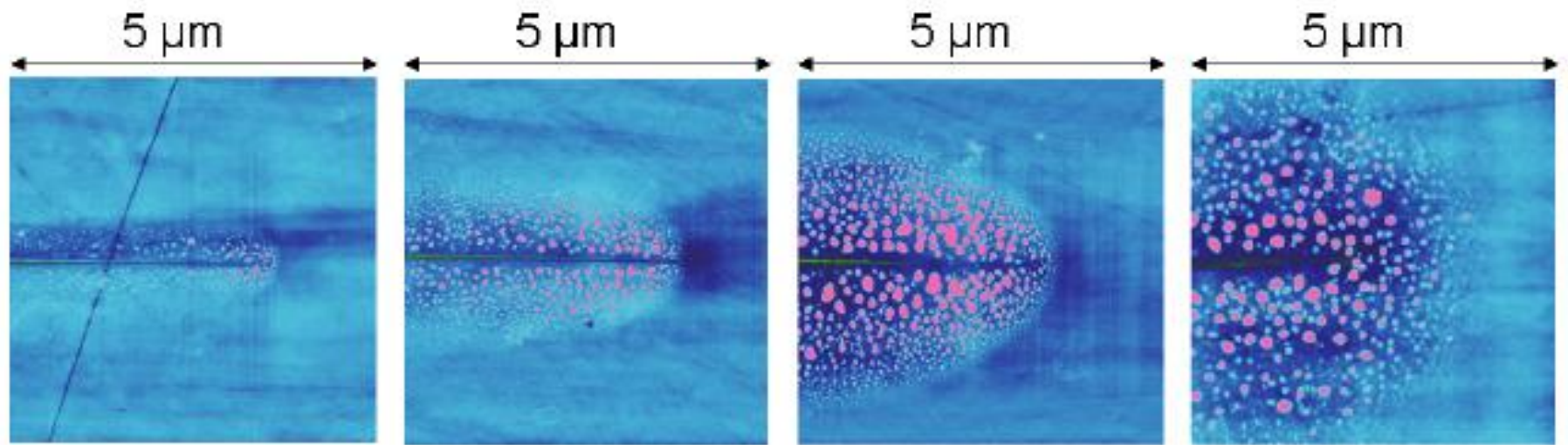
Change in crack tip geometry due to corrosion: (a) Flaw sharpening for stresses greater than the fatigue limit; (b) Constant flaw sharpness for stresses equal to the fatigue stress; (c) Flaw blunting for stresses below the fatigue limit.

.T.-J. Chuang and E.R. Fuller, Jr. "Extended Charles-Hillig Theory for Stress Corrosion Cracking of Glass," *J. Am. Ceram. Soc.* 75[3] 540-45 (1992).

W.B. Hillig, "Model of effect of environmental attack on flaw growth kinetics of glass," *Int. J.*

*Fract.* 143 219-230 (2007)

# AFM detects significant morphological changes around the crack-tip in aged samples



$$K_I = 0.422 \text{ MPa}\cdot\text{m}^{1/2}$$
$$v = 3 \text{ nm}\cdot\text{s}^{-1}$$

$$K_I = 0.42 \text{ MPa}\cdot\text{m}^{1/2}$$
$$v = 2.2 \text{ nm}\cdot\text{s}^{-1}$$

$$K_I = 0.415 \text{ MPa}\cdot\text{m}^{1/2}$$
$$v = 1.5 \text{ nm}\cdot\text{s}^{-1}$$

$$K_I = 0.38 \text{ MPa}\cdot\text{m}^{1/2}$$
$$v = 0.5 \text{ nm}\cdot\text{s}^{-1}$$

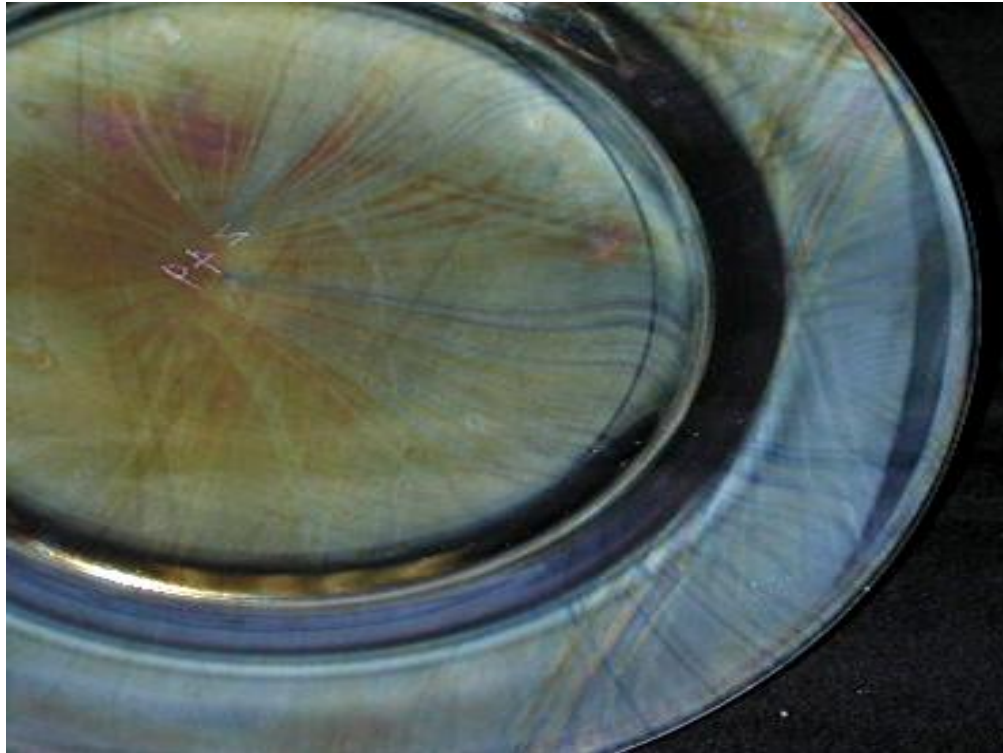
SLS glass, 45% RH

Célarié, et al., JNCS (2007)

- Formation of alkali-rich regions modeled by  $\text{Na}^+$ - $\text{H}_3\text{O}^+$  inter-diffusion
- Alkali depletion from crack-tip region leads to stress-relaxation
  - Crack extension threshold



# The 'corrosion reactions' at a crack tip are similar to those that occur at glass surfaces



From Prof. Jain:

A clear glass plate is made of soda lime silicate glass by pressing molten gob. It shows the following undesirable pattern upon washing in a dishwasher. Discuss this problem with your roommate. Then develop a collaborative research program to characterize and solve the problem. The proposal should be about 1500 words long.

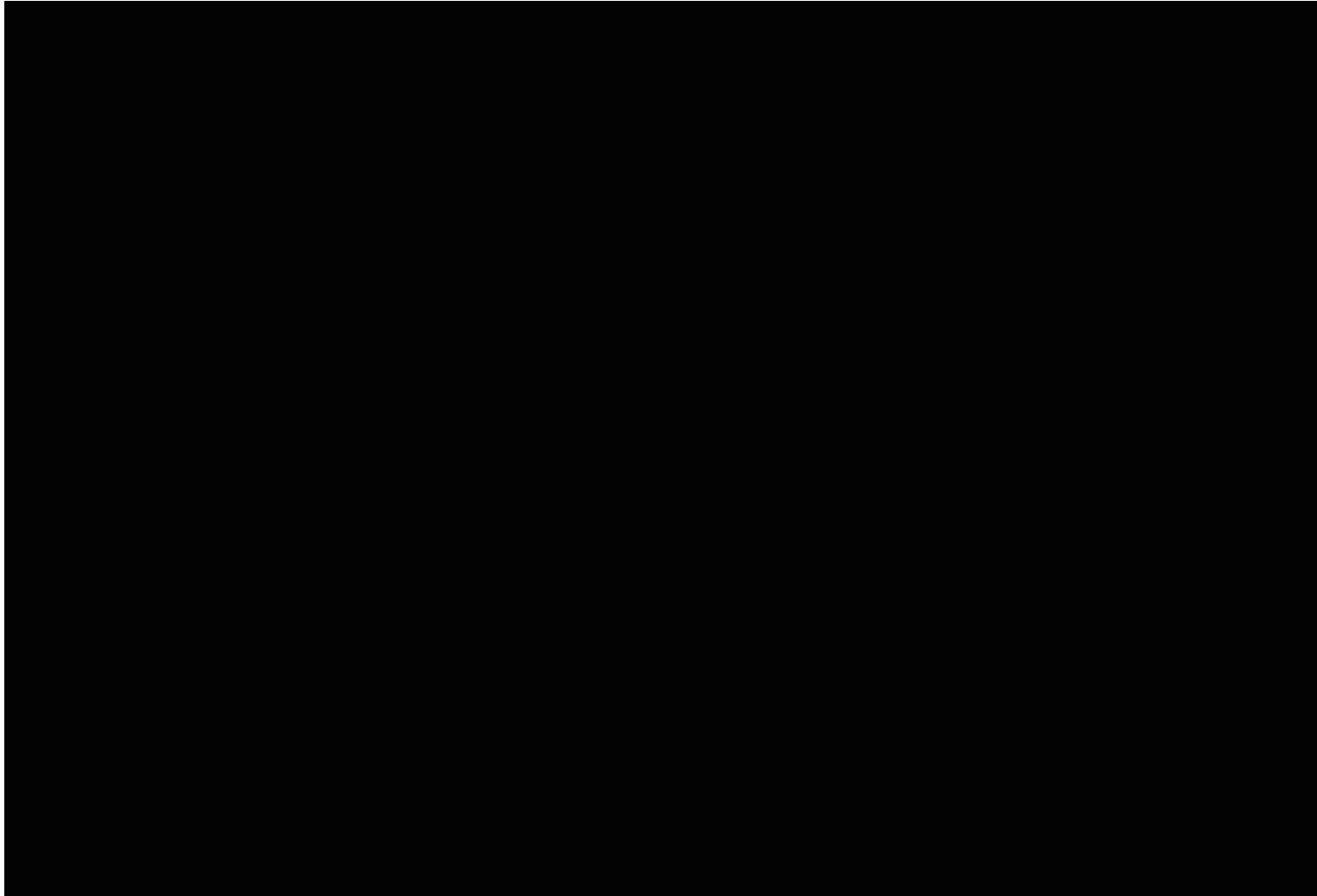
# Water plays many roles at a crack-tip

1. Chemical attack on strained bonds to extend flaws
2. Water films adsorbed on crack surfaces
3. Capillary condensation at the crack tip
4. Water diffusion into the glass network, changing elastic properties
5. Inter-diffusion with alkali ions, changing pH and attacking glass

Strengthening- What can we do to make glass stronger (or more reliable)?

- Polished surfaces
- Surface dealkalization
- Protective coatings
- Relaxation of residual stresses (annealing)
- Reduction of expansion coefficients (thermal shock)
- Thermal tempering
- Chemical tempering
- Modified compositions:
  - Increasing elastic modulus and/or surface energy
  - Reducing stress-corrosion
  - Propagation threshold
  - Crack healing

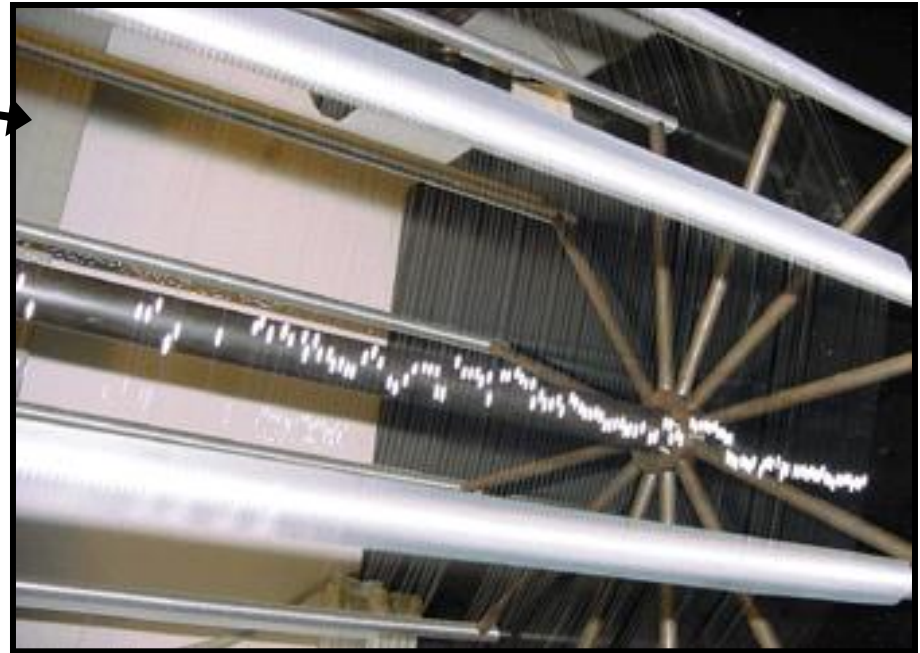
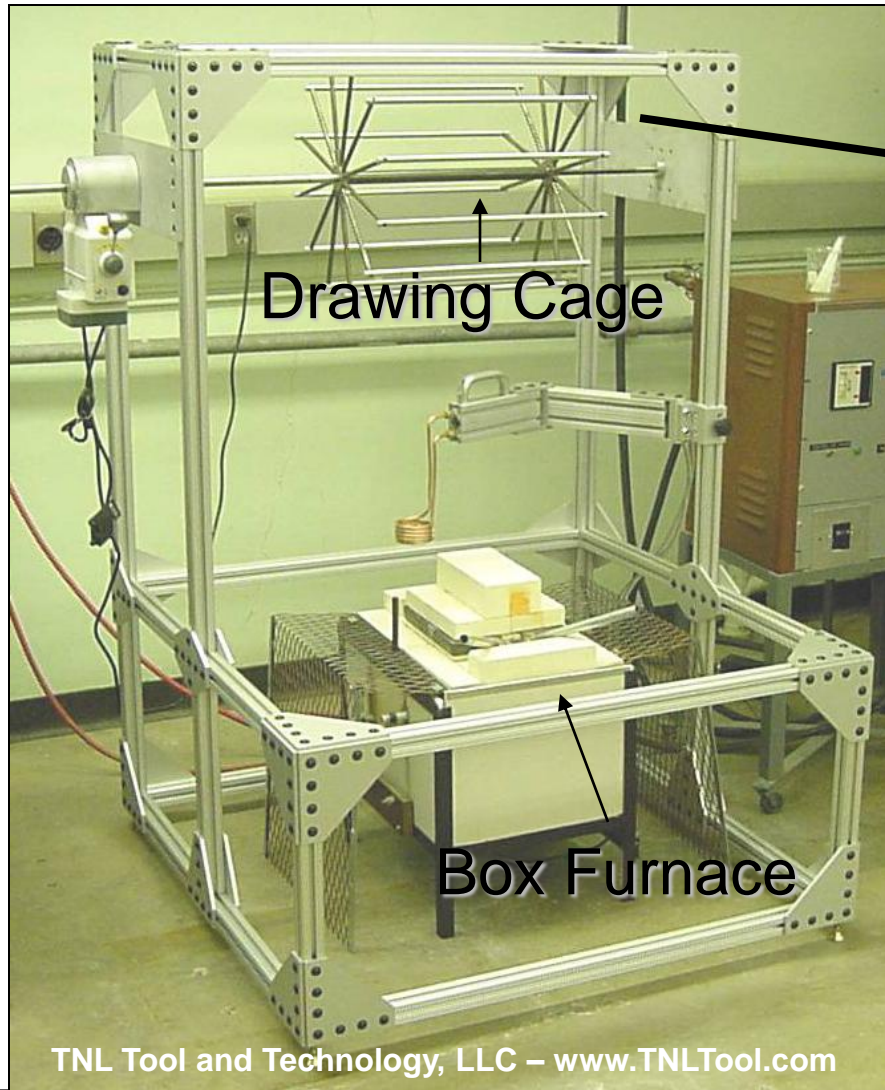
# Annealed vs. chemically tempered glass



From Jill Glass, Sandia National Labs

# Two-point bend studies of the failure characteristics of silicate glasses

# We have produced and tested pristine fibers

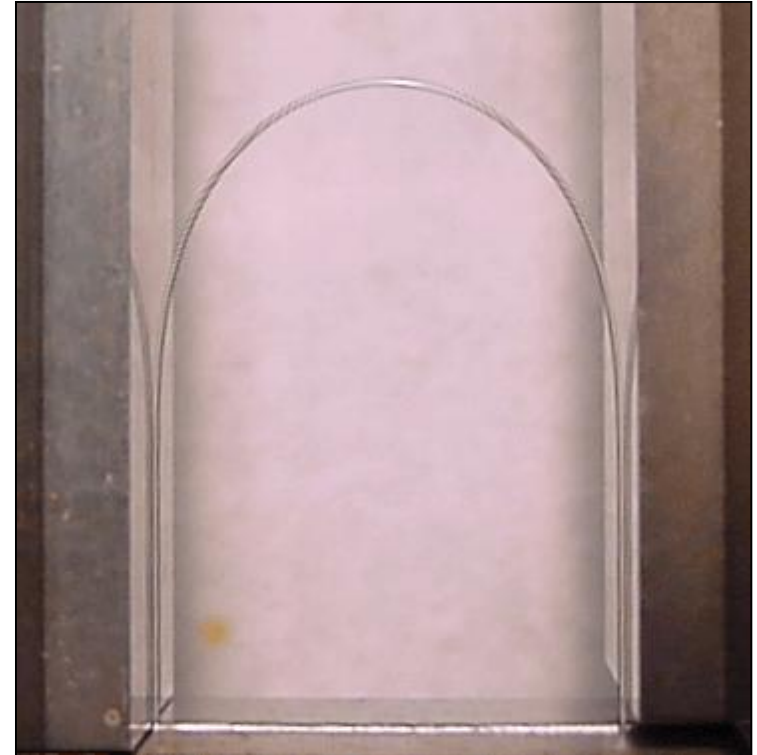


- “Pristine” 10 cm length fibers
- Fiber diameters  $\sim 125$   $\mu\text{m}$ .
- Fibers can be tested immediately.

# We have measured failure strains using a Two-Point Bend technique



TNL Tool and Technology, LLC – [www.TNLTool.com](http://www.TNLTool.com)

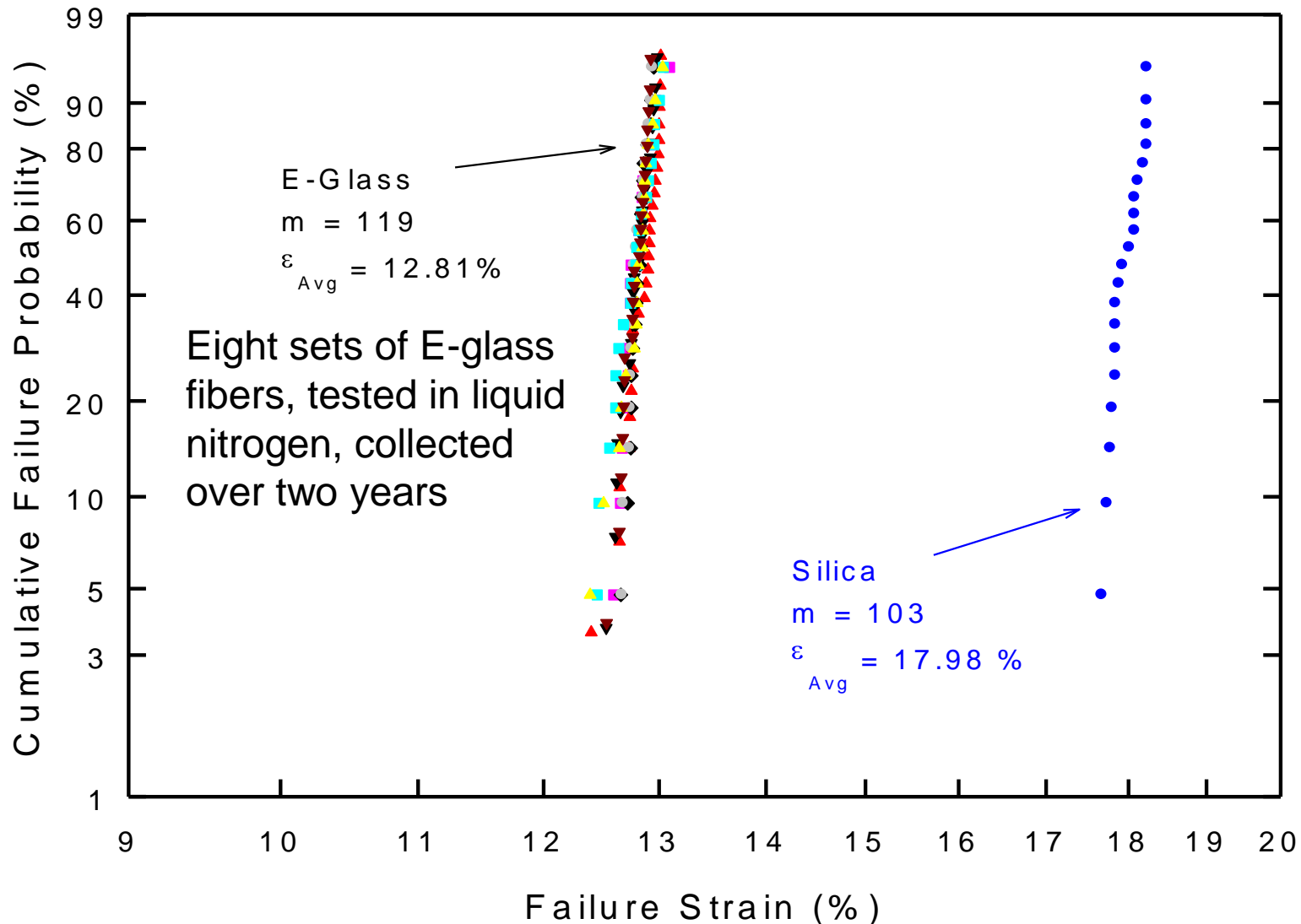


$$\varepsilon_f = \left( \frac{1.198 \cdot d}{D - d} \right)$$

\*M.J. Matthewson, C.R. Kurkjian, S.T. Gulati, *J. Am. Cer. Soc.*, **69**, 815 (1986).



# The inert failure strain measurements are reproducible

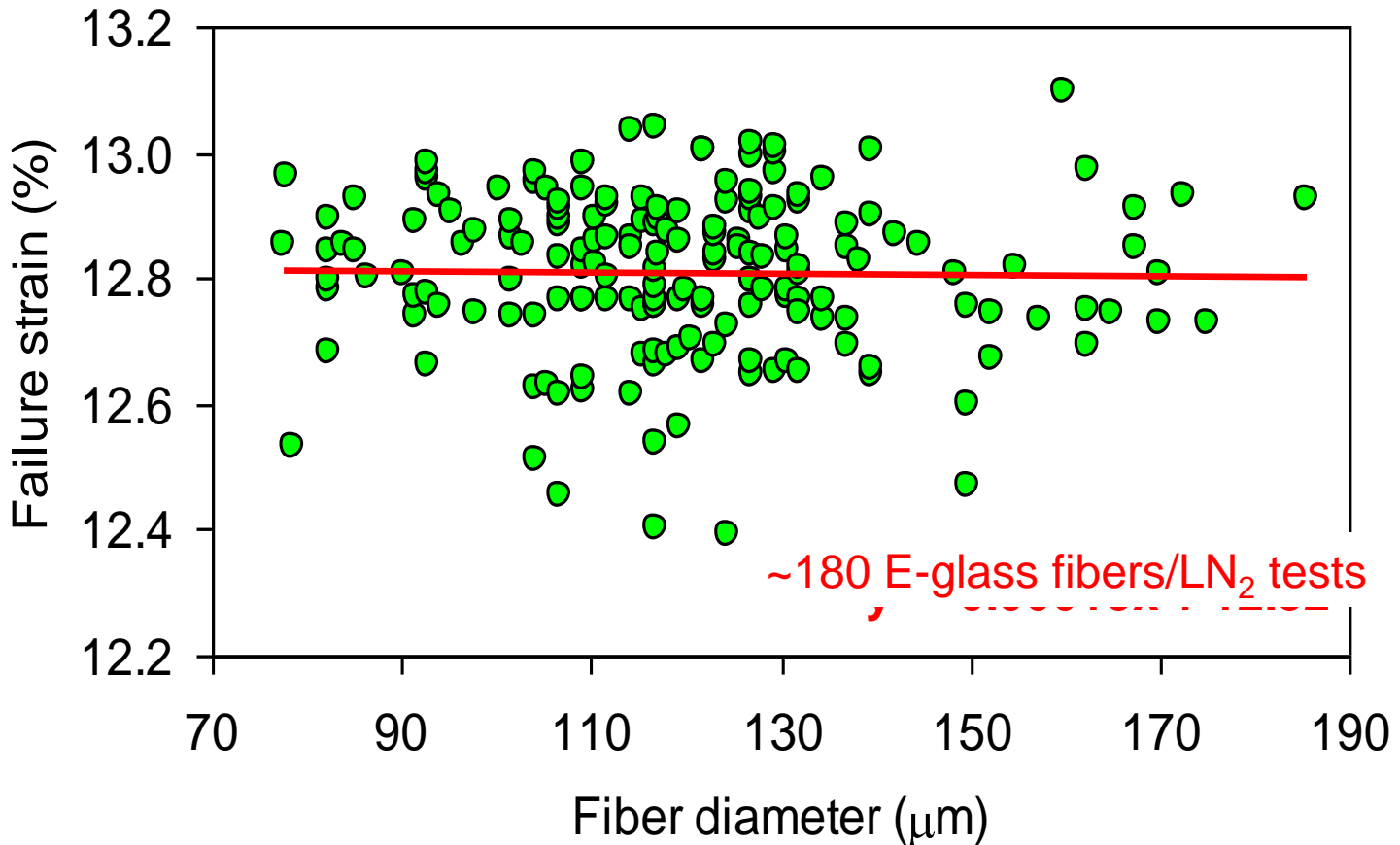


# The inert failure strain measurements are intrinsic

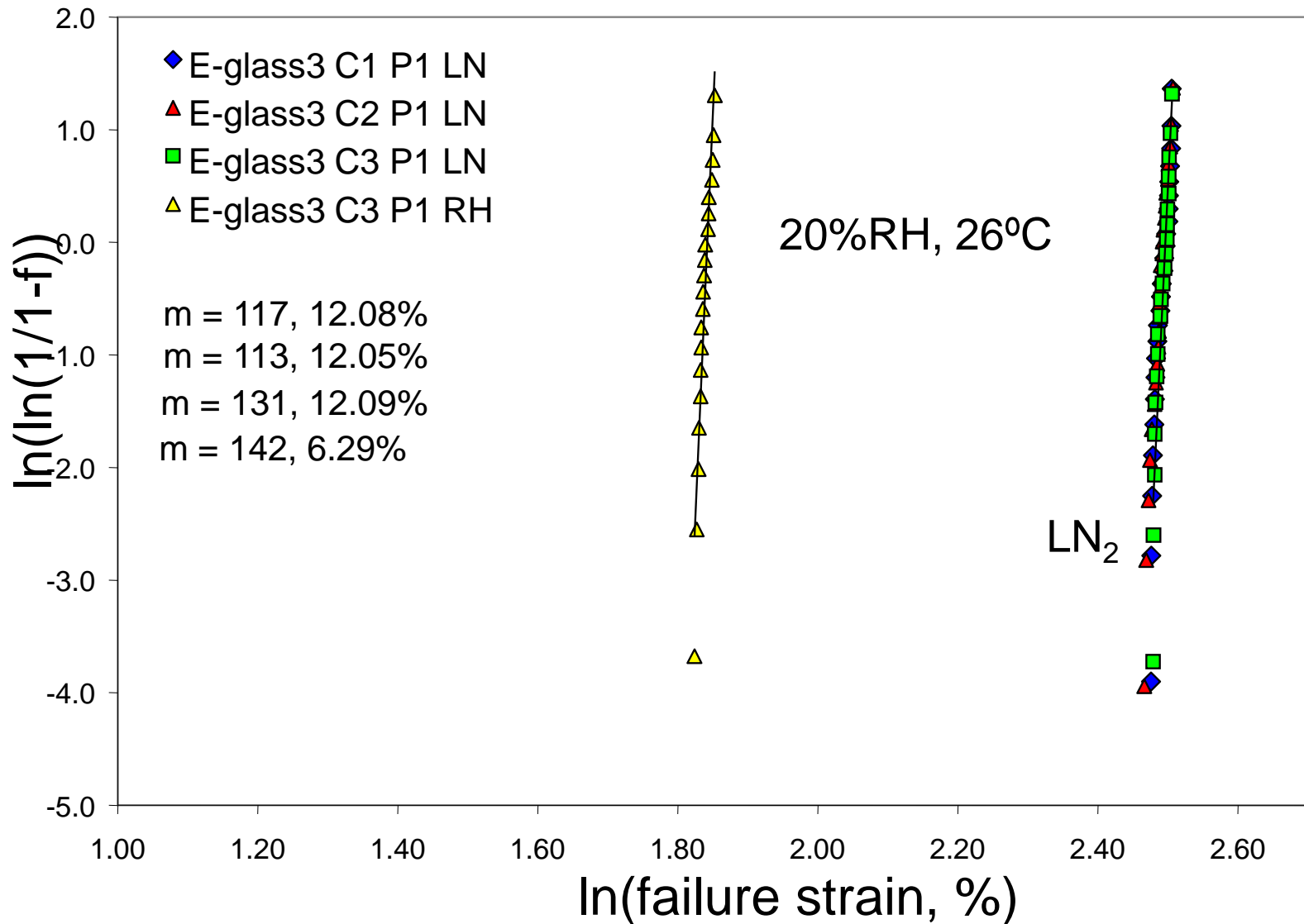
## Criteria for 'intrinsic' failure properties\*

- Narrow failure distributions:  $s(\text{failure}) < s(\text{fiber diameter})$
- Failure property (strength, strain) independent of diameter

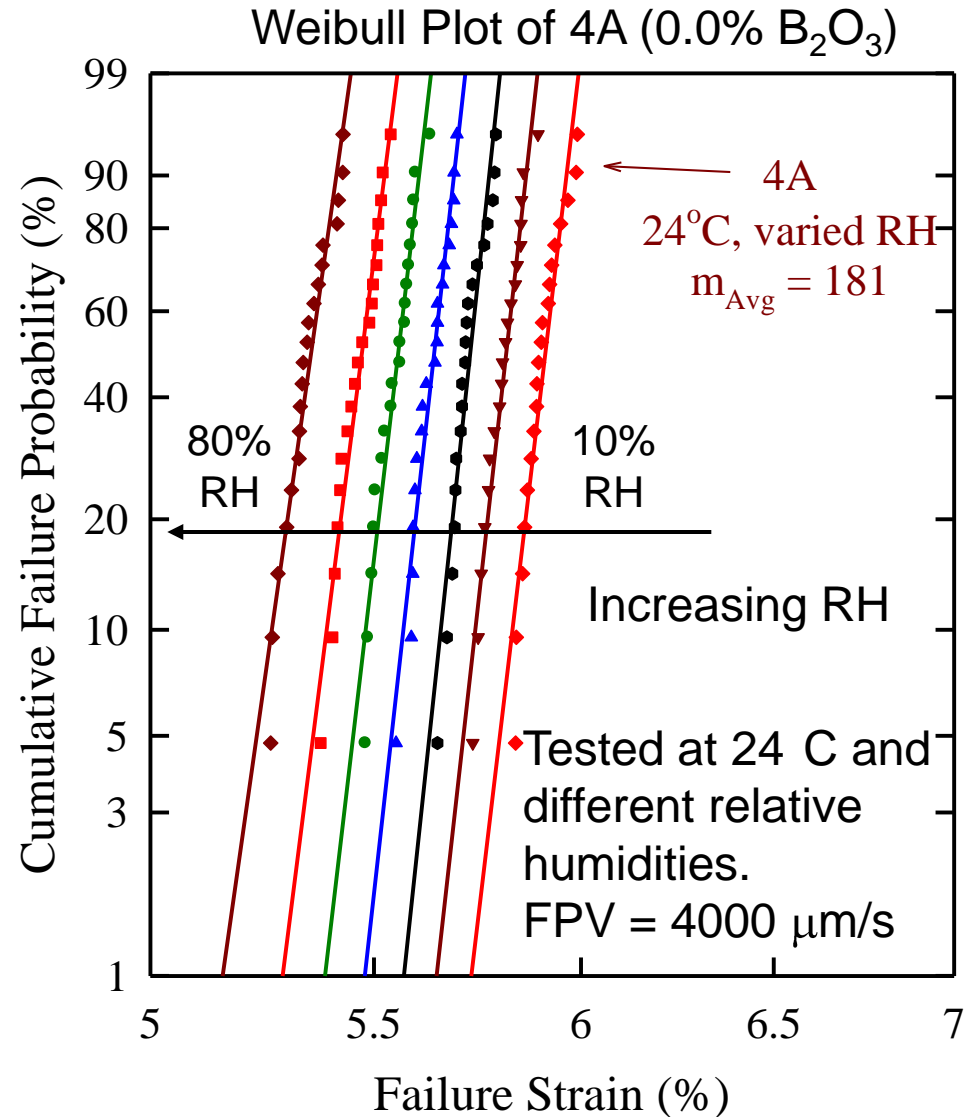
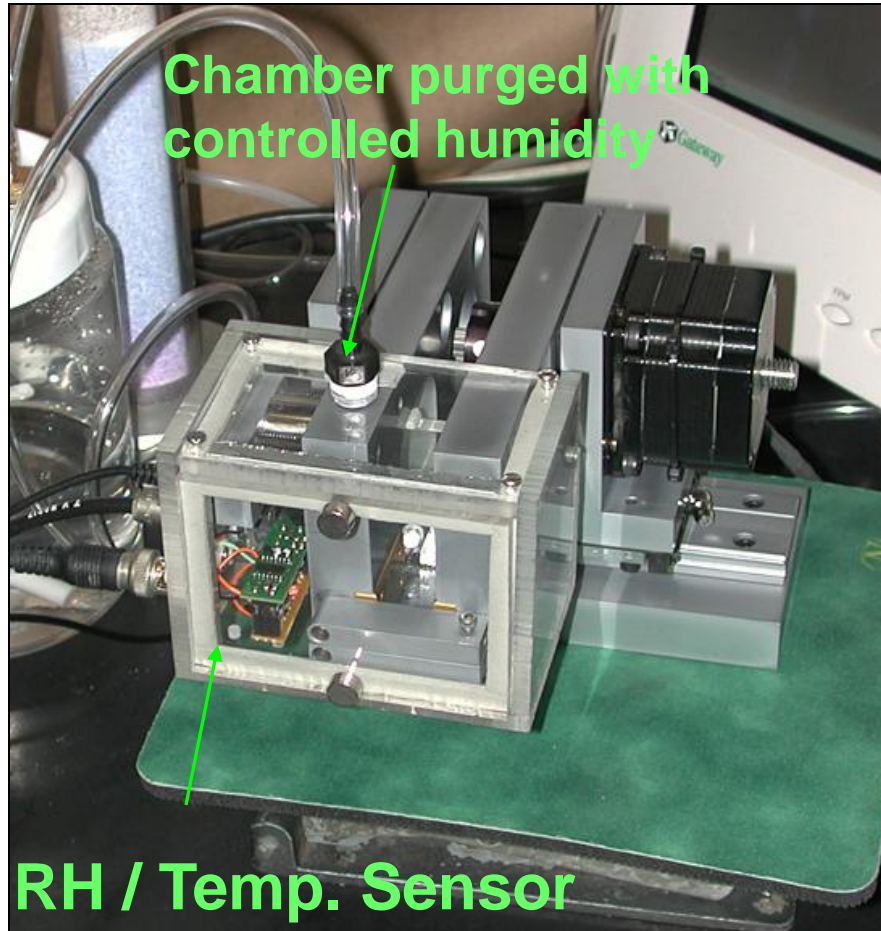
\*Gupta and Kurkjian, JNCS 351 (2005) 2343.



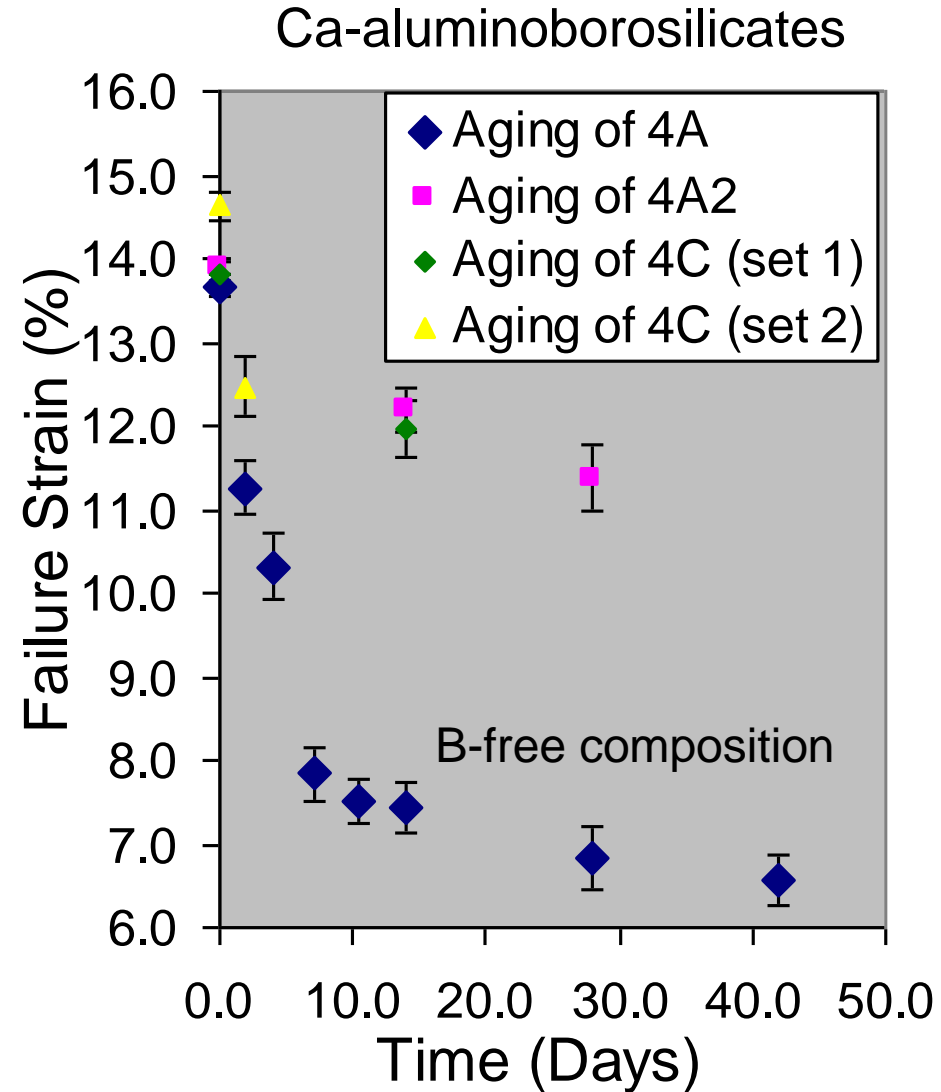
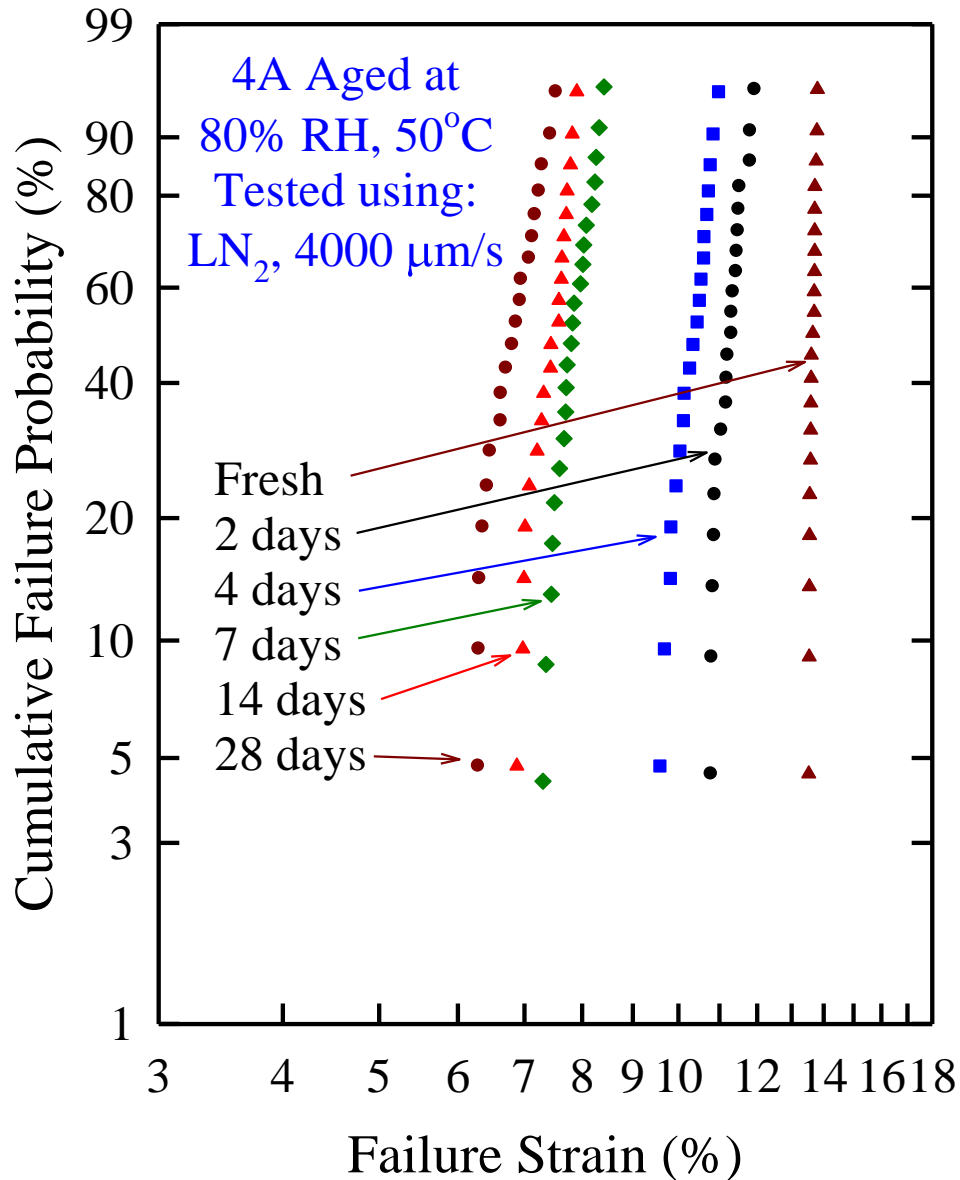
# Fibers fail at lower strains in ambient conditions



# Fatigue effects can be characterized



# Aging effects have also been characterized

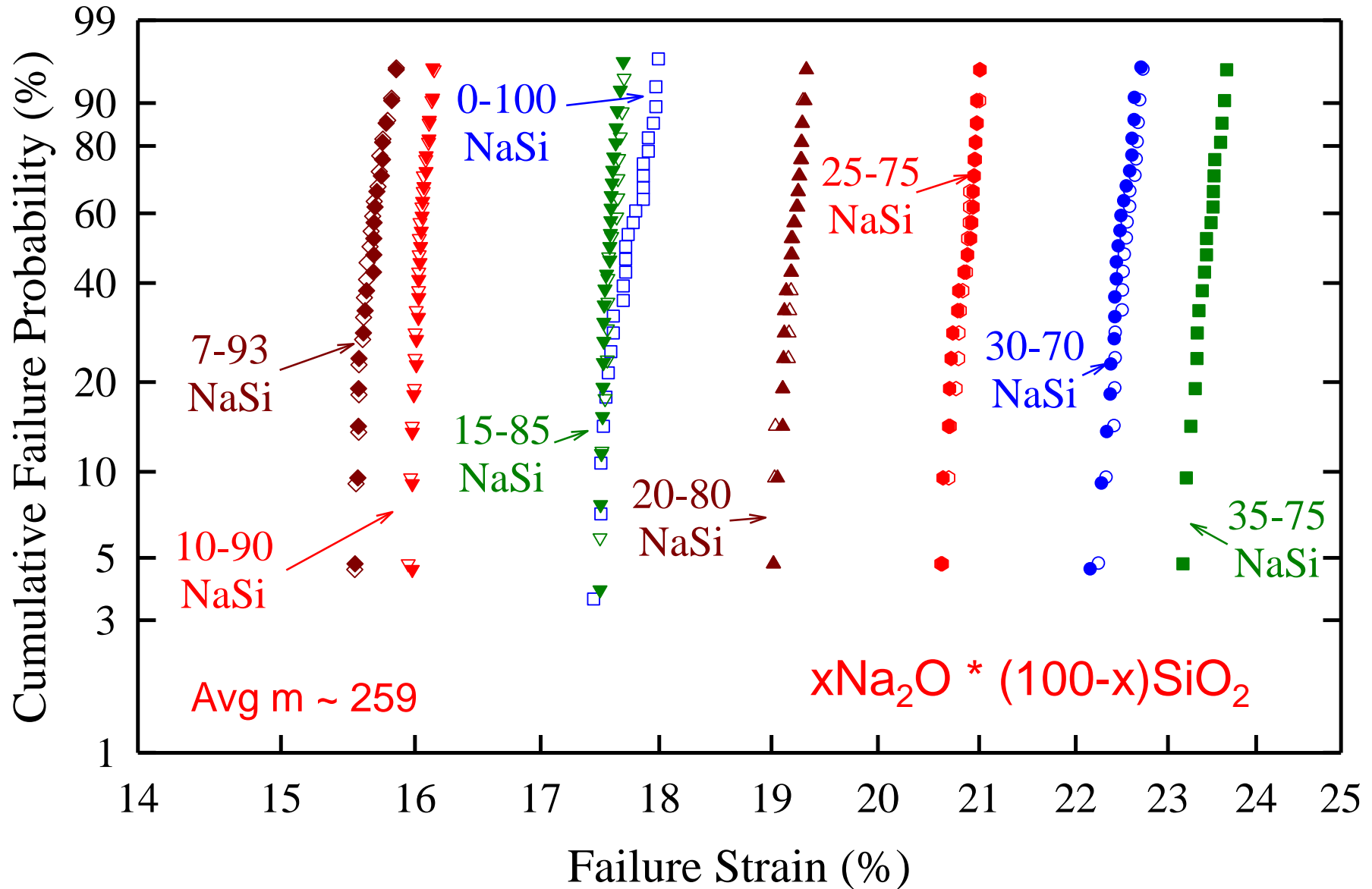


What might inert 2pb studies tell us about the failure characteristics of silicate glasses?

# Compositions Studied

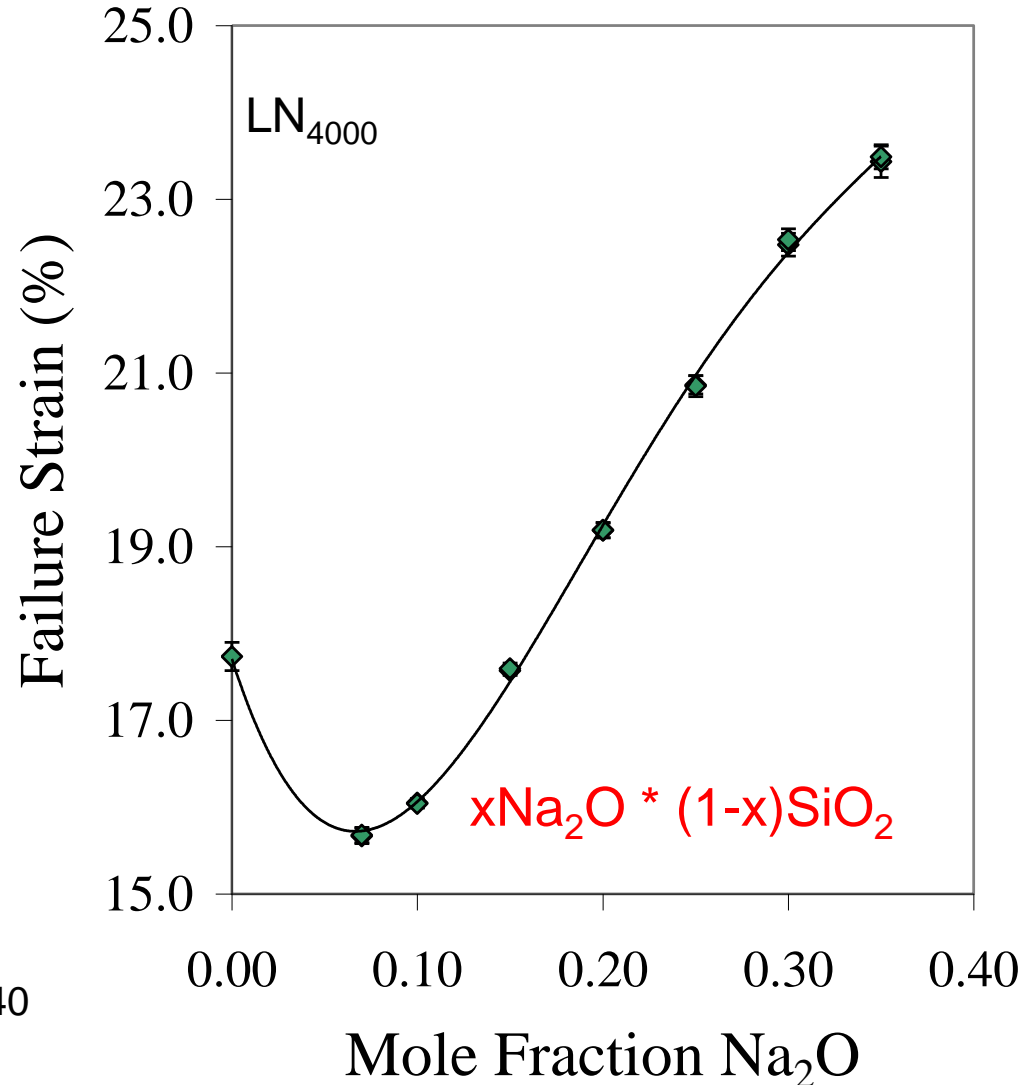
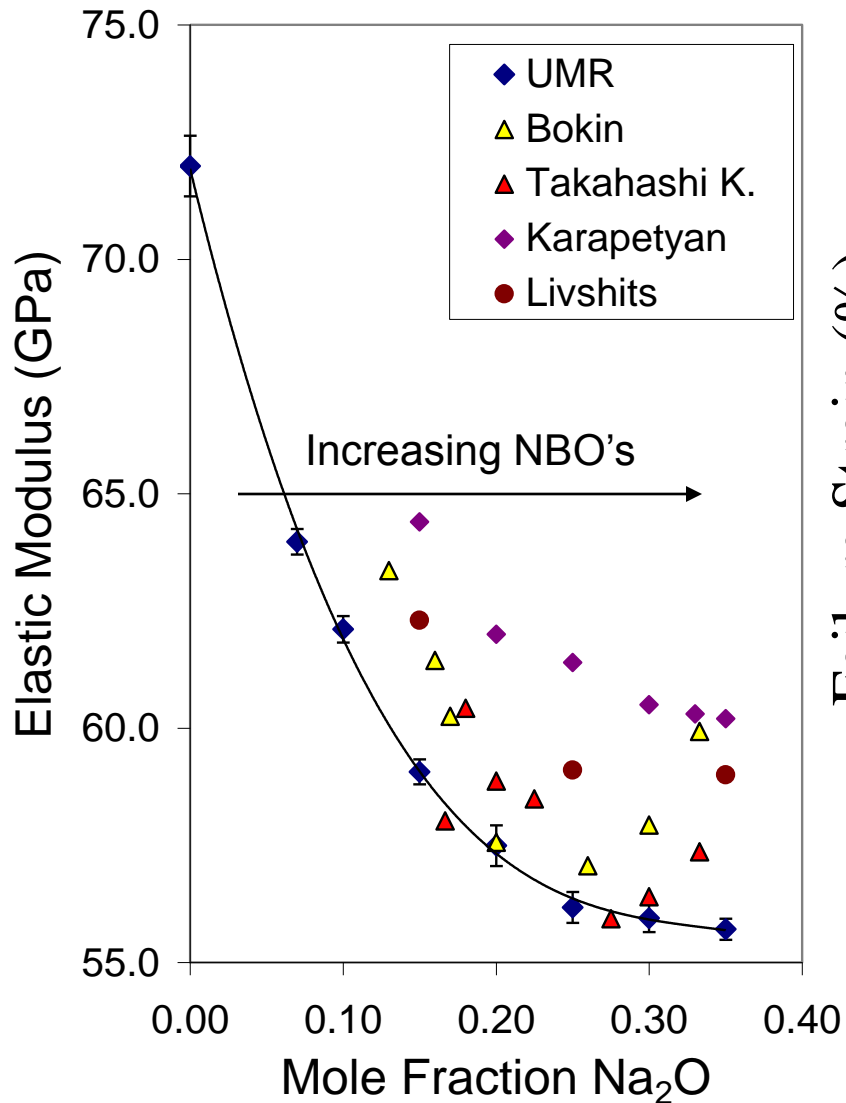
- $x\text{Na}_2\text{O} * (100-x)\text{SiO}_2$ 
  - $x = 0, 7, 10, 15, 20, 25, 30, 35$
- $x\text{K}_2\text{O} * (100-x)\text{SiO}_2$ 
  - $x = 0, 4.5, 7, 10, 15, 20, 25$
- $25\text{Na}_2\text{O} * x\text{Al}_2\text{O}_3 * (75-x)\text{SiO}_2$ 
  - $x = 0, 5, 10, 15, 20, 25, 30, 32.5$
- $x\text{Na}_2\text{O} * y\text{CaO} * (100-x-y)\text{SiO}_2$ 
  - *Compositions studied by Ito, et al.*

# Na-silicate inert failure strains depend on composition

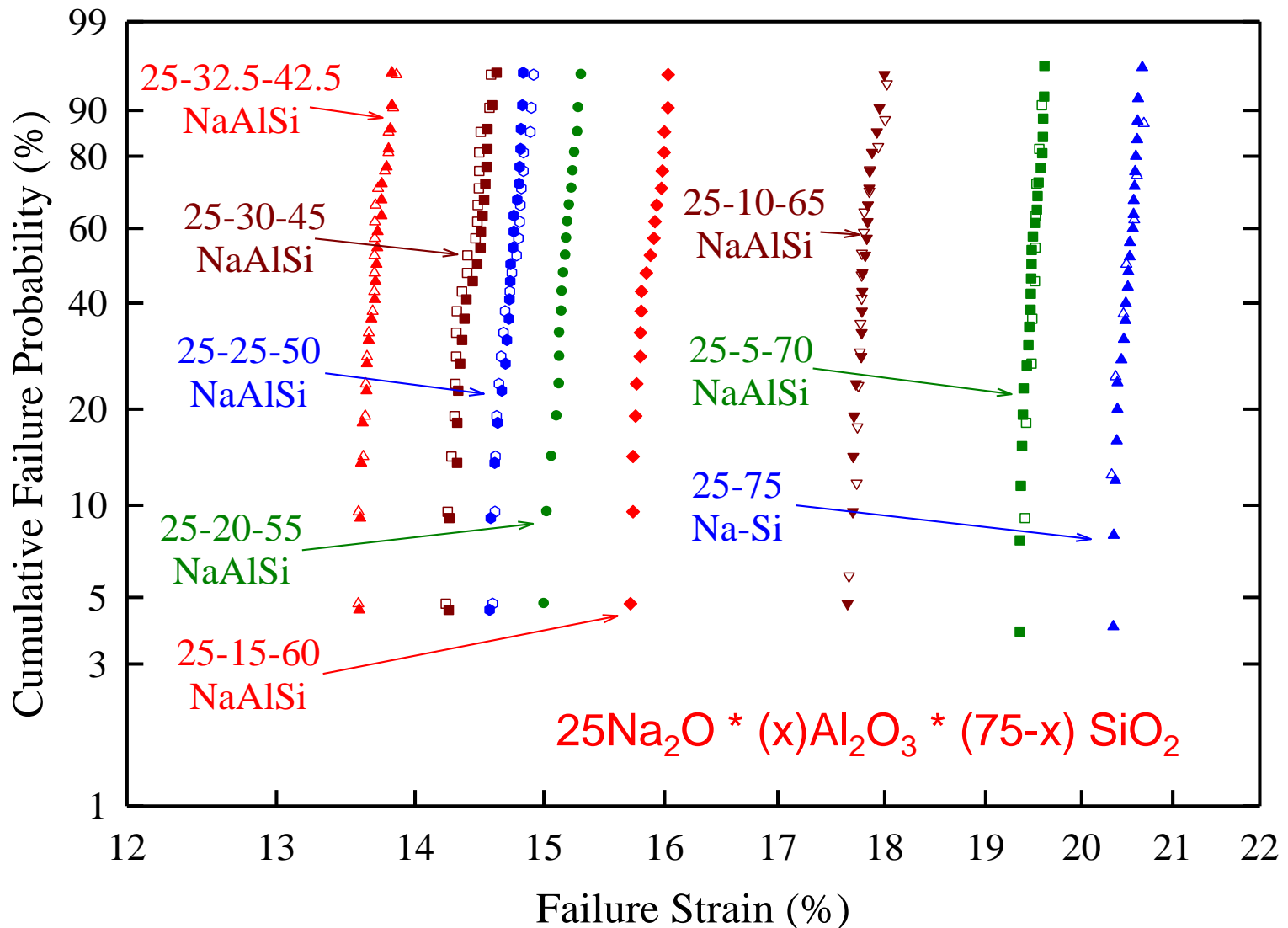




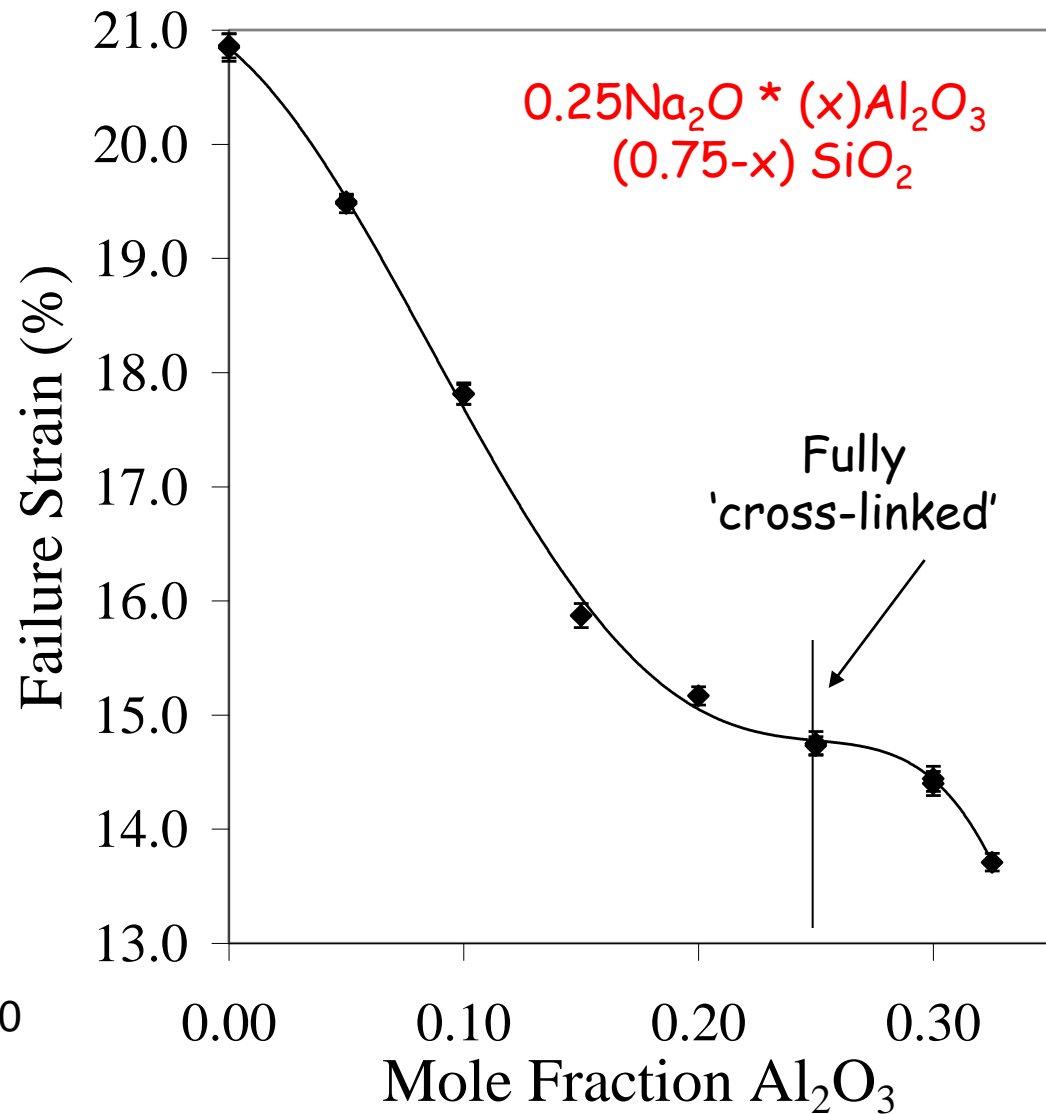
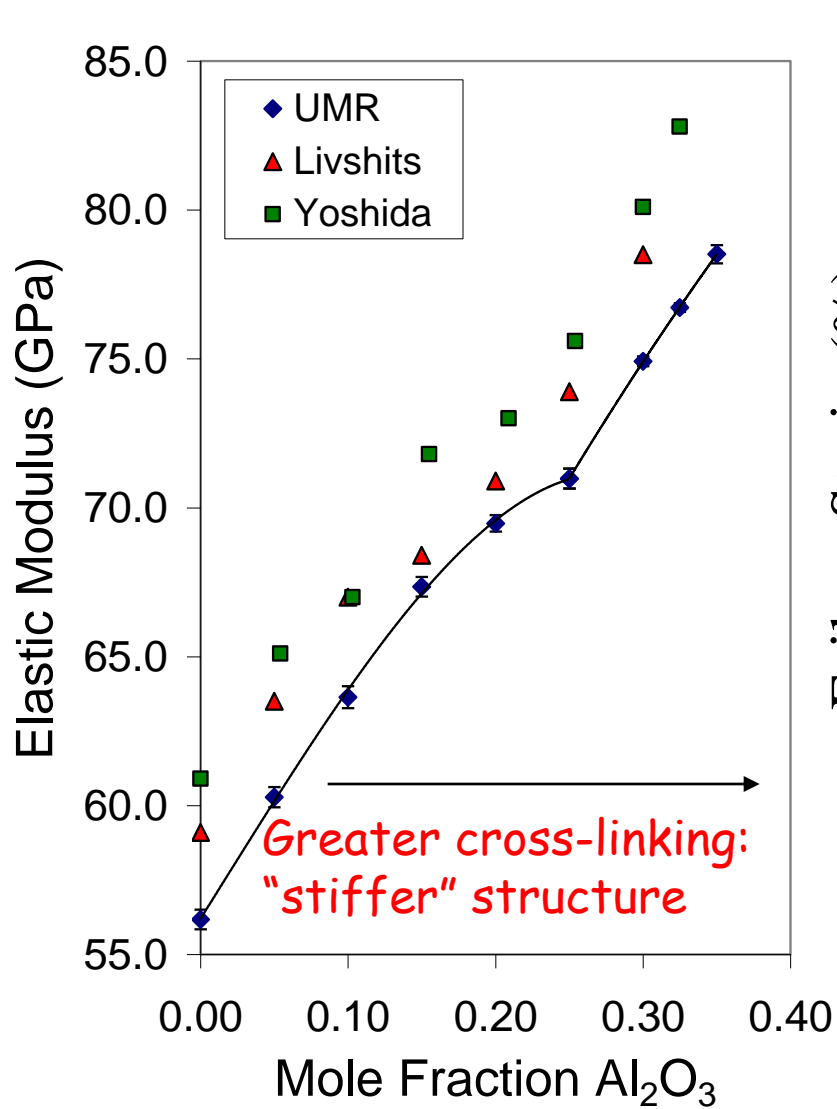
# Sodium silicate properties



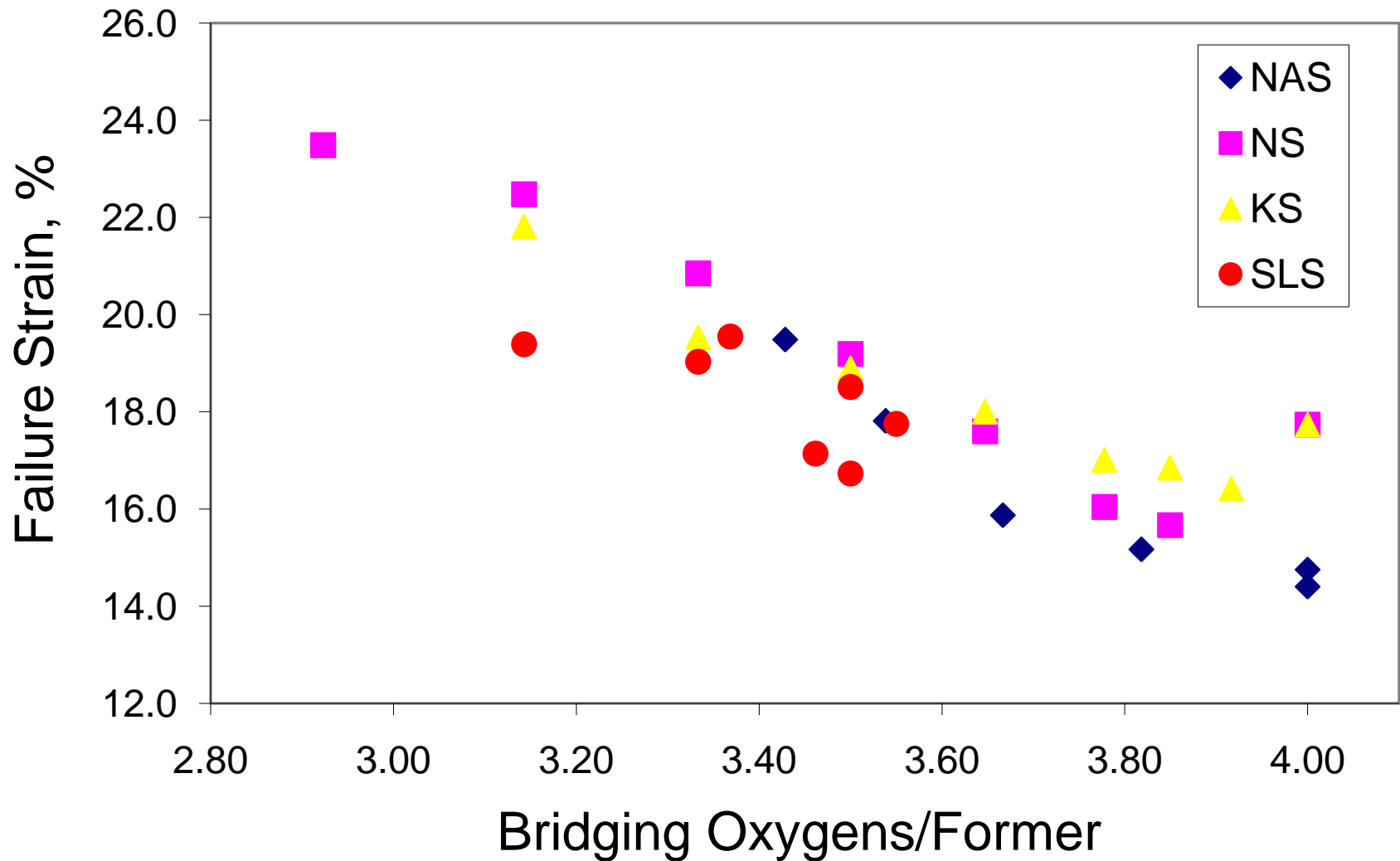
# Na-Al-silicate inert failure strains depend on composition



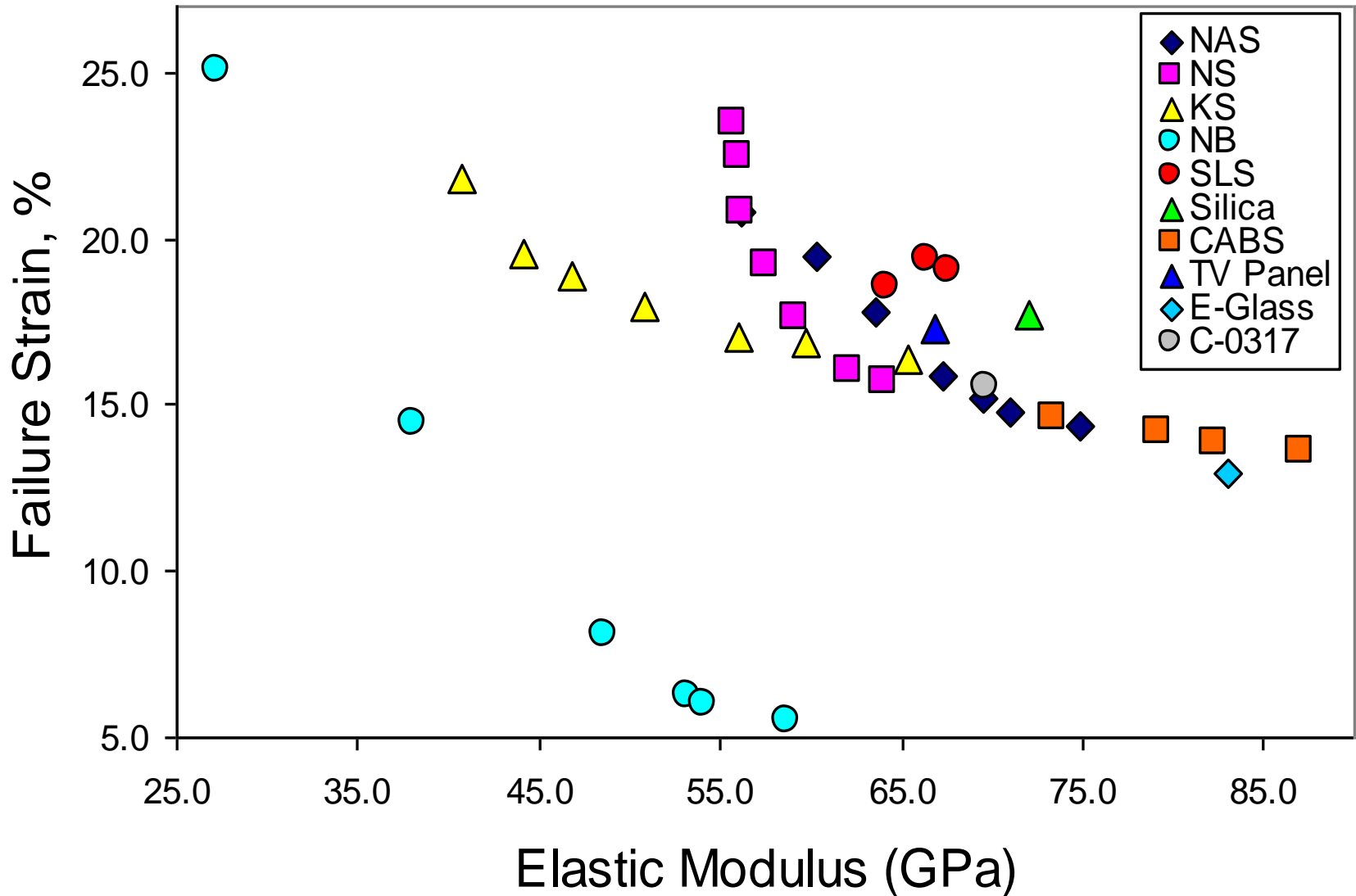
# Na-Al-silicate properties depend on structure



# Inert failure strain decreases for 'cross-linked' structures



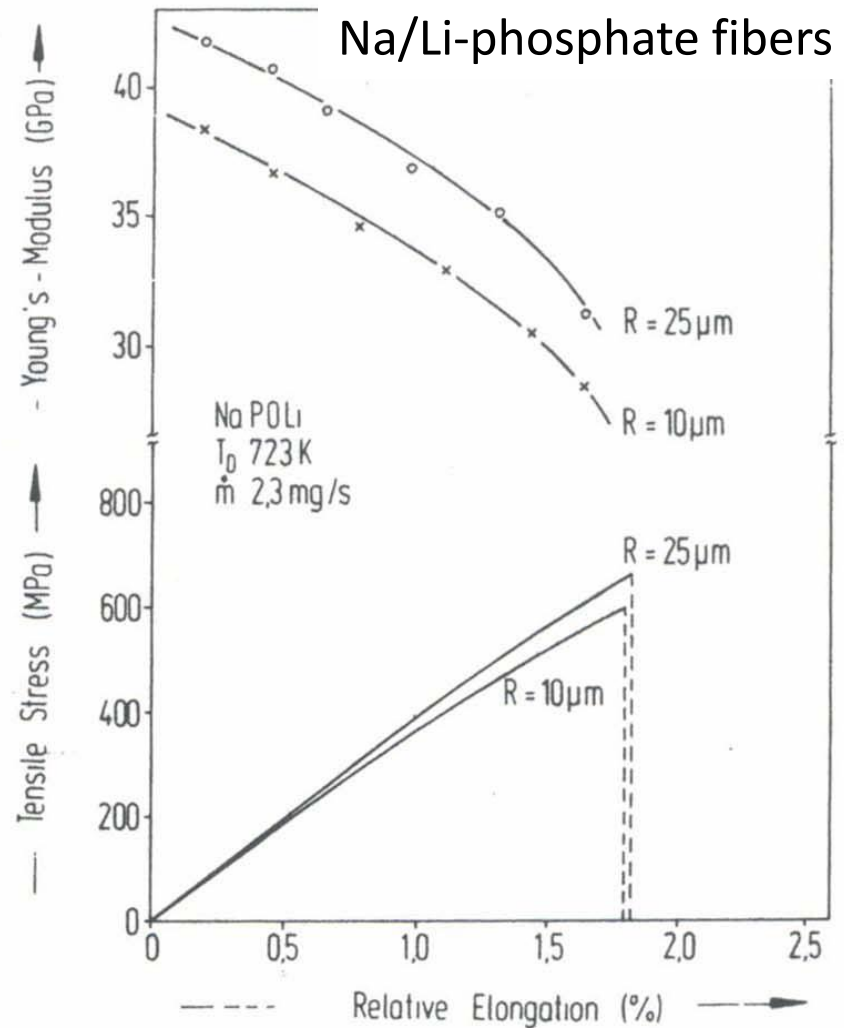
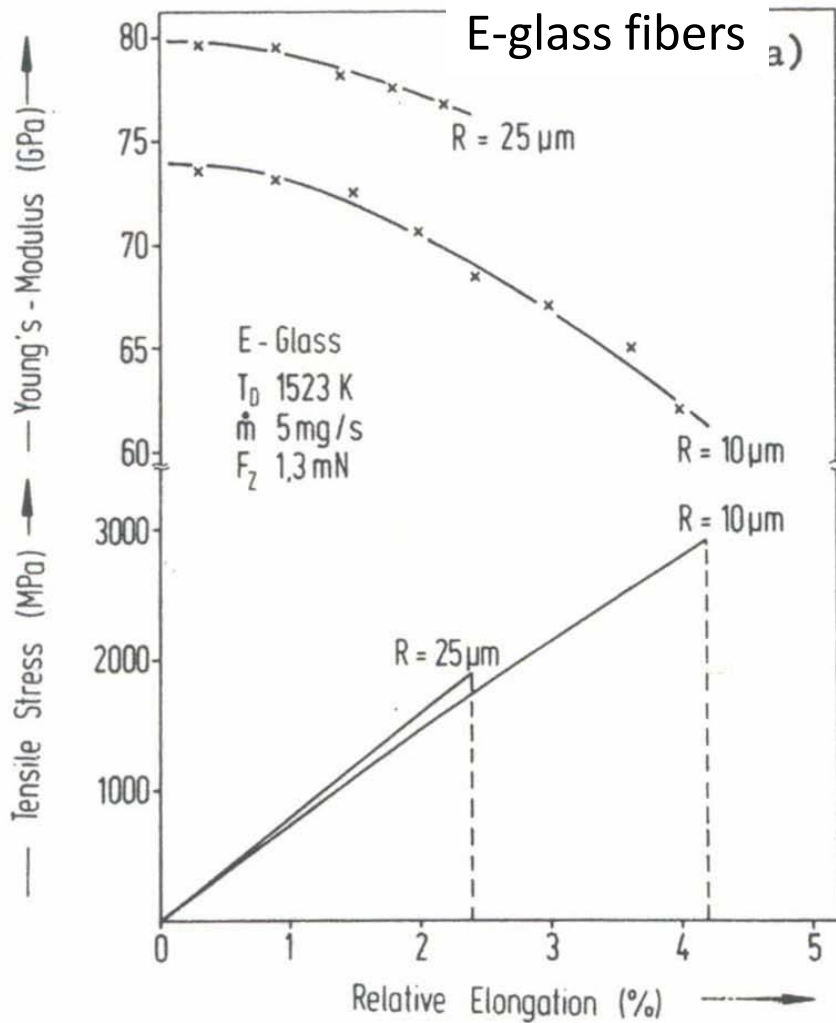
# Failure strain depends on elastic modulus



Do these measurements provide information  
about the strength of glass?

...depends on what we know about  
the elastic modulus

# Elastic modulus depends on strain

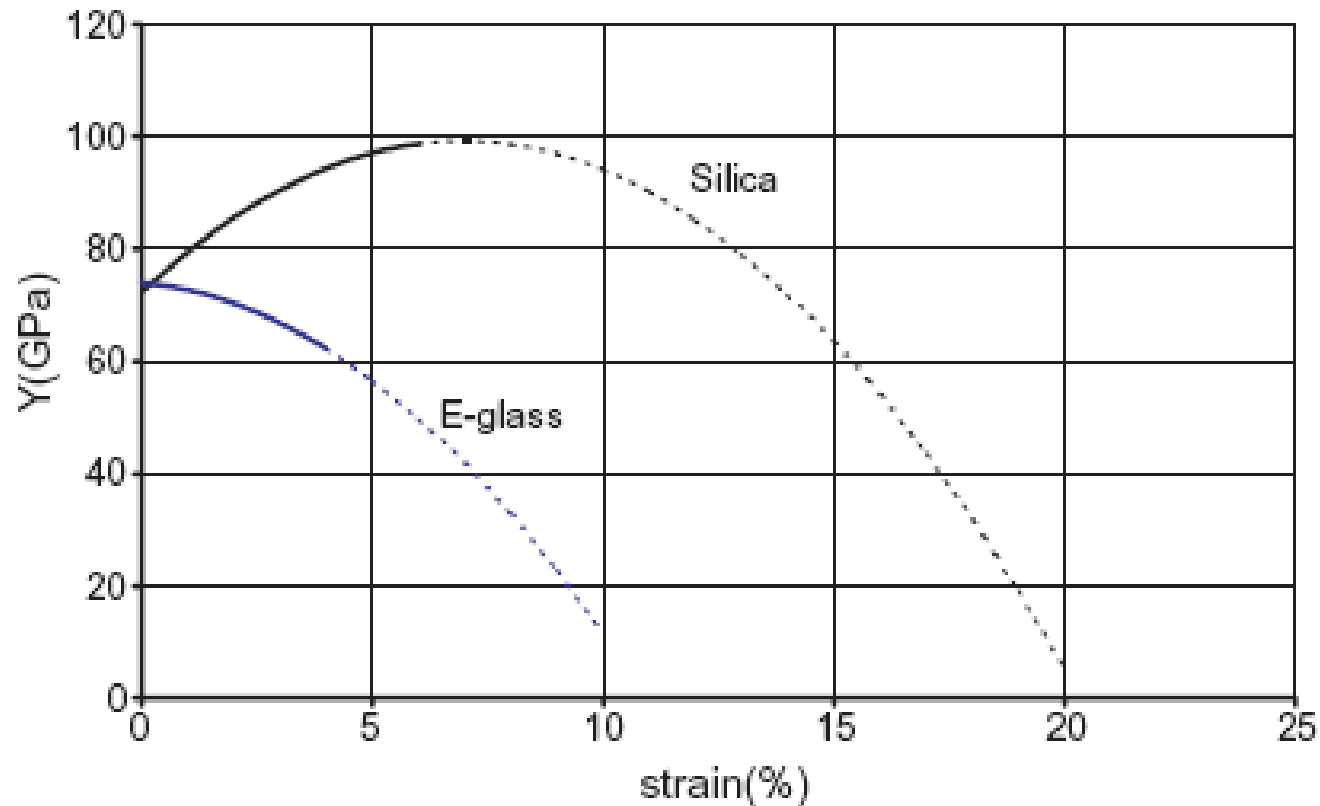


Bruckner, *Strength of Inorg. Glass* 1986

# Strain dependence of modulus has been modeled

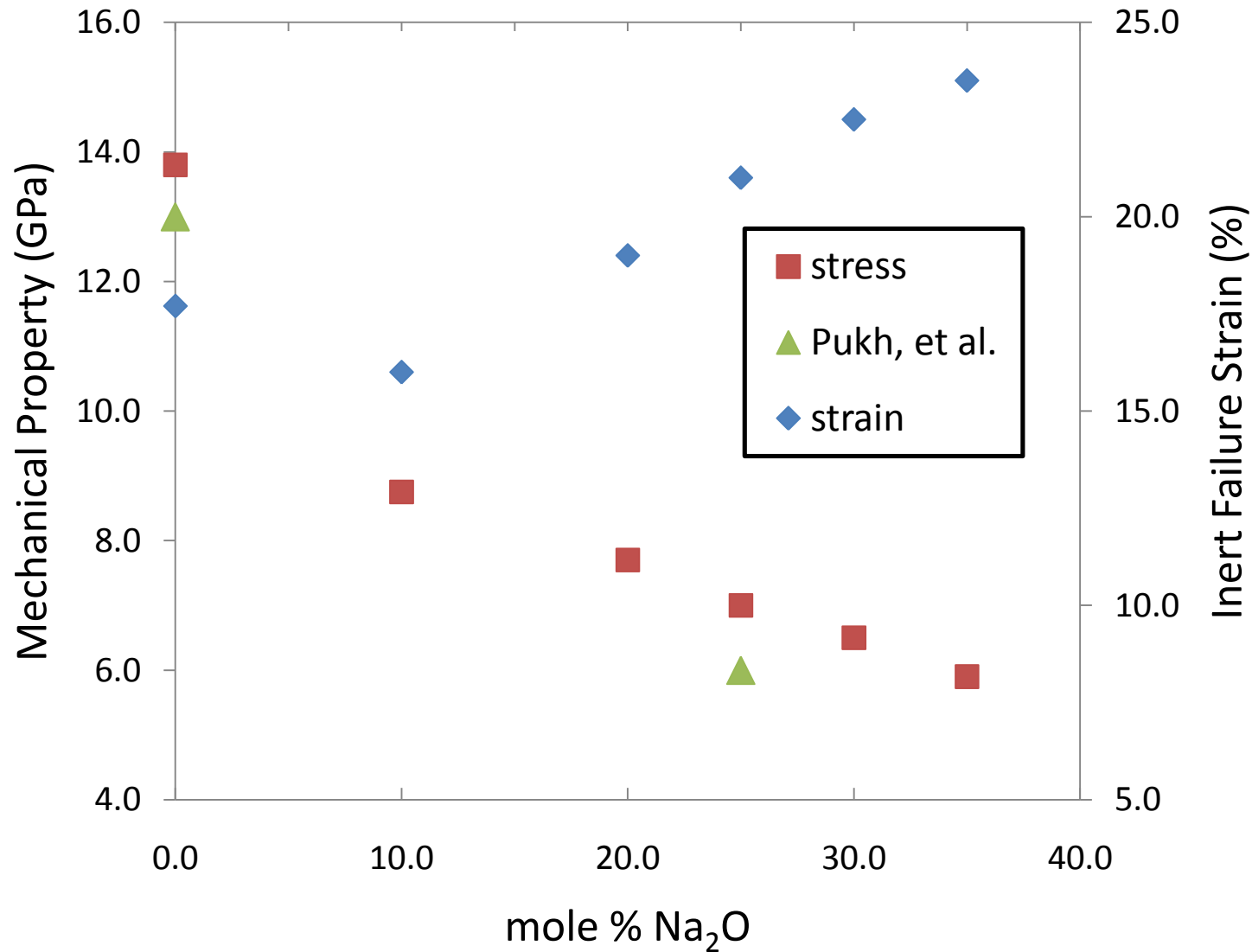
Converting failure strain to failure stress requires knowledge of  $Y(\varepsilon)$ : Gupta and Kurkjian, JNCS 351 (2005) 2343

$$Y(\varepsilon) = Y_0 + Y_1\varepsilon + (Y_2/2)\varepsilon^2 ; \sigma_f = \varepsilon_f[(2/3)Y_0 + (Y_1/6)\varepsilon_f]$$





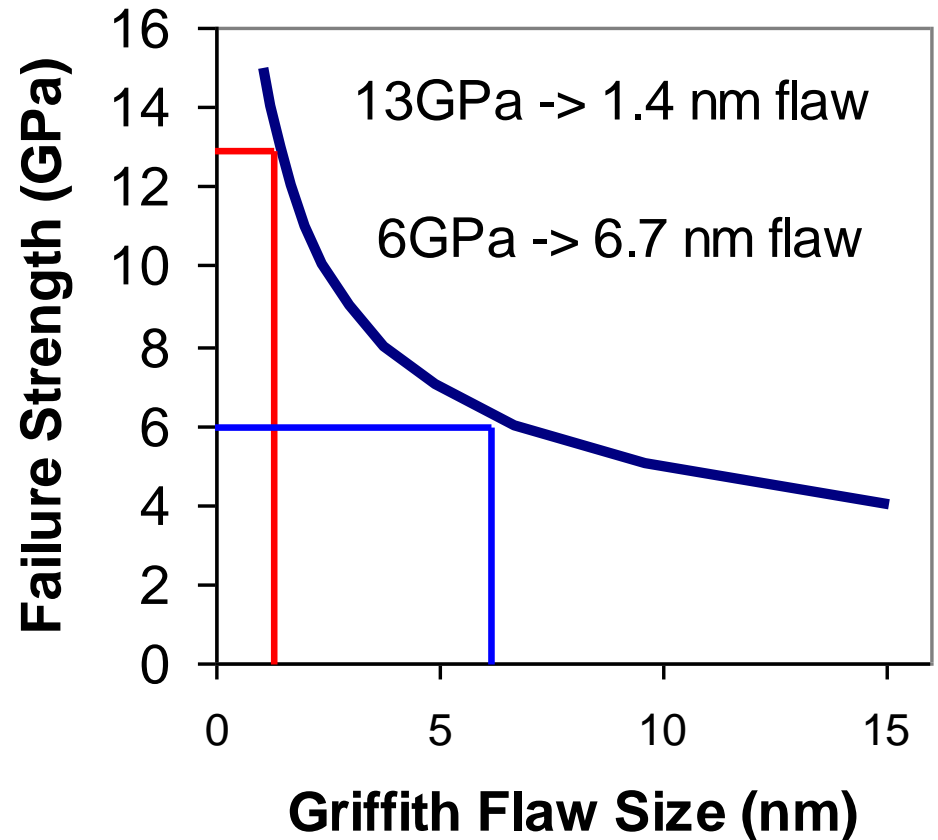
# Failure strengths can be calculated if $\gamma(\epsilon)$ is known



# What role is played by 'critical flaws'?

- There are no apparent surface heterogeneities.
- If Griffith flaws are responsible for low strengths, they will be in the range of 2-7 nm, depending on the flaw (stress concentrator) geometry.

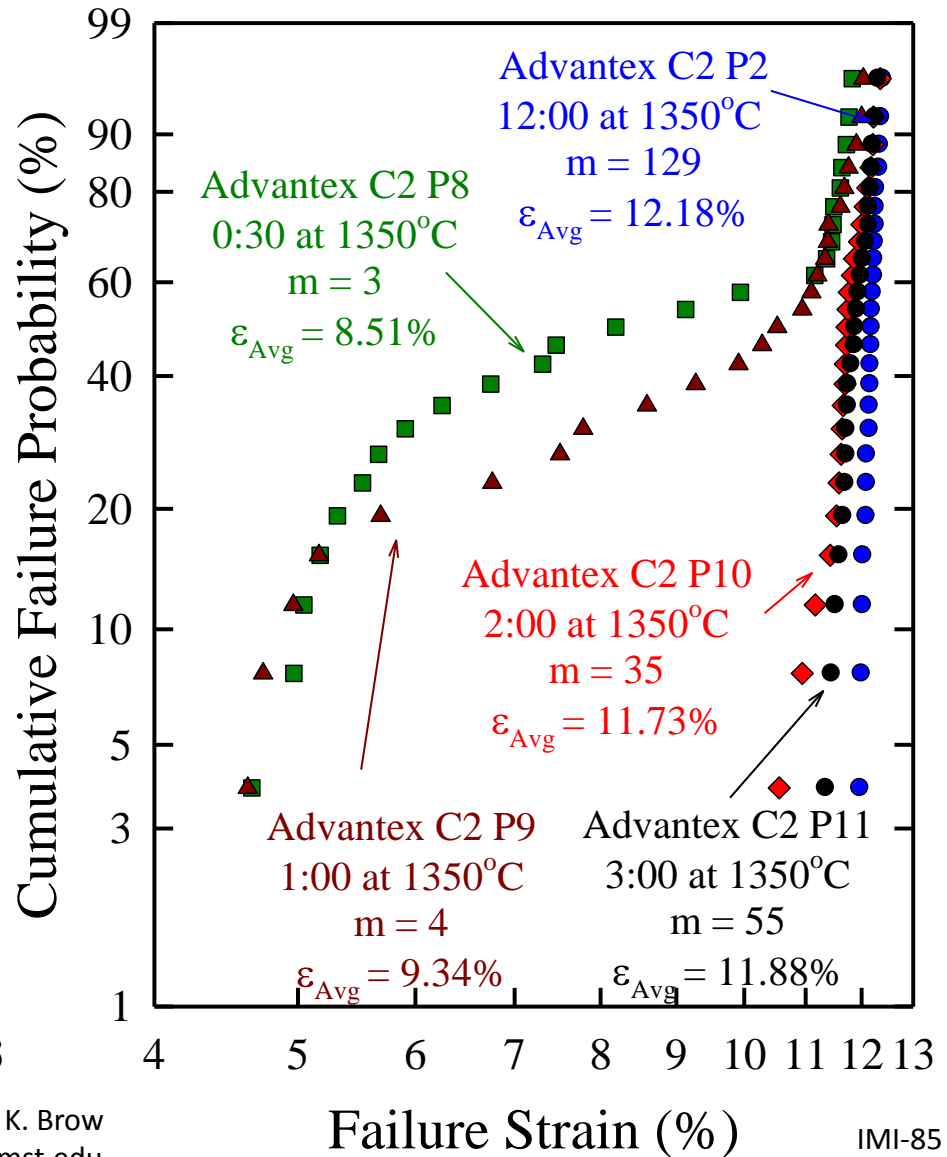
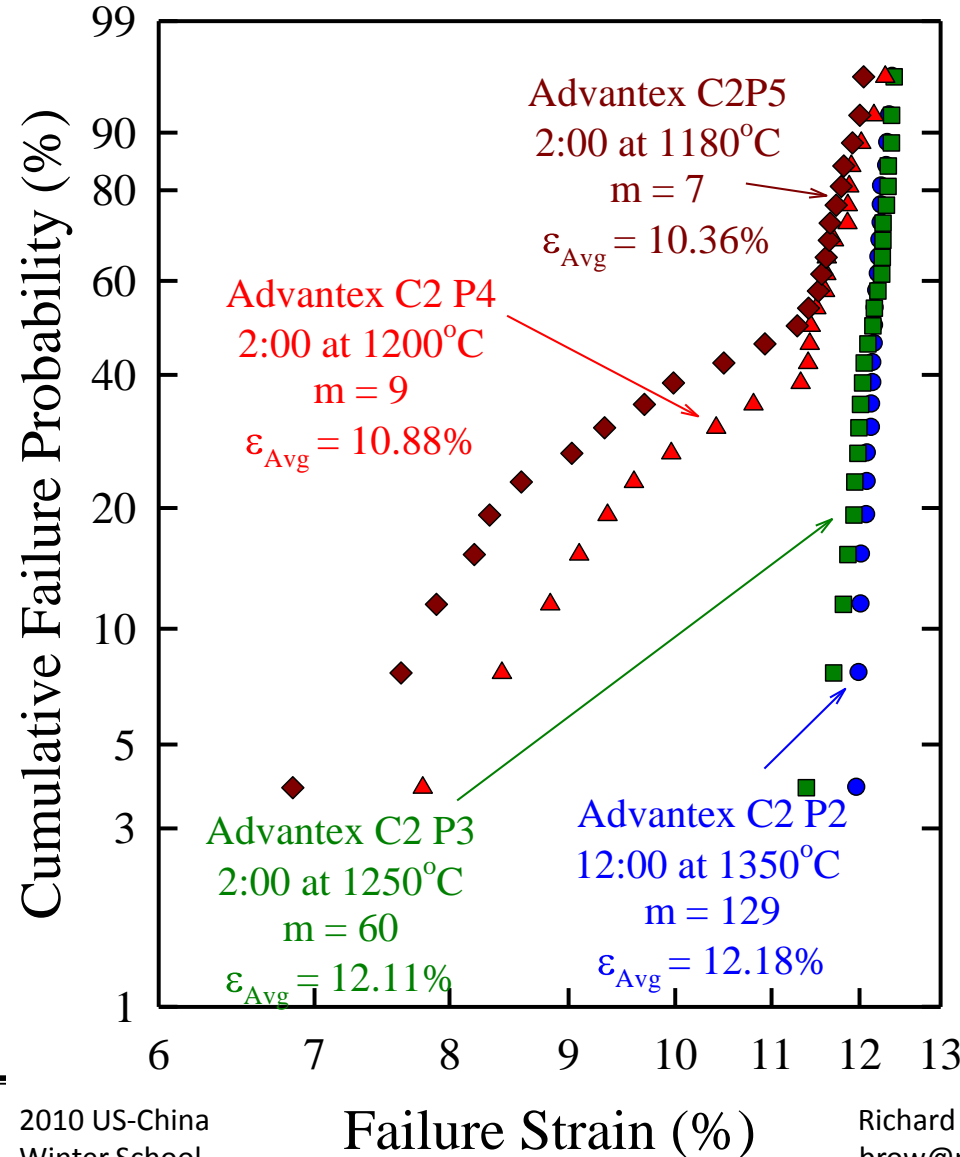
$$\sigma_f = \left( \frac{2 E \gamma}{\pi c} \right)^{\frac{1}{2}}$$



Recall processing effects

# Advantex Failure Strains

Weibull distributions of fibers drawn after different melt histories. Weibull modulus ( $m$ ), average failure strain ( $\epsilon_{Avg}$ ), and melt history are reported for each data set.



## Some questions related to Prof. Sen's lecture:

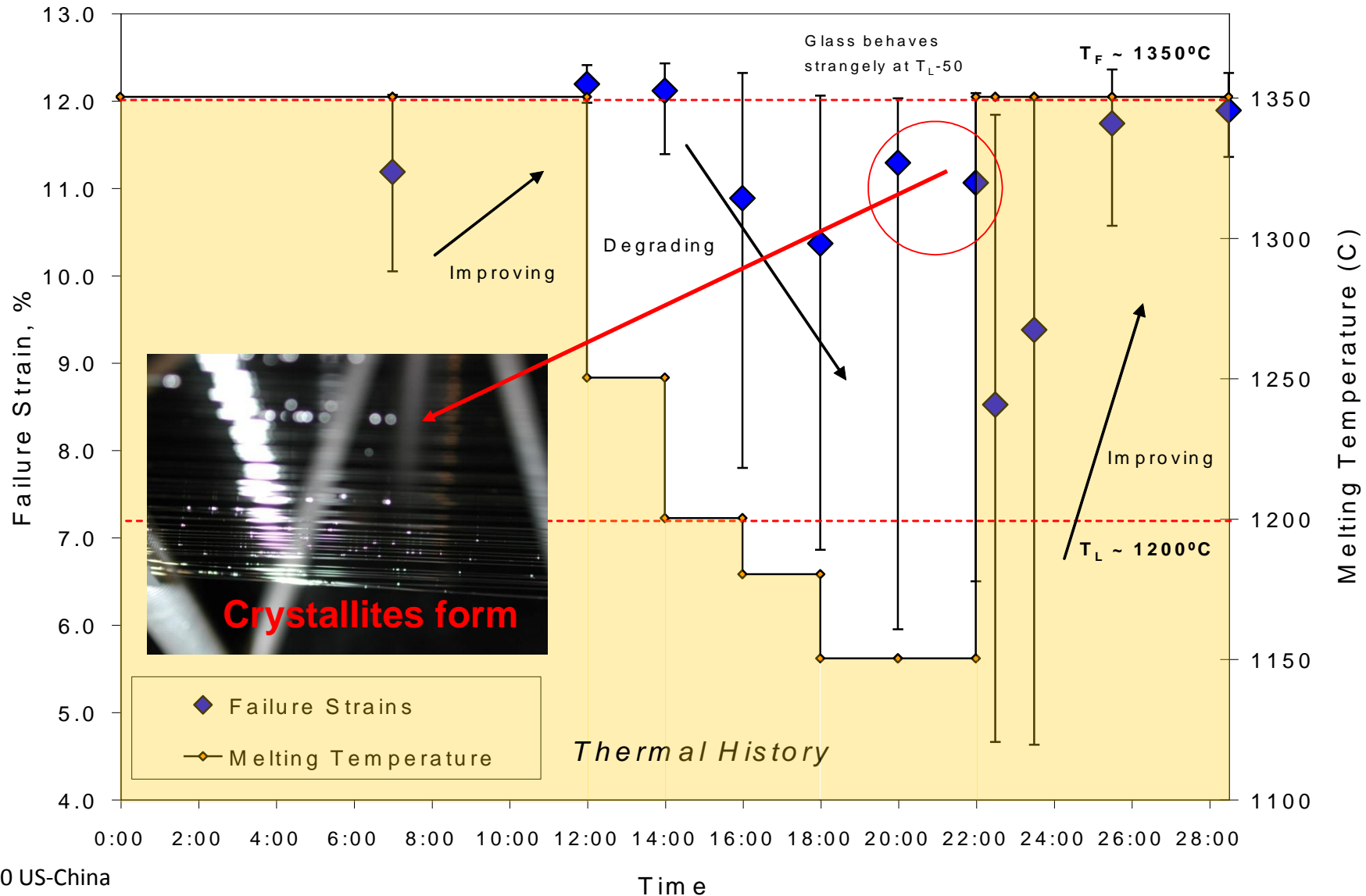
What type of heterogeneities might account for these distributions in failure strains?

What techniques could you use to characterize these heterogeneities?

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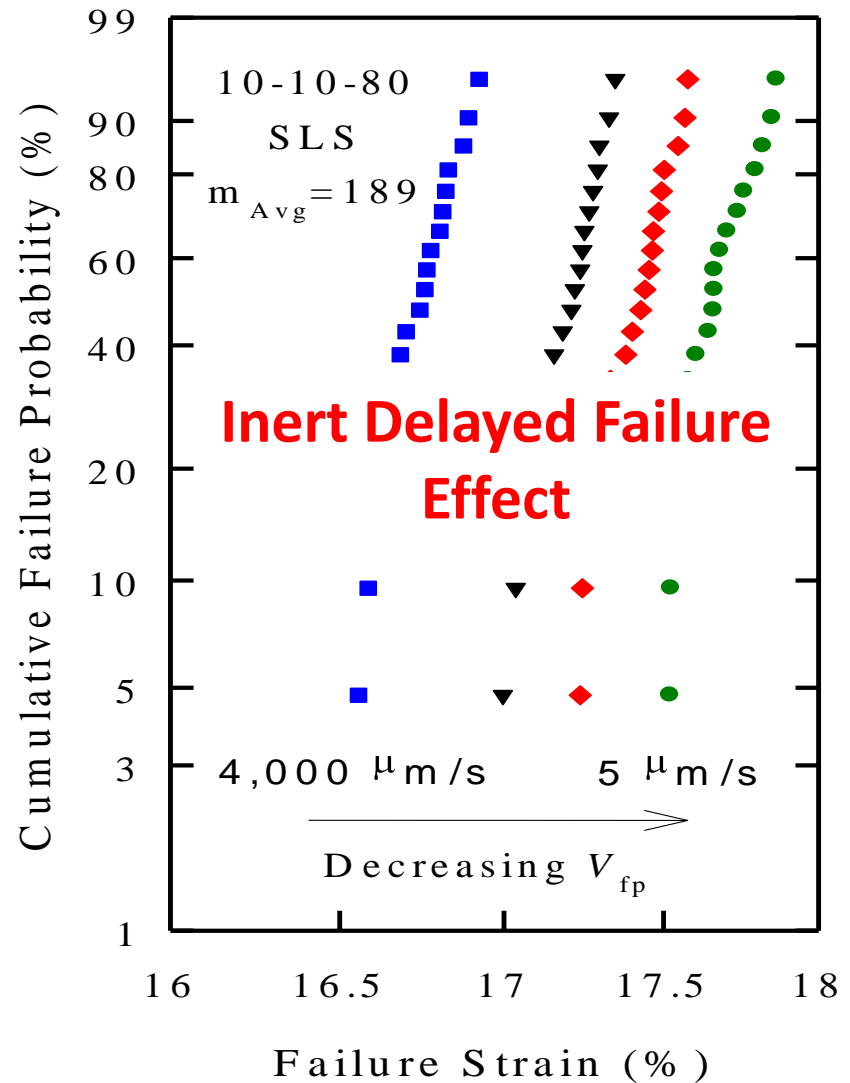
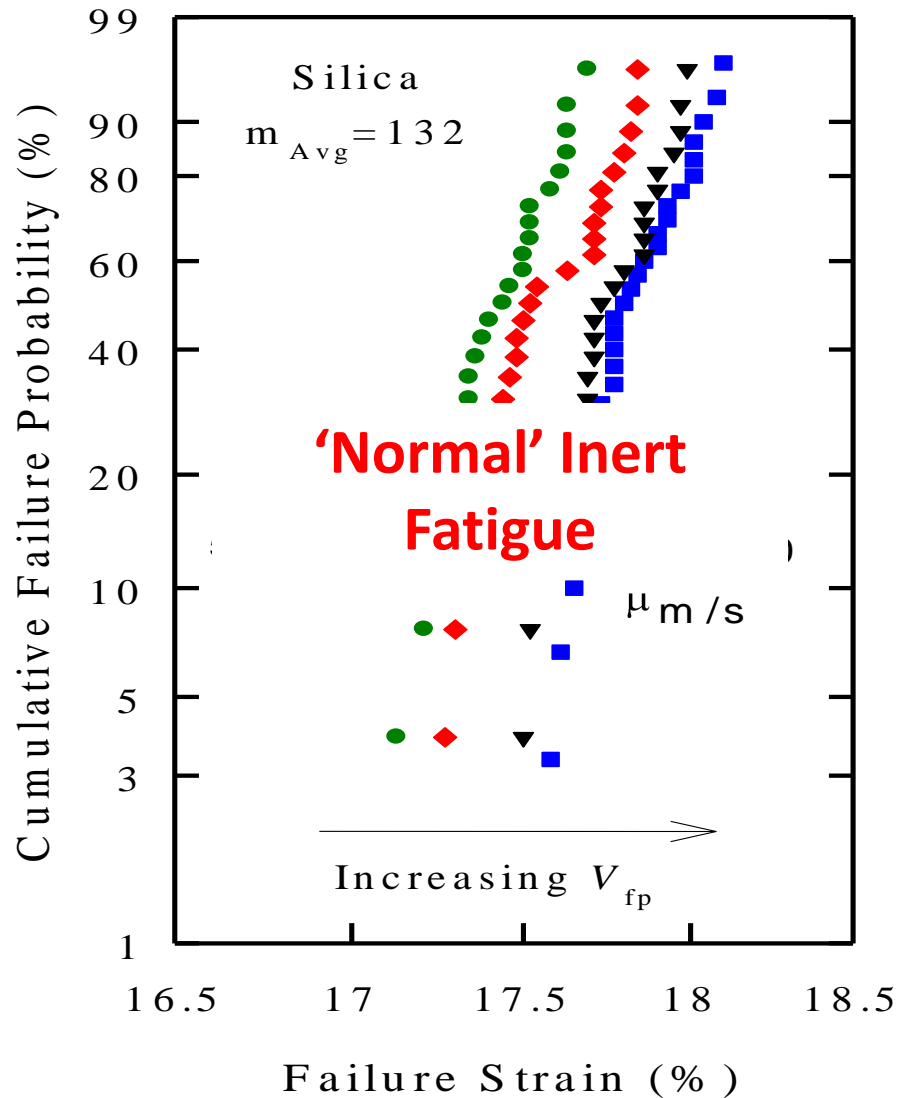
# Advantex Thermal History Summary

When the glass was melted at 1350°C, the failure strain distributions narrow with time. Failure strain distributions begin to broaden when melts are cooled to  $T_L + 50^\circ\text{C}$ .

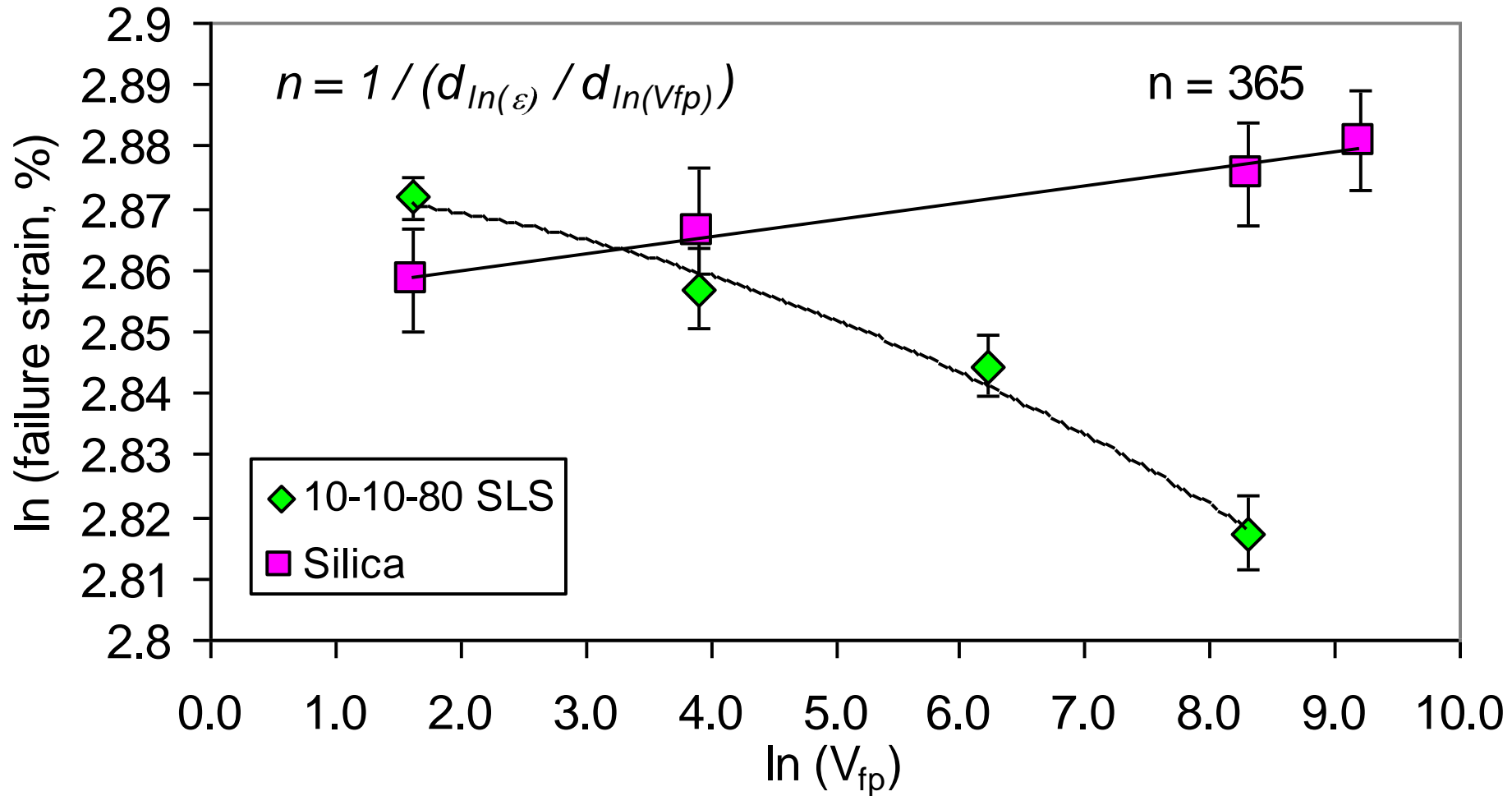


# How does glass break?

# Inert 'failure rate' studies

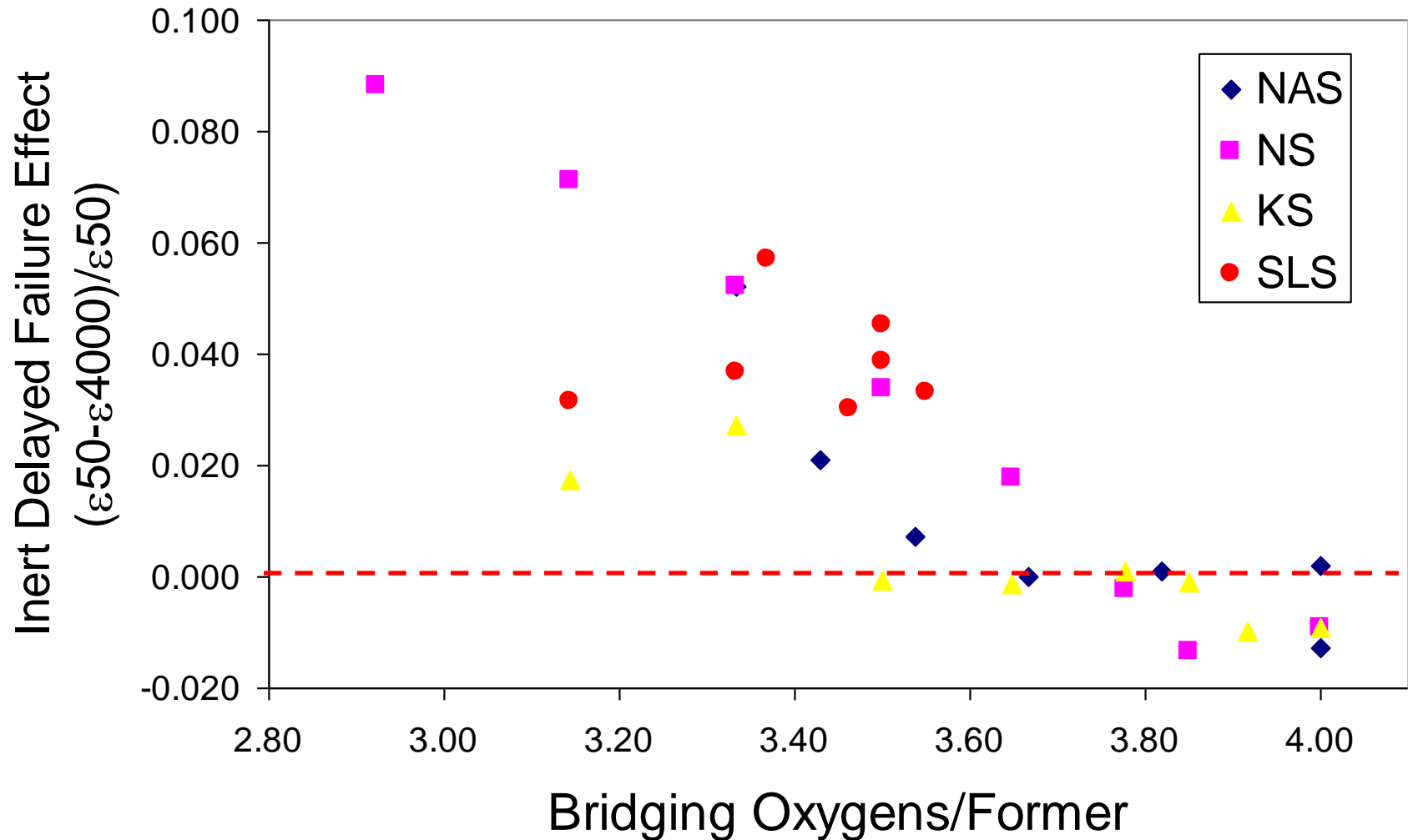


# Inert 'failure rate' studies

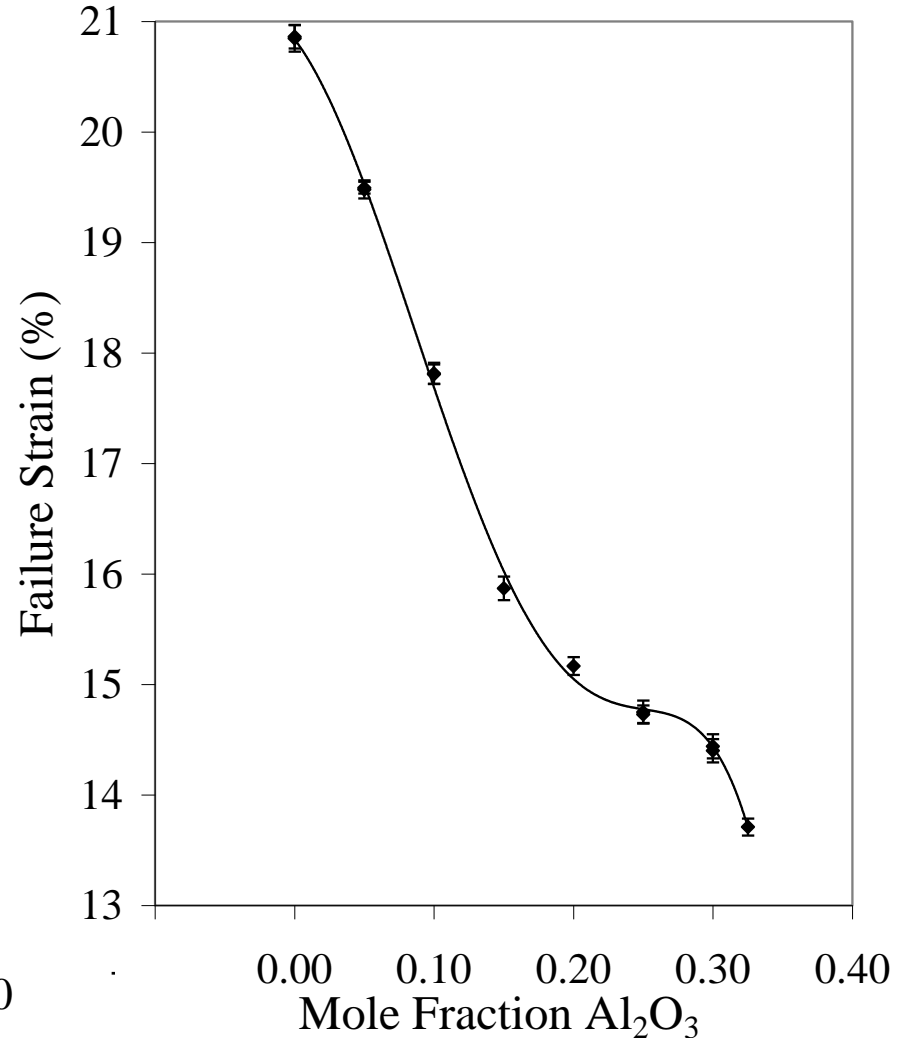
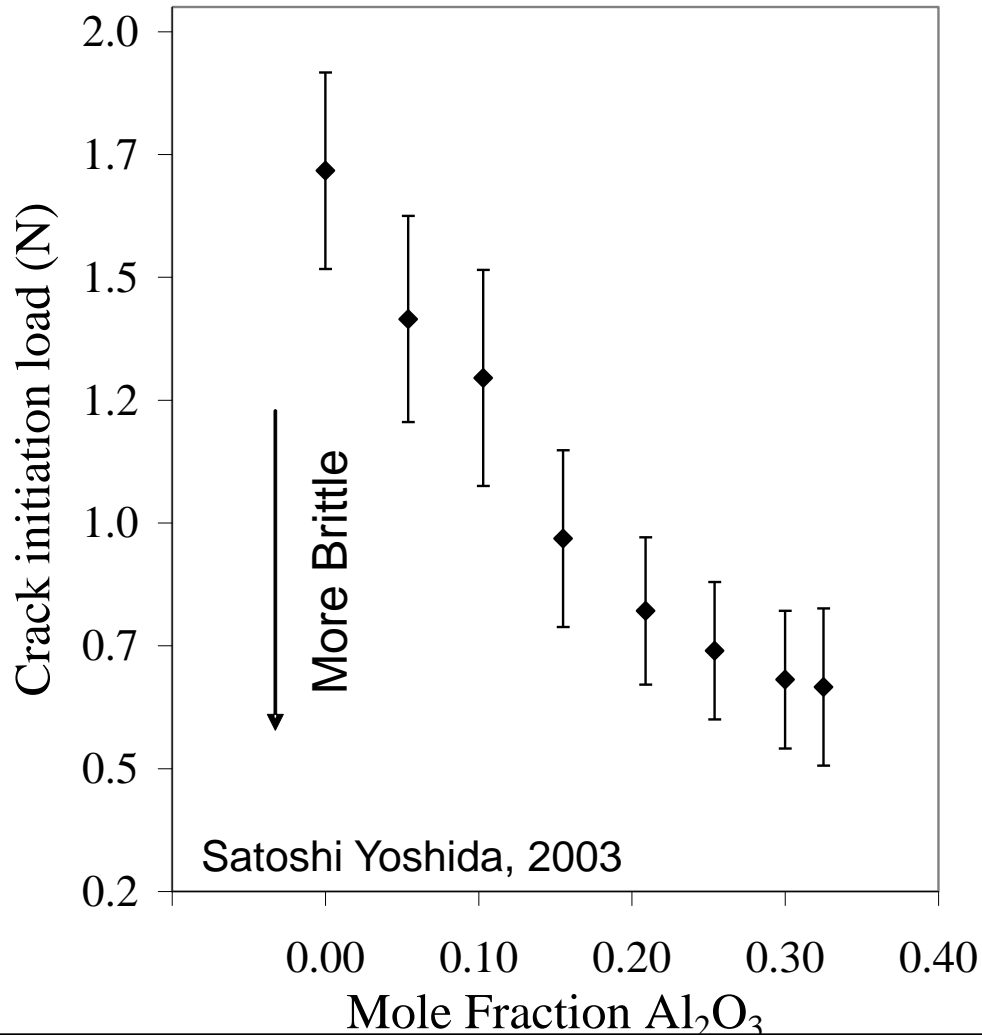
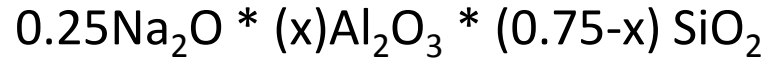




# The inert delayed failure effect depends on structure



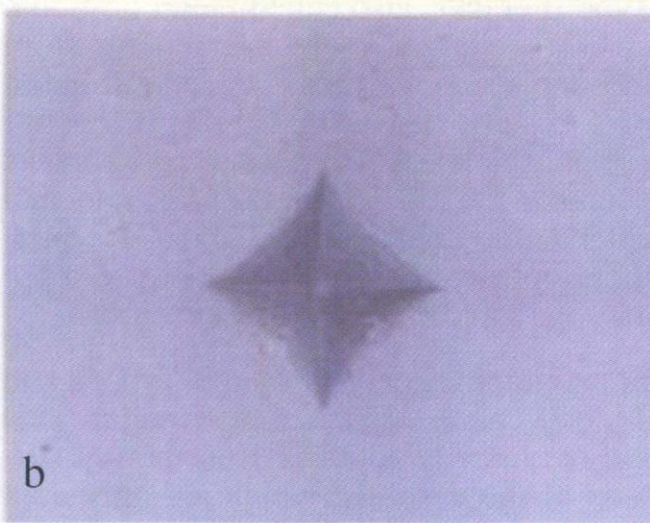
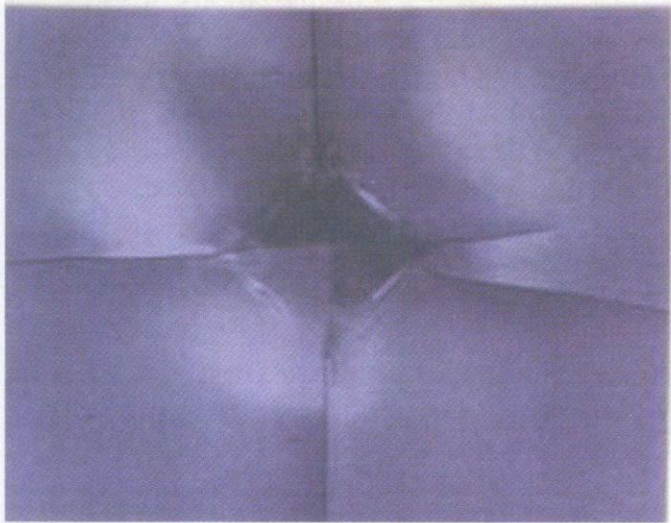
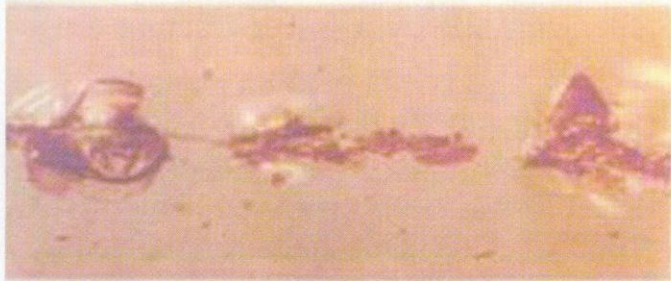
# Failure strain measurements also correlate with crack initiation loads



# Failure strain measurements may provide information about 'less brittle' glasses

Soda-lime-silica  
commercial window glass

Less brittle glass



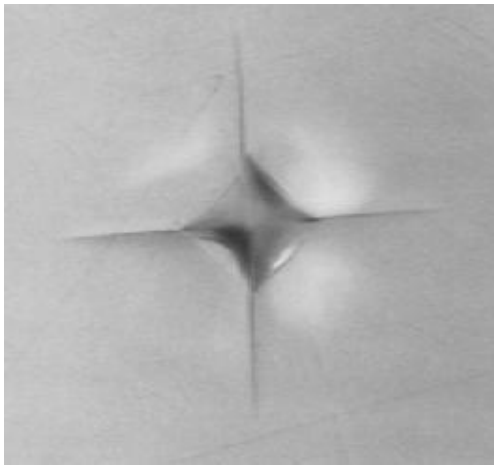
Setsuro Ito,  
2002

**Figure 4** Micrographs of surfaces scratched by steel roller cutter (a) and indented by a diamond tool (b) at (one)1kg load for a commercial window glass and a new less brittle glass.

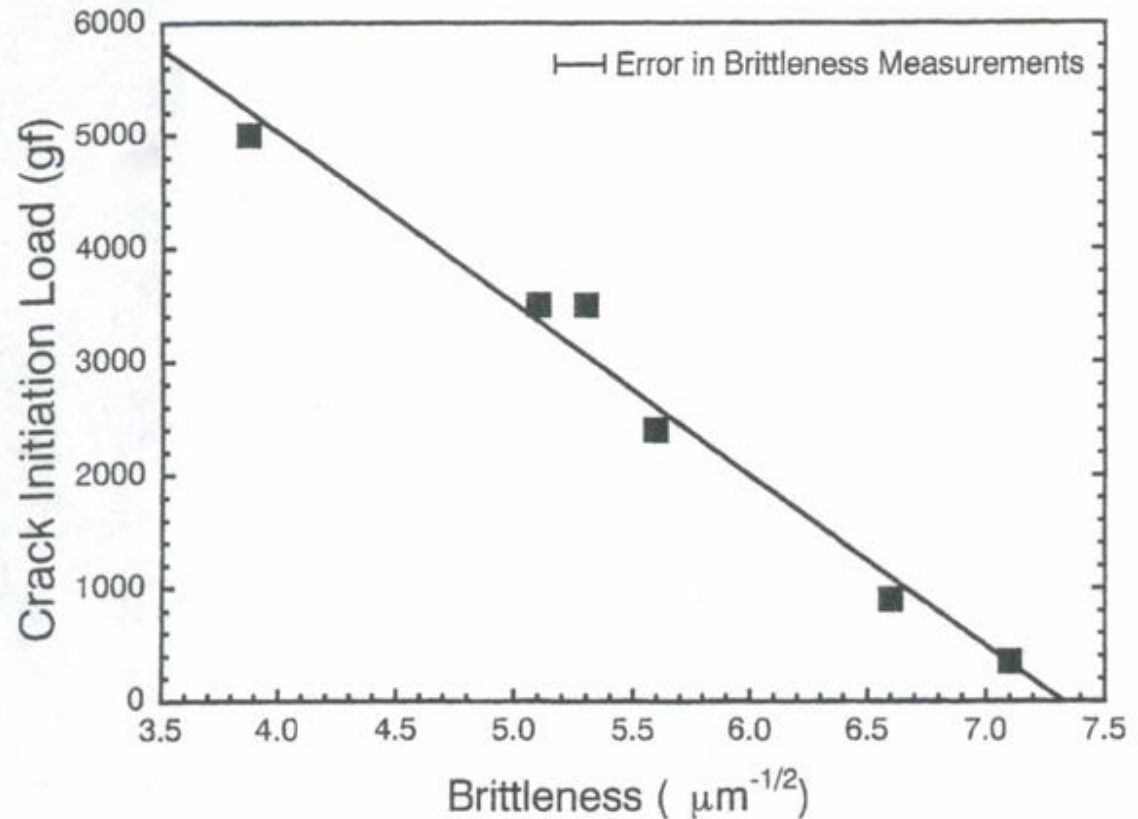
# “Brittleness parameter” has been determined from indentation measurements

$$\text{Brittleness } s \equiv B = 2.39 P^{1/4} \left( \frac{C}{a} \right)^{3/2}$$

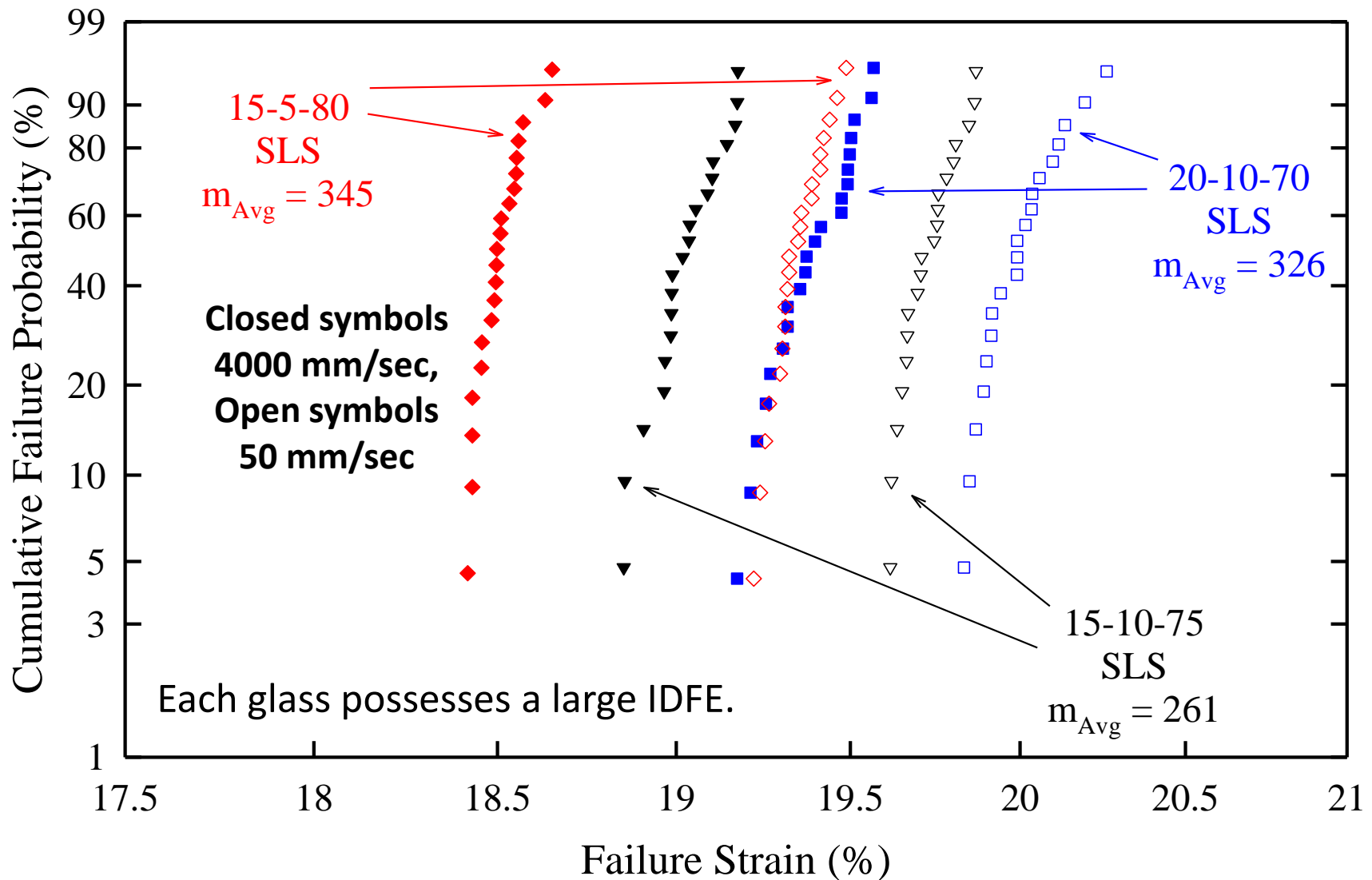
P is applied load, C is crack length, and a is Vickers indentation diagonal length



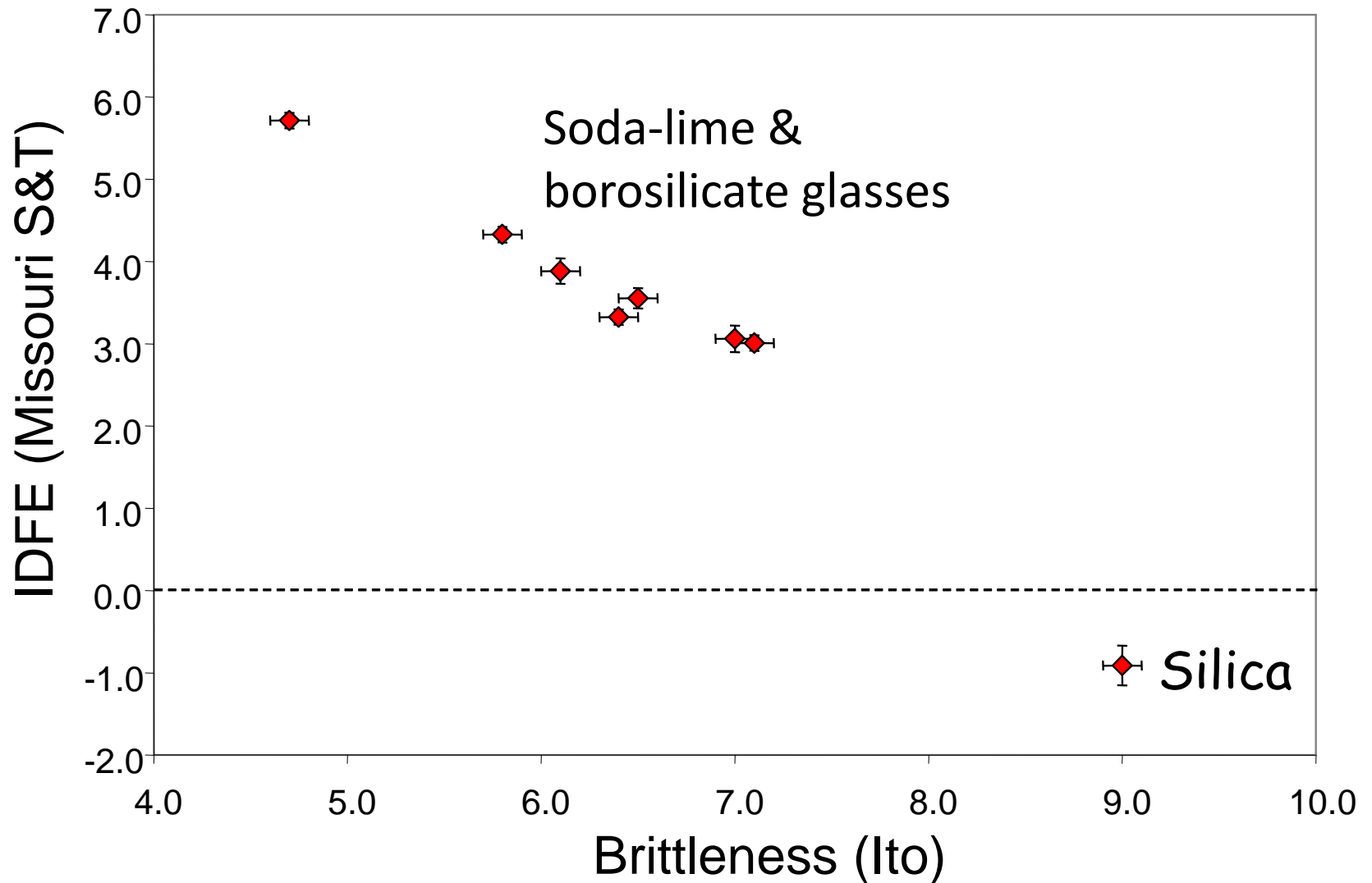
Setsuro Ito, 2002



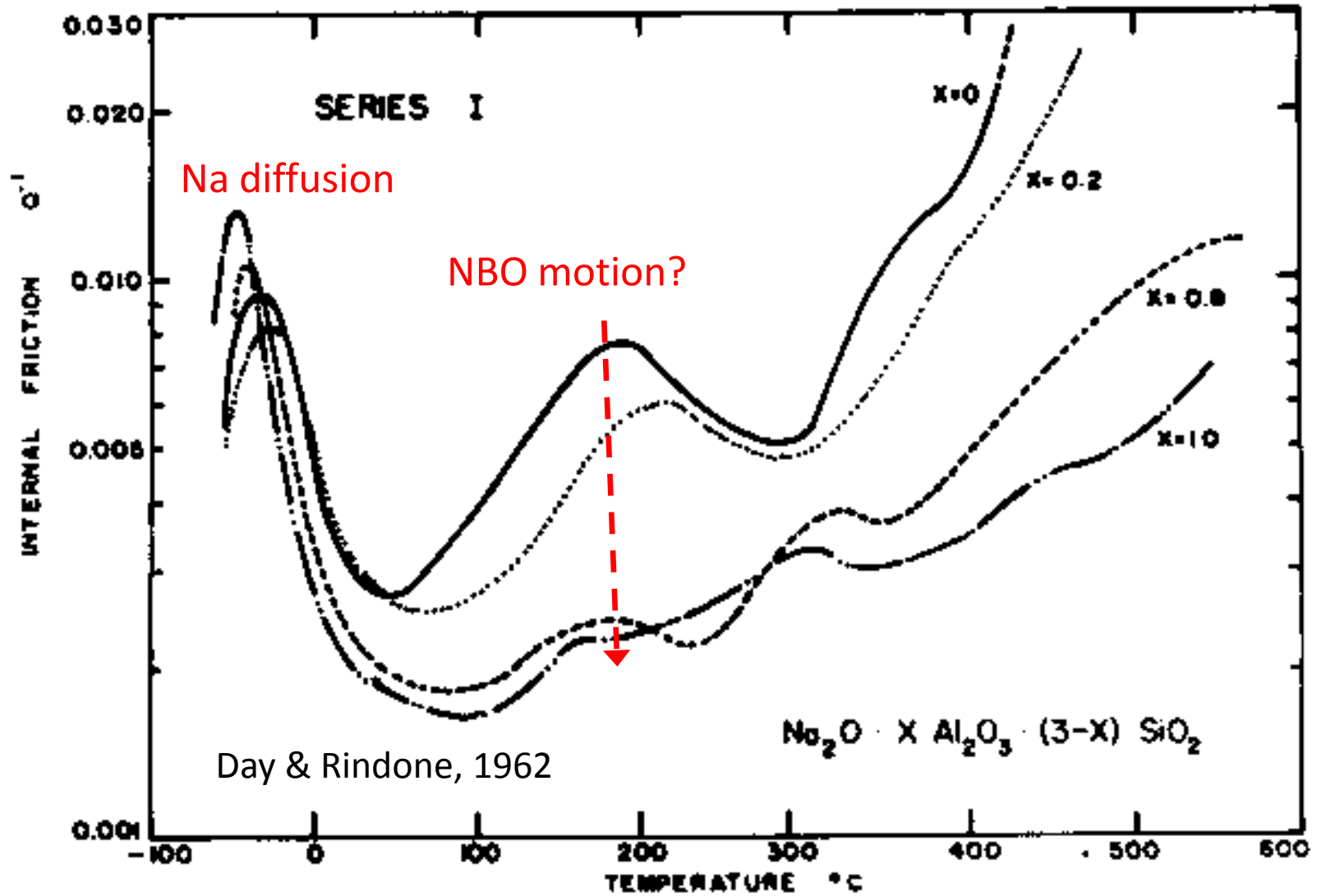
# Soda-lime silicate glasses exhibit the 'delayed failure' effect



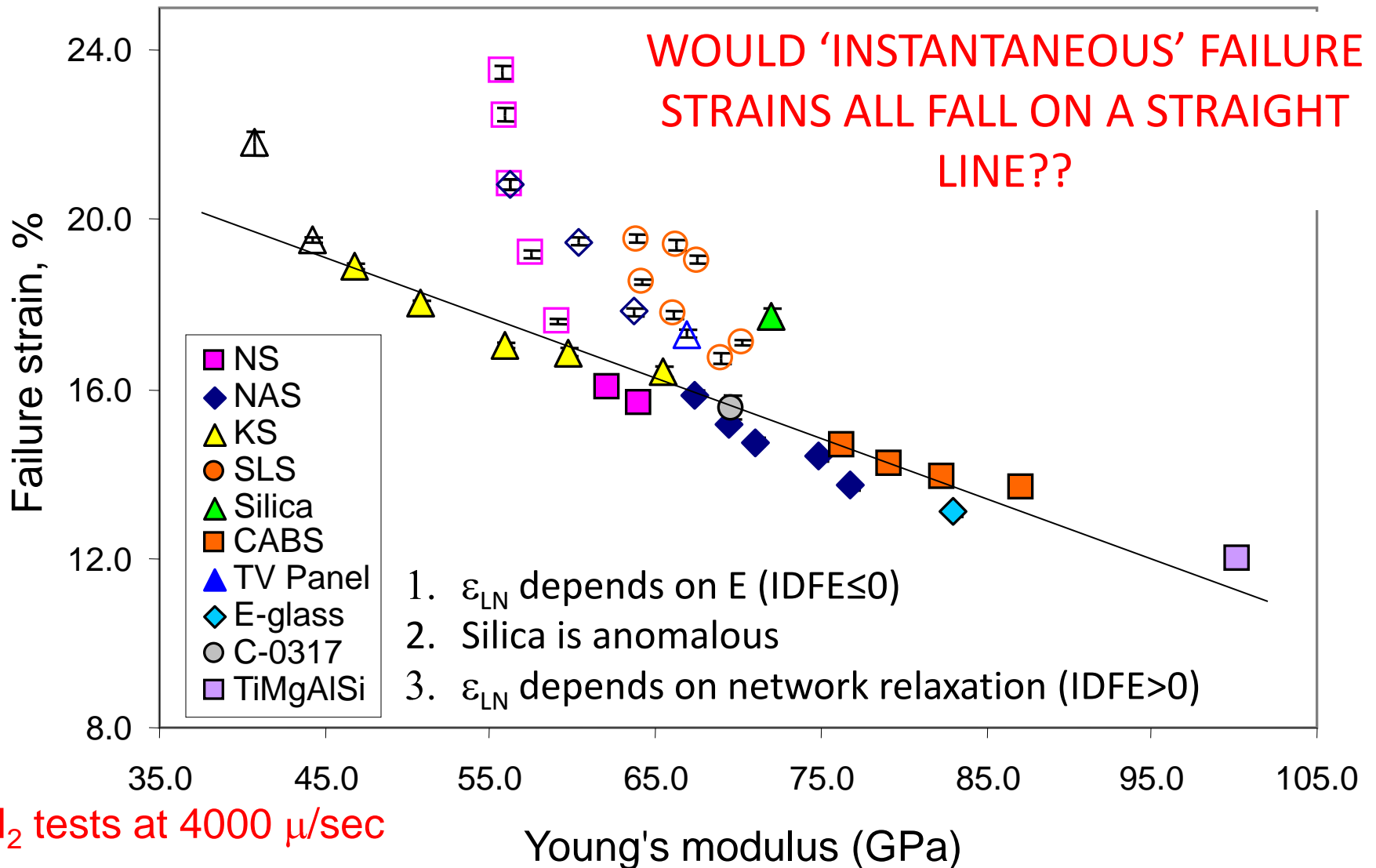
# 'Brittleness' and 'inert delayed failure' may be related



# Is IDFE related to network relaxation?



# Is there a universal dependence of glass failure characteristics on network structure?





# Summary

- Inert failure strains are sensitive to the composition/structure of glass fibers.
  - $\varepsilon_f$  increases when NBO's replace BO's
  - $\varepsilon_f$  increases when Young's modulus decreases
- Inert failure strains are dependent on the applied stressing rates ( $V_{fp}$ ).
  - Structure with non-bridging oxygens fail at larger strains with slower  $V_{fp}$ .
  - 'Framework' structures do not exhibit this 'inert delayed failure effect'.
  - Is IDFE due to relaxation of the network? What role is played by the NBO's?

The NSF/Industry/University *Center for Glass Research* sponsored the two-point bend studies at Missouri S&T

Nate Lower and Zhongzhi Tang collected the data

Chuck Kurkjian (retired, AT&T) inspired the work